

1. The amplitude and phase constant of an oscillator are determined by:

- a) the frequency
- b) the angular frequency
- c) the initial displacement alone
- d) the initial velocity alone
- e) both the initial velocity and the initial displacement.

2. An object hangs from a spring balance. The balance indicates 30 N in air, 20 N when the object is immersed in water and 24 N when it is immersed in an unknown liquid. The density of the unknown liquid equals the density of water multiplied by:

- Handwritten notes: I) $\rho_{H_2O} g V_{obj} = 10$ $V_{obj} = \frac{10}{\rho_{H_2O} g}$
 II) $\rho_{u} g V_{obj} = 6$ $\rho_u = \frac{6}{g} \frac{g}{10} \rho_{H_2O}$
- a) 10/4
 - b) 6/10
 - c) 24/20
 - d) 4/10
 - e) 10/30

3. A guitar string vibrates at a frequency of 440 Hz. A point on its centre moves in Simple Harmonic Motion with an amplitude of 3.0 mm and a phase constant of zero.

a) Write an equation for the position of the centre of the string as a function of time.

1
$$X = (3.0 \times 10^{-3} \text{ m}) \cos 880\pi t$$

b) What are the maximum values of the magnitudes of the velocity and acceleration of this point.

2
$$\omega A = 2\pi 440 \times 3.0 \times 10^{-3} = 8.3 \text{ m/s}$$

$$\omega^2 A = 2.3 \times 10^4 \text{ m/s}^2$$

4. A 0.400 kg object is undergoing SHM on the end of a horizontal spring with force constant 400 N/m. When the object is 0.012 m from its equilibrium position, it is observed to have speed 0.300 m/s. What is:

a) the total energy of the object at any point in its motion?

1
$$U_{\text{total}} = \frac{1}{2} k x^2 + \frac{1}{2} m v^2$$

$$= 0.0288 + 0.018 = 0.0468 \text{ J}$$

b) the amplitude of the motion?

1
$$\frac{1}{2} k A^2 = 0.0468 \text{ J}$$

$$A = 0.0153 \text{ m}$$

c) the maximum speed attained by the object during its motion?

1
$$\frac{1}{2} m v_{\text{max}}^2 = 0.0468 \text{ J}$$

$$v_{\text{max}} = 0.484 \text{ m/s}$$

5. A single ice cube of mass 8.40 g floats in a glass that is completely full of 350 cm³ of water. ($\rho_{\text{ice}} = 0.917 \times 10^3 \text{ kg/m}^3$)

a) What volume of water does the ice cube displace?

$$1 \quad F_B = mg = \rho_f g V_f \quad V_f = \frac{m}{\rho_f} = 8.4 \times 10^{-6} \text{ m}^3$$

b) When the ice cube has melted, has any water overflowed? If so how much? If not explain why this is so.

1 Volume water in ice cube $\frac{8.4 \times 10^{-3} \text{ kg}}{1000 \text{ kg/m}^3} \rightarrow$ as in a no water overflows

c) Suppose the water in the glass had been very salty water of density 1050 kg/m³. What volume of the salt water would a 8.40 g ice cube displace?

$$1 \quad V_f = \frac{8.4 \times 10^{-3} \text{ kg}}{1050 \text{ kg/m}^3} \rightarrow \text{fluid displaced } 8.0 \times 10^{-6} \text{ m}^3$$

d) For the cube in salty water, when the ice cube has melted, has any water overflowed? If so how much?

1 volume water in ice cube $8.4 \times 10^{-6} \text{ m}^3$
 $\therefore 0.4 \times 10^{-6} \text{ m}^3$ overflows

6. Water flows out steadily out of an open tank. The elevation of point 1 is 10.0 m and the elevation of points 2 and 3 is 2.00 m. The cross-sectional area at point 2 is 0.0300 m²; and at point 3 it is 0.0150 m². The area of the tank is very large in comparison with the cross sectional area of the pipe. If Bernoulli's equation applies determine:

a) The speed of the water at point 3

$$V_1 = 0 \quad h = 8 \text{ m}$$

$$2 \quad V_3 = \sqrt{2gh} = 12.5 \text{ m/s}$$

b) the speed of the water at point 2

$$A_2 v_2 = A_3 v_3$$

$$v_2 = \frac{A_3}{A_2} v_3 = \frac{0.015}{0.030} \times 12.52 = 6.26 \text{ m/s}$$

c) the gauge pressure at point 2

$$P_3 = \text{atm.}$$

$$P_2 + \frac{1}{2} \rho v_2^2 = P_3 + \frac{1}{2} \rho v_3^2 \leftarrow \text{same height}$$

$$P_2 - P_3 = \frac{1}{2} (1000) (12.52^2 - 6.26^2)$$

$$= 5.88 \times 10^4 \text{ Pa}$$

Gauge pressure is $5.88 \times 10^4 \text{ Pa}$.

