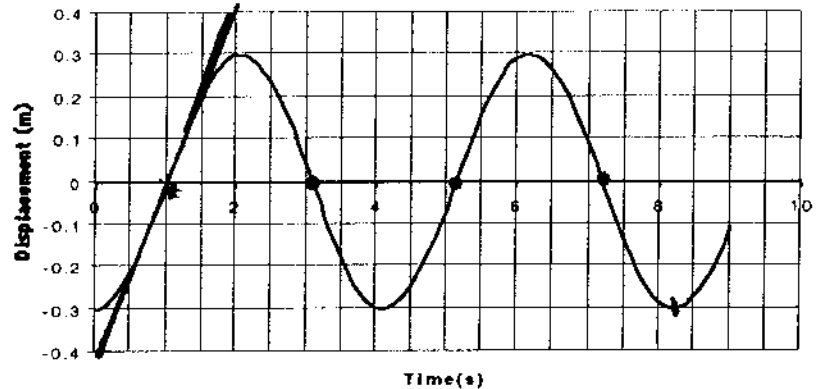


Physics 101 Test 2 SS02

Question 1

8

Displacement versus Time



An object moves with a displacement x as shown in the above diagram.

a) What is the amplitude of oscillation?

$$\text{Amplitude} = 0.30 \text{ m}$$

b) What is the period of an oscillation?

$$\text{Period} = 4.1 \text{ s}$$

c) What is the angular frequency of the oscillation?

$$\omega = \frac{2\pi}{T} = 1.53 \text{ rad/s}$$

d) What is the velocity at $t = 1.0 \text{ s}$?

Either $v_m = \omega A = 0.460 \text{ m/s}$ or slope $= \frac{0.8}{1.8} = 0.44 \text{ m/s}$

e) When is the acceleration zero?

$$\text{When } x = 0 \text{ at } 1.0, 3.1, 5.2, 7.2$$

f) What is the phase constant ϕ ?

$$x = A(\cos \omega t + \phi) \quad x = -A \text{ at } t = 0$$

$$-A = A \cos \phi \quad \cos \phi = -1 \quad \phi = \pi$$

g) Write an expression for the velocity of the motion as a function of time.

$$v = -\omega A \sin(\omega t + \phi) = -0.46 \sin(1.53t + \pi)$$

h) When is the Kinetic energy zero?

$$\text{When } x = \pm A \quad ; \quad t = 0, 2.1, 4.1, 6.2, 8.3 \text{ s}$$

Question 2

2) The cross-sectional area of a stream of water becomes smaller as the water falls from a tap.

Explain how this happens and also predict what you would see if water is shot upwards as from a fountain.

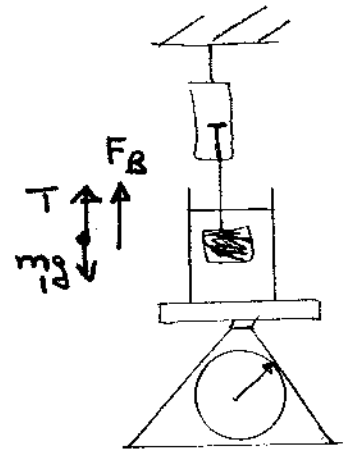
As water falls $|v| \uparrow$ & since $A v = \text{const}$ then $A \downarrow$

If water goes up $|v| \downarrow$ " " " " then $A \uparrow$

Physics 101 Test 2 SS02

Question 3

A beaker of mass 1.0 kg contains 2.0 kg of water and is sitting on a balance. A 2.0 kg block of aluminium (density $2.70 \times 10^3 \text{ kg/m}^3$) is suspended from a spring scale and is submerged in the water as shown



a) What is the volume of the aluminium block?

$$1 \quad V = \frac{m}{\rho} = \frac{2.0 \text{ kg}}{2.7 \times 10^3 \text{ kg/m}^3} = 7.41 \times 10^{-4} \text{ m}^3$$

b) What is the buoyant force acting on the aluminium block?

$$1 \quad F_B = \rho_{\text{water}} V_0 g = (1000 \frac{\text{kg}}{\text{m}^3}) (9.8 \frac{\text{m}}{\text{s}^2}) (7.41 \times 10^{-4} \text{ m}^3) = 7.26 \text{ N}$$

c) What is the reading on the spring scale?

$$1 \quad T = m_1 g - F_B = 12.3 \text{ N}$$

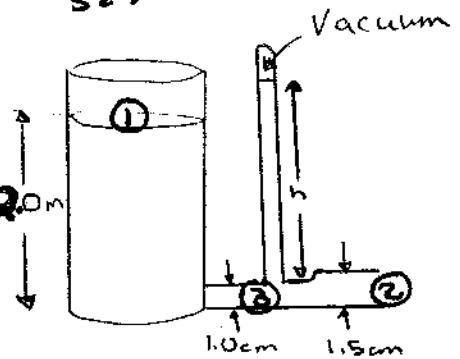
d) What is the reading on the balance?

2 Beaker (N 3rd law action reaction)

$$(m_b + m_w) g + F_B = (3.0 \text{ kg}) (9.8 \frac{\text{m}}{\text{s}^2}) + 7.26 \text{ N} = 36.7 \text{ N}$$

Question 4

A 1.0 m diameter tank is filled with water to a depth of 20 m and is open to the atmosphere at the top. The water drains first through a 1.0 cm diameter pipe and then through a 1.5 cm diameter pipe which is open to the atmosphere as shown



At point ① $v_1 = 0$ $P_1 = P_0$ $y_1 - y_2 = 20 \text{ m}$
 At point ② $v_2 = ?$ $P_2 = P_0$

$$\frac{1}{2} \rho v_2^2 + \rho g y_2 = \rho g y_1$$

$$v_2^2 = 2g(y_1 - y_2); \quad v_2 = 6.26 \text{ m/s}$$

a) What is the flow speed in the 1.5 cm diameter pipe?

2 6.26 m/s

b) What is the flow speed in the 1.0 cm diameter pipe?

$$A_1 v_1 = A_2 v_2 \quad v_3 = \frac{A_2}{A_3} v_2 = \left(\frac{1.5}{1.0}\right)^2 6.26 \text{ m/s} = 14.1 \text{ m/s}^2$$

c) What is the height, h, of the water in the sealed vertical tube?

2 $P_3 + \frac{1}{2} \rho v_3^2 = P_2 + \frac{1}{2} \rho v_2^2$ since $y_2 = y_3$

$$P_3 = 1.01 \times 10^5 \text{ Pa} + 500 \frac{\text{kg}}{\text{m}^3} (6.26^2 - 14.1^2) = 2.14 \times 10^5 \text{ Pa}$$

$$h = \frac{2.14 \times 10^5 \text{ Pa}}{9.8 \text{ m/s}^2 \times 1000 \text{ kg/m}^3} = 2.18 \text{ m}$$