

# LAST TIME: to describe motion of objects

Introduce coordinates: choose origin, +ve directions  
describe motion by  $(x(t), y(t), z(t))$

Useful concepts:

Velocity:  $v_x = \frac{\Delta x}{\Delta t}$  in limit where  $\Delta t \rightarrow 0$

→ similar for  $v_y, v_z$   
- (defines derivative  $\frac{dx}{dt} = \lim_{\delta t \rightarrow 0} \frac{x(t+\delta t) - x(t)}{\delta t}$ )

$v(t)$ : slope of  $x(t)$  graph at time  $t$

acceleration:  $a_x = \frac{\Delta v_x}{\Delta t}$  in limit where  $\Delta t \rightarrow 0 \equiv \frac{dv}{dt}$

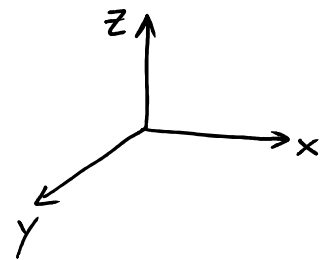
$a(t)$ : slope of  $v(t)$  graph at time  $t$

## PHYSICS:

1st observation: Need 3 space coordinates to describe locations of objects (plus 3 more to describe their orientation in space - see clicker Q. answer)

We live in 3 dimensions

Extra coordinate: time



locations can change w. time:

$(x(t), y(t), z(t)) \leftarrow 3 \text{ functions} = 3 \times \text{infinity numbers}$

PHYSICS allows us to predict these from

$(x(0), y(0), z(0))$  and  $(v_x(0), v_y(0), v_z(0))$  + knowledge of object's environment.

Simplest environment: outer space  
(far from planets, etc...)

empty space: lots of SYMMETRY

move in any direction by any amount:  
looks the same TRANSLATIONAL  
SYMMETRY

turn in any direction by any angle:  
looks the same ROTATIONAL  
SYMMETRY

wait some amount of time:  
looks the same TIME TRANSLATION  
SYMMETRY

(also: "boost" symmetry - no perceptible  
difference if we are moving at  
constant velocity)

EMMY NOETHER 1882-1935

proved that **SYMMETRIES** imply **CONSERVATION LAWS**

translation symmetry  $\Rightarrow$  conservation of  
momentum

time translation sym  $\Rightarrow$  conservation of  
energy

rotation sym  $\Rightarrow$  cons. of angular momentum

e.g.

## CONSERVATION OF MOMENTUM

same story for  
y, z

for an object in an environment with translational symmetry in the x direction, there is a quantity  $p_x$  associated with the object that is constant (unchanging) in time

Small velocities  
 $|v| \ll 3 \times 10^8 \text{ m/s}$

approximately equal to

$$p_x \approx m v_x$$

generally

$$p_x = \frac{m v_x}{\sqrt{1 - \frac{v_x^2 + v_y^2 + v_z^2}{c^2}}}$$

Constant  $\vec{p} = (p_x, p_y, p_z)$  implies constant  $\vec{v}$

Conclusion: for an isolated object (i.e. no interactions w. other things)  $\vec{v}$  is constant in time

## NEWTON'S 1ST LAW