



UNIVERSITY OF BRITISH COLUMBIA



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# ARPES on Correlated Electron Systems

CUSO Lecture – Lausanne 02/2011



## Outline Part II

- $\text{Sr}_2\text{RuO}_4$ : A Fermi liquid + spin-orbit coupling
- HTSC: Mott gap and strong correlations
- Sudden approx. and QP renormalization
- HTSC: The fate of quasiparticle strength
- References, slides, and lecture notes

CUSO Lecture – Lausanne 02/2011





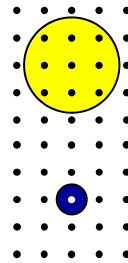
## Outline Part II

$\text{Sr}_2\text{RuO}_4$ : A Fermi liquid  
with spin-orbit coupling

CUSO Lecture – Lausanne 02/2011

# Strongly Correlated Electron Systems

d - f  
open  
shells  
materials



$U \ll W$   
Charge fluctuations

$U \gg W$   
Spin fluctuations

I	II	IIIb	IVb	Vb	VIb	VIIb	VIIIb	Ib	IIb	III	IV	V	VI	VII	0		
H															He		
Li	Be									B	C	N	O	F	Ne		
Na	Mg									Al	Si	P	S	Cl	Ar		
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba	La*	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
Fr	Ra	Ac**	Rf	Db	Sg	Bh	Hs	Mt									
Lanthanides *		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu		
Actinides **		Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr		

Degrees of  
freedom

Charge / Spin  
Orbital  
Lattice

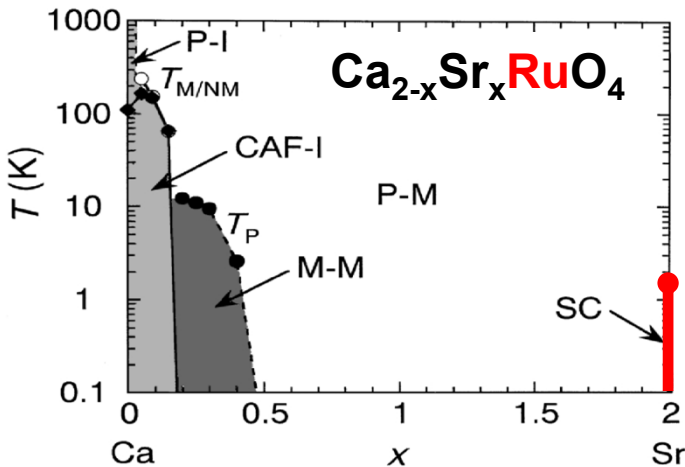
Control

parameters

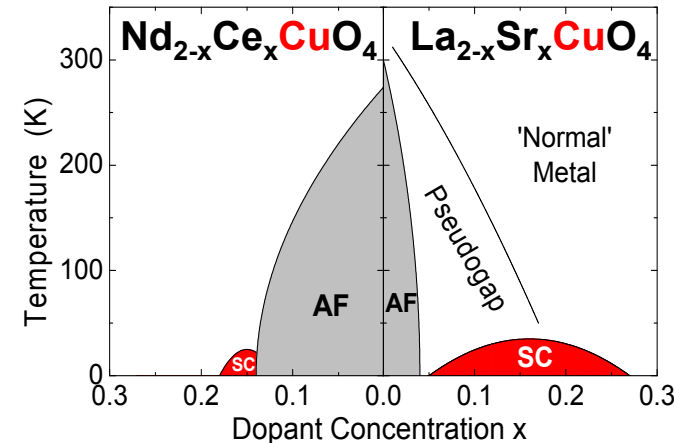
Bandwidth ( $U/W$ )

Band filling

Dimensionality

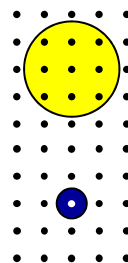


- Kondo
- Mott-Hubbard
- Heavy Fermions
- Unconventional SC
- Spin-charge order
- Colossal MR



# Strongly Correlated Electron Systems

d - f  
open  
shells  
materials



$U \ll W$   
Charge fluctuations

$U \gg W$   
Spin fluctuations

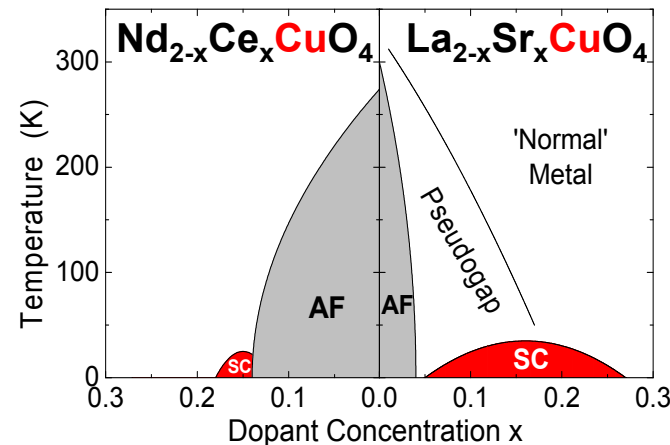
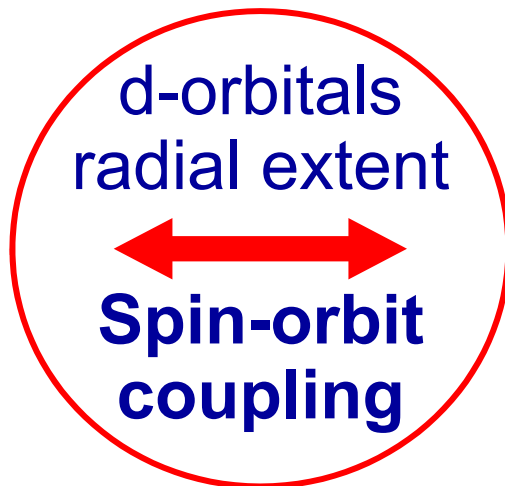
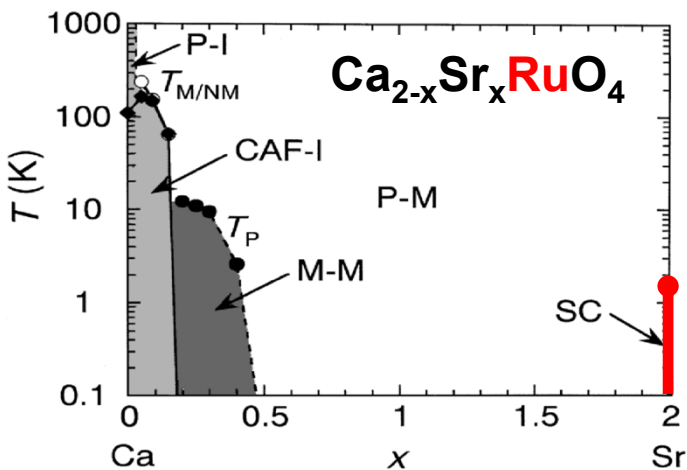
I	II	IIIb	IVb	Vb	VIb	VIIb	VIIIb	Ib	IIb	III	IV	V	VI	VII	0		
H															He		
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Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
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Control  
parameters

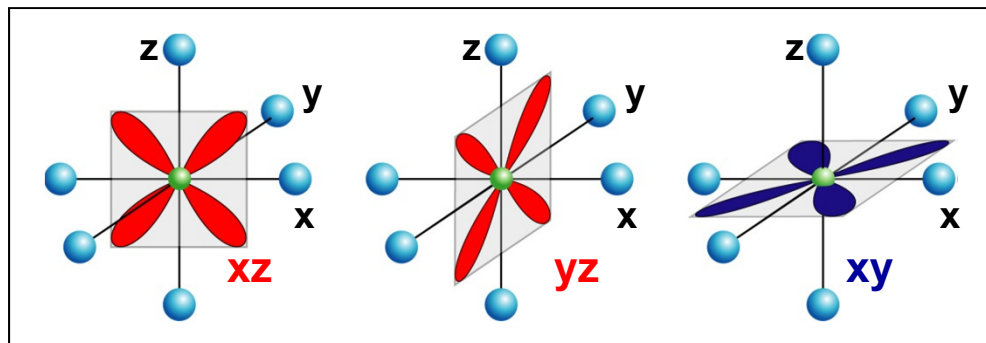
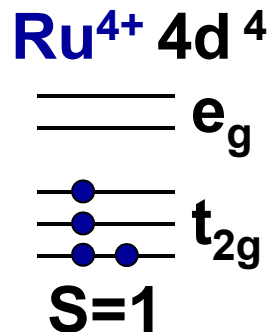
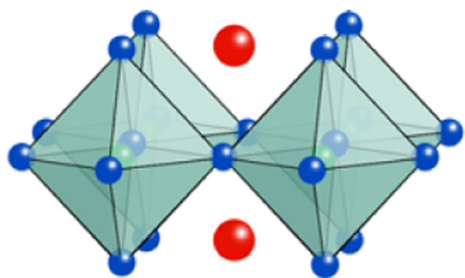
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Band filling  
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Degrees of  
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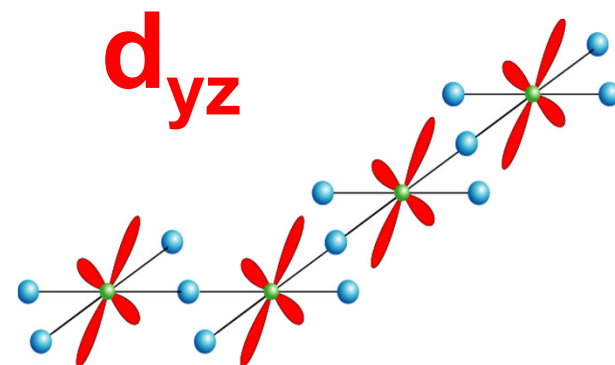
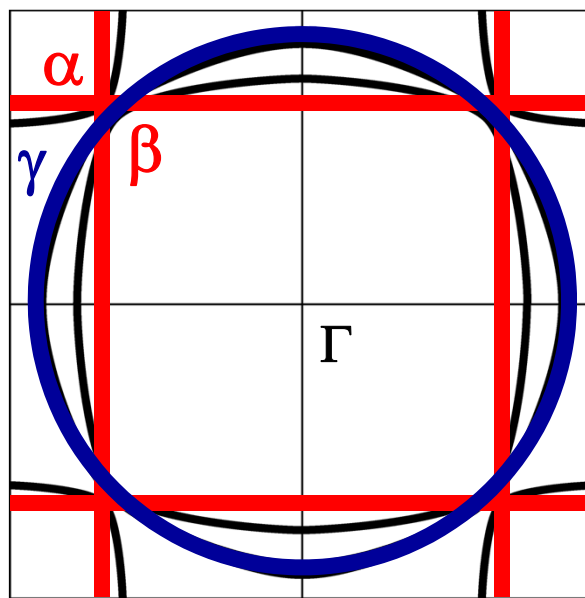
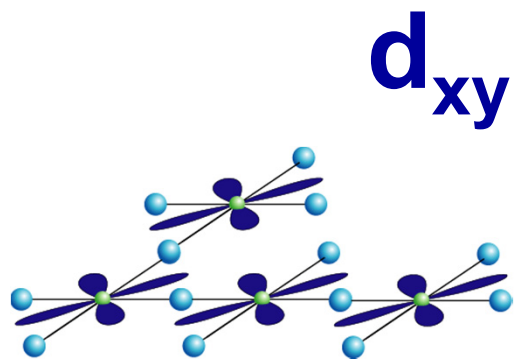
Charge / Spin  
Orbital  
Lattice



# 1D ( $d_{xz,yz}$ ) versus 2D ( $d_{xy}$ ) Superconductivity ?



► Band structure calculation: **3 t<sub>2g</sub>** bands crossing **E<sub>F</sub>**



# Eigenstates with Spin-Orbit Coupling

Starting from degenerate  $t_{2g}$  orbitals

$$\sqrt{1/2} (-d_{xz} - i d_{yz}) = d_1$$

$$\sqrt{1/2} (d_{xz} - i d_{yz}) = d_{-1}$$

$$d_{xy}$$

3-orbitals with orbital momentum 0, +/- 1  
like  $p$ -orbitals

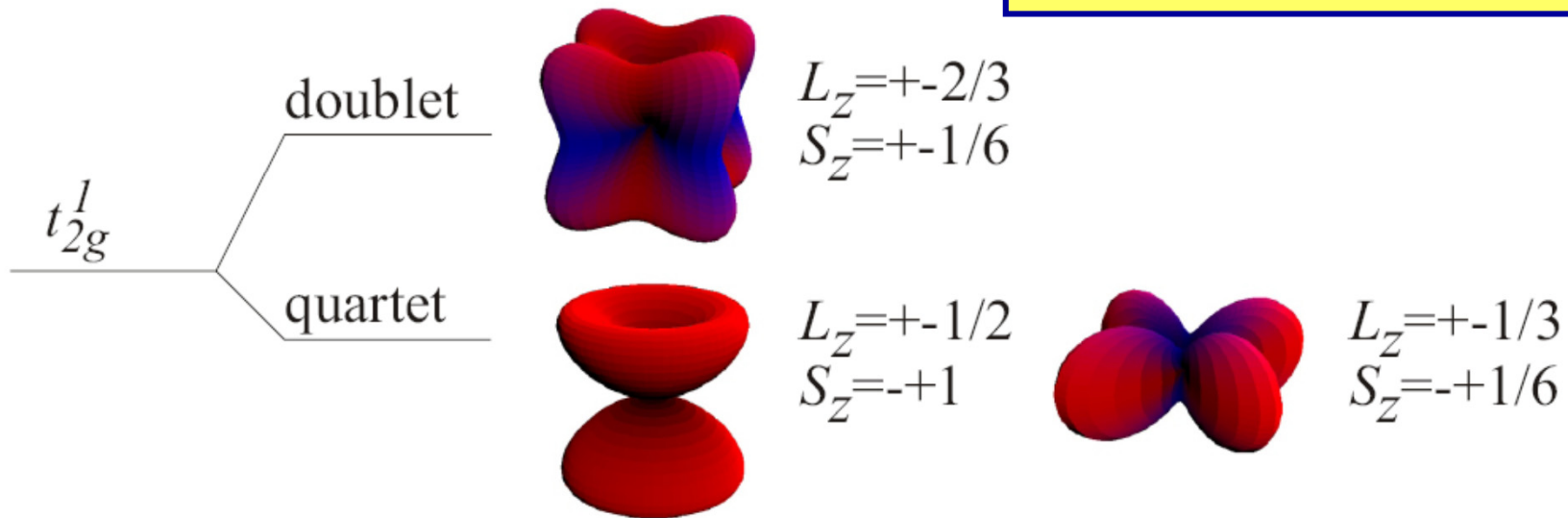
$$H = \zeta \sum_i \mathbf{l}_i \cdot \mathbf{s}_i$$

Atomic relativistic SOC

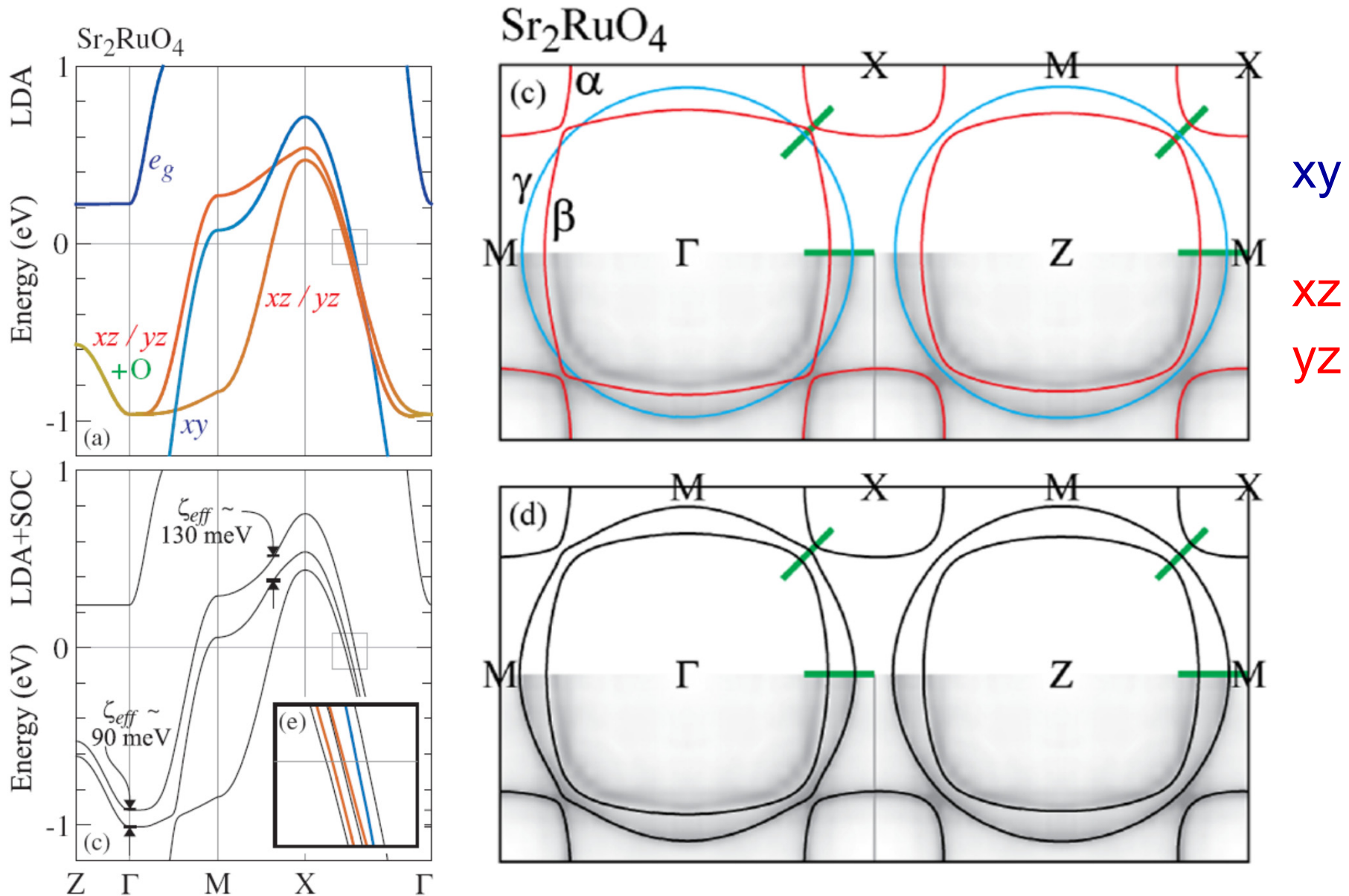
$$\text{Ru}^{4+} \quad \zeta = 161 \text{ meV}$$

$$\text{Rh}^{4+} \quad \zeta = 191 \text{ meV}$$

Earnshaw, JCS **601**, 3132 (1961)

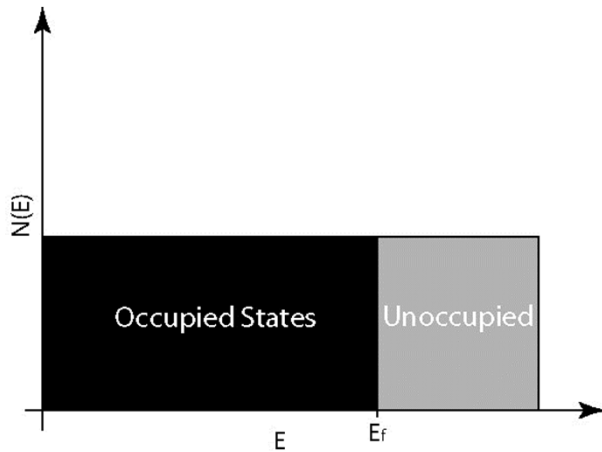


# Importance of Spin-Orbit Coupling in 4d Oxides

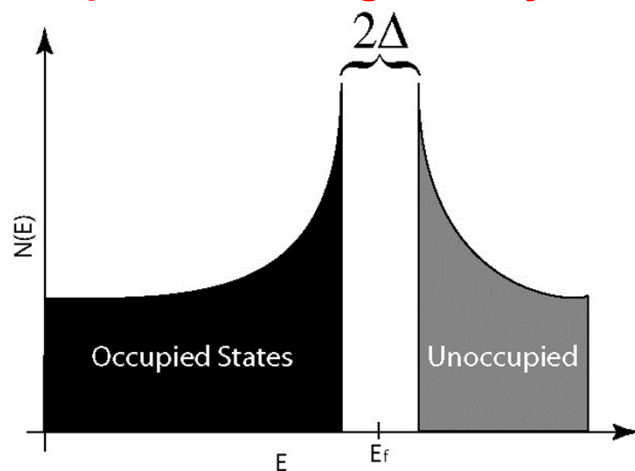


# “Classic Low-temperature” Superconductors

Metallic Density of States



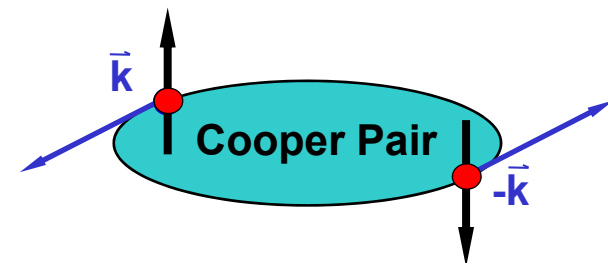
Superconducting Density of States



**Superconductivity** can only be seen on low energy scales and needs **high resolution**!

## Superconductivity

2-electron  
bound state

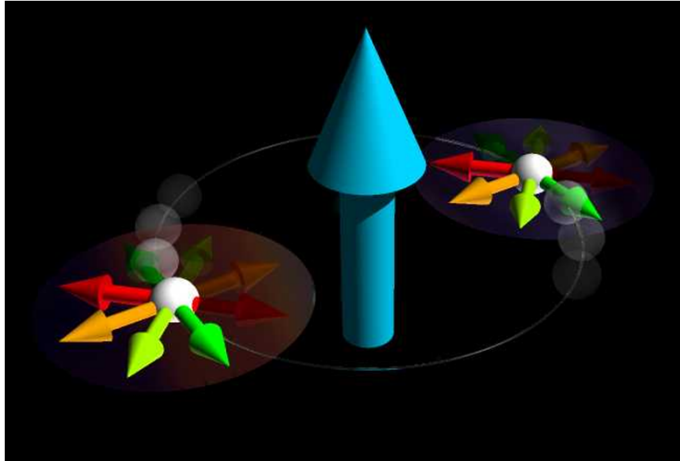


spin-singlet pairing

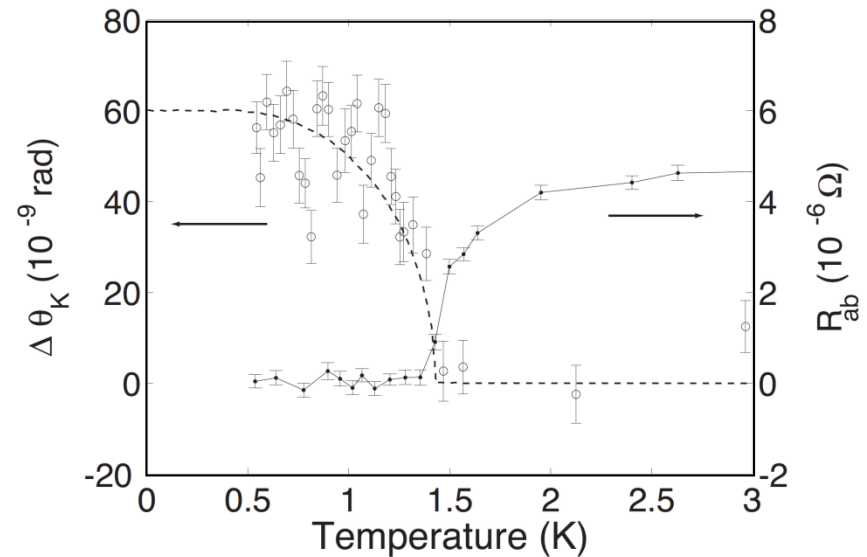


# Spin-Triplet Superconductivity in $\text{Sr}_2\text{RuO}_4$

Mackenzie & Maeno, RMP **75**, 657 (2003)



Xia et al., PRL **97**, 167002 (2006)



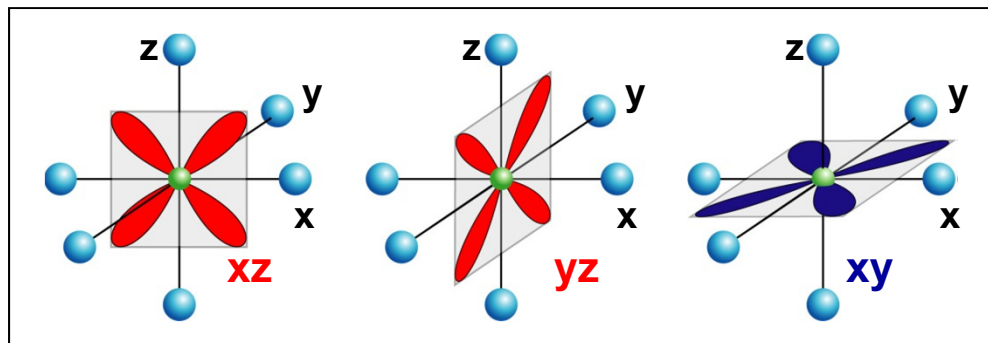
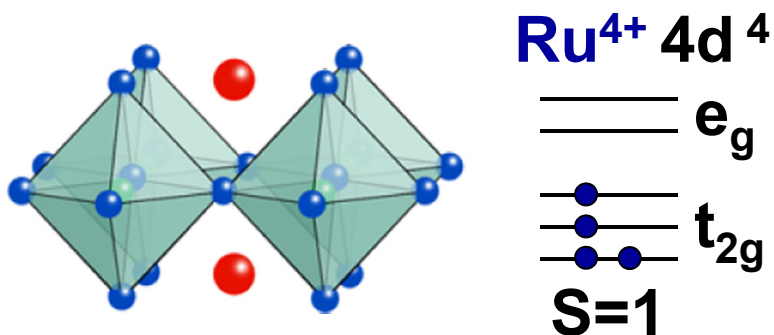
**Weak  
SOC**

- Equal **spin-triplet pairing** for any quantization axis
- **Single-band** ( $d_{xy}$ ) isotropic p-wave order parameter
- **TRSB**:  $p_x + ip_y$  with no disorder gives zero Kerr signal

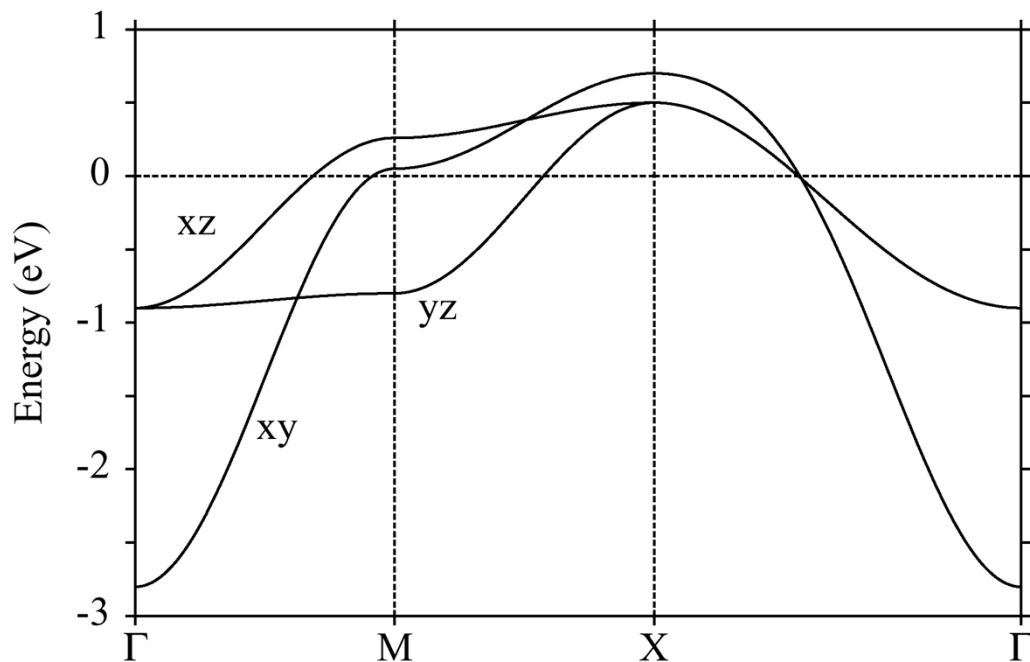
**Strong  
SOC**

- k-dependent spin-triplet mixing: **order parameter?**
- Orbital character mixing: **multiband superconductivity?**
- Is **TRSB** a signature of **spin-orbit** coupling?

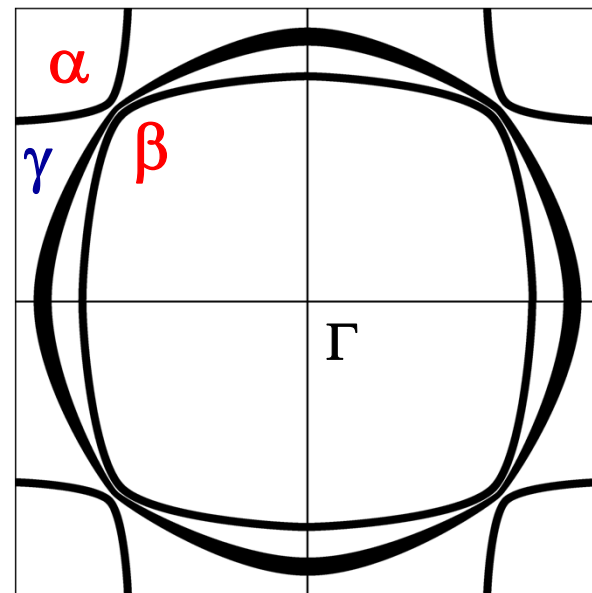
# Band Renormalization by Electronic Correlations



► Band structure calculation: **3 t<sub>2g</sub>** bands crossing **E<sub>F</sub>**

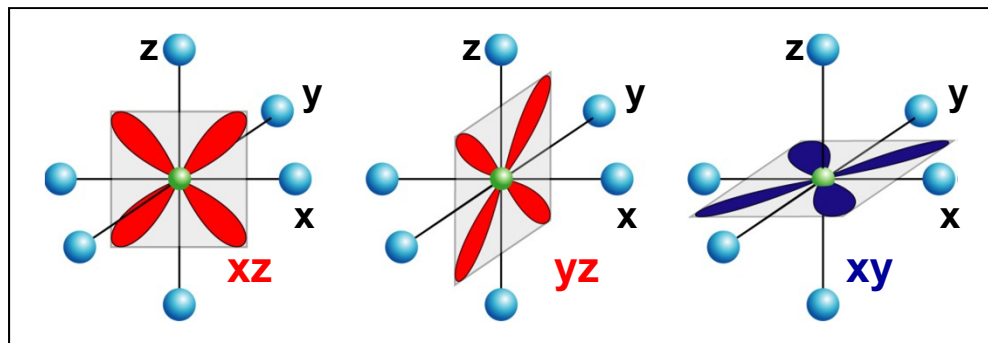
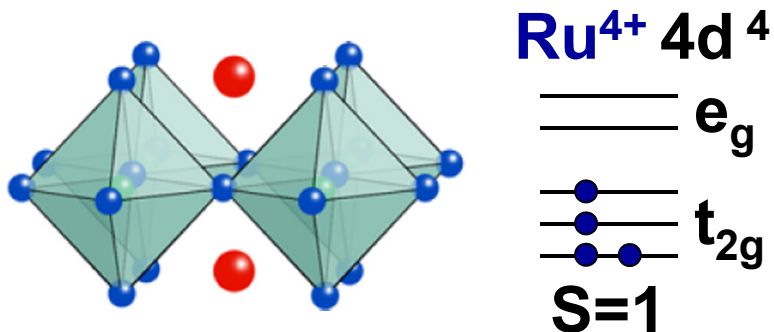


A. Liebsch *et al.*, PRL **84**, 1591 (2000)

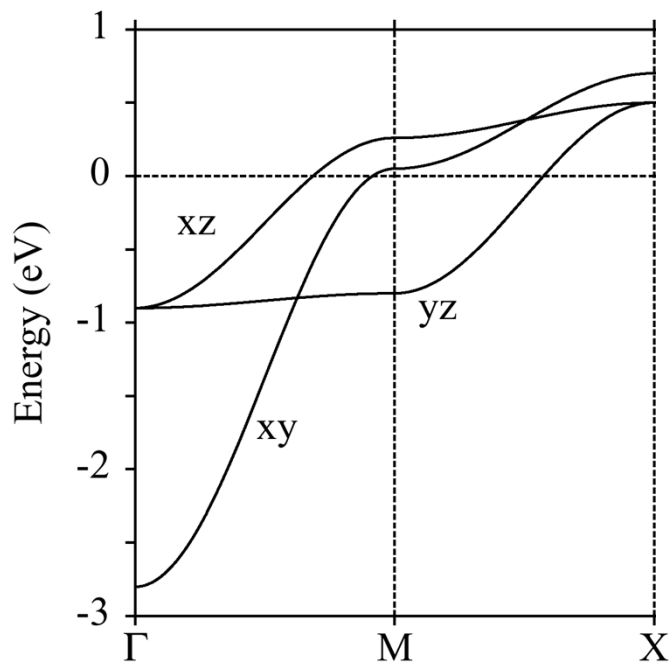


Mazin *et al.*, PRL **79**, 733 (1997)

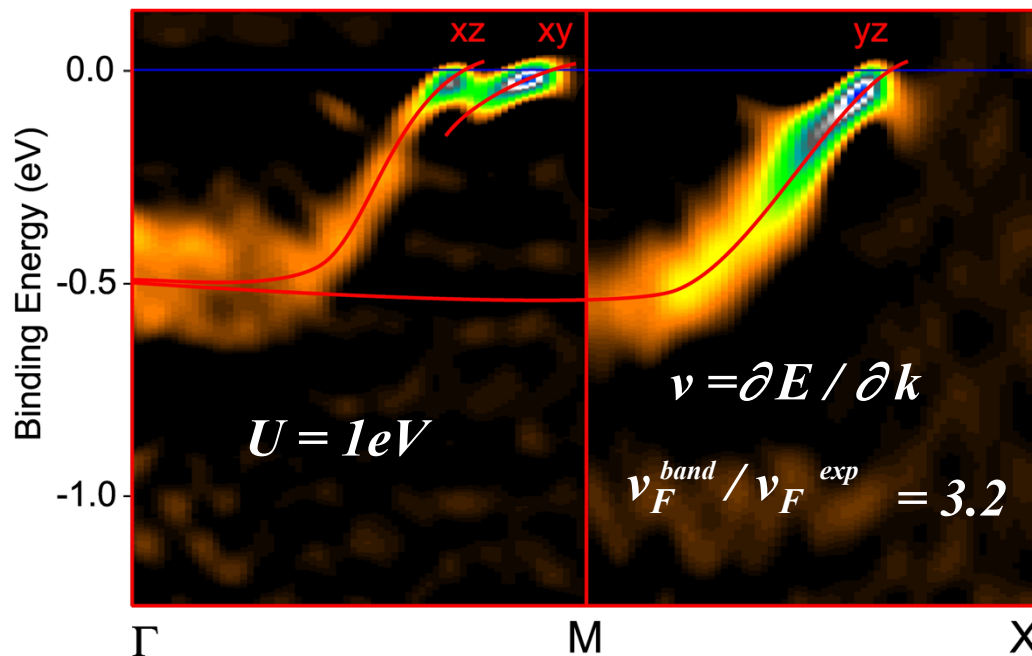
# Band Renormalization by Electronic Correlations



► The first indication of correlations is band narrowing



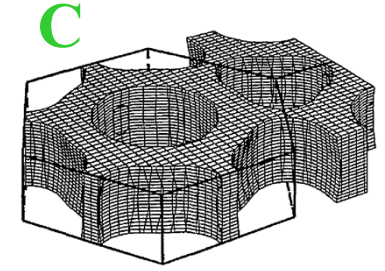
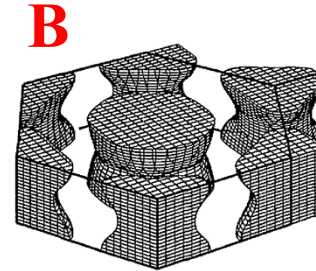
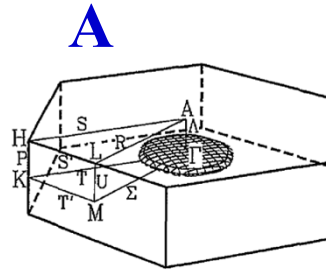
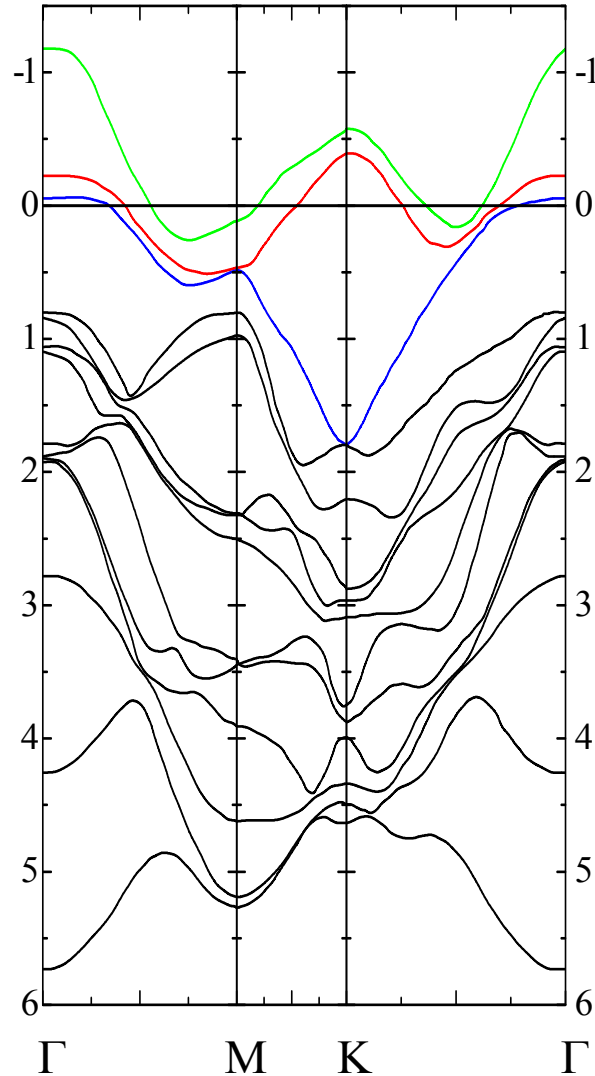
A. Liebsch *et al.*, PRL **84**, 1591 (2000)



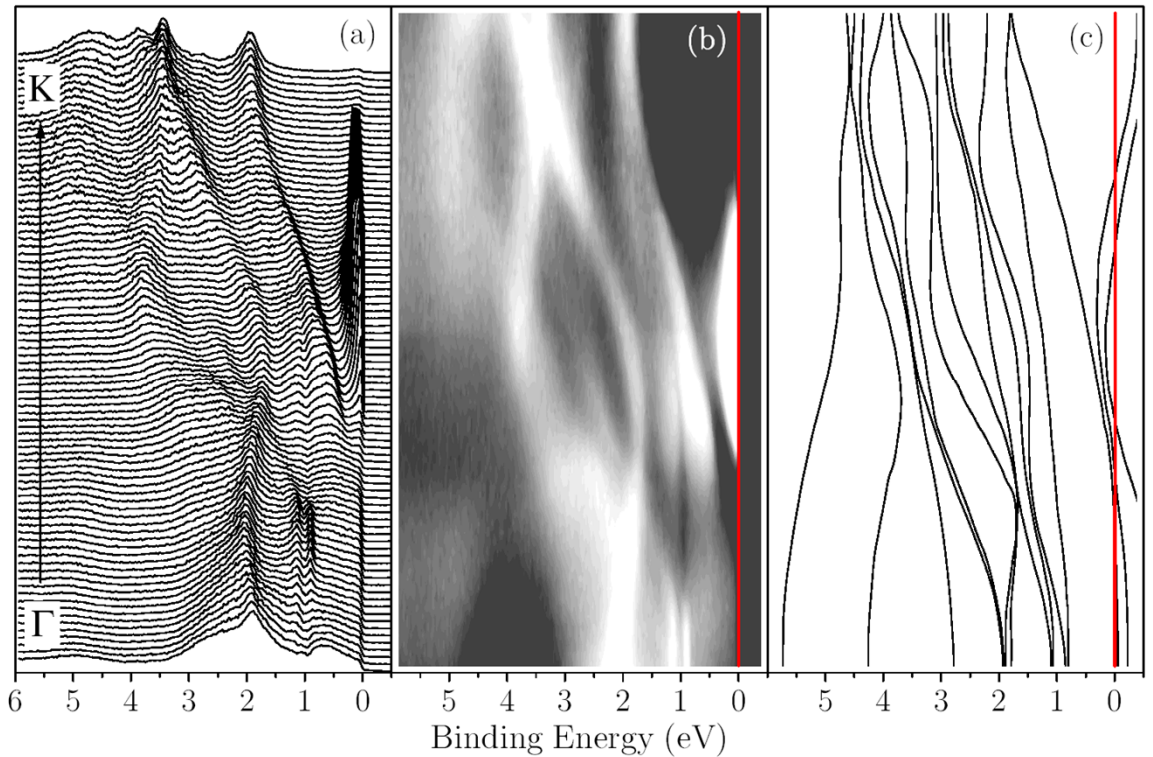
Damascelli *et al.*, PRL **101**, 026406 (2008)

# 2H-NbSe<sub>2</sub>: Normal State Electronic Structure

Corcoran *et al.*, JPCM **6**, 4479 (1994)



Damascelli *et al.* (2000)

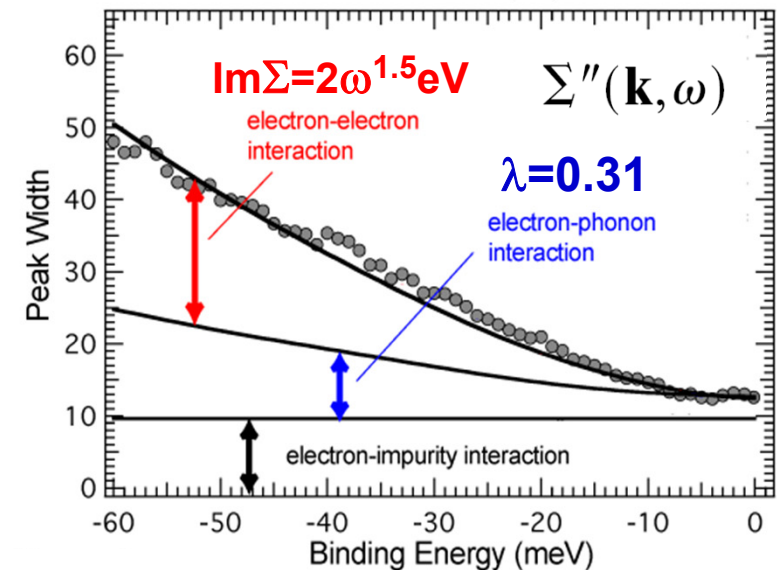
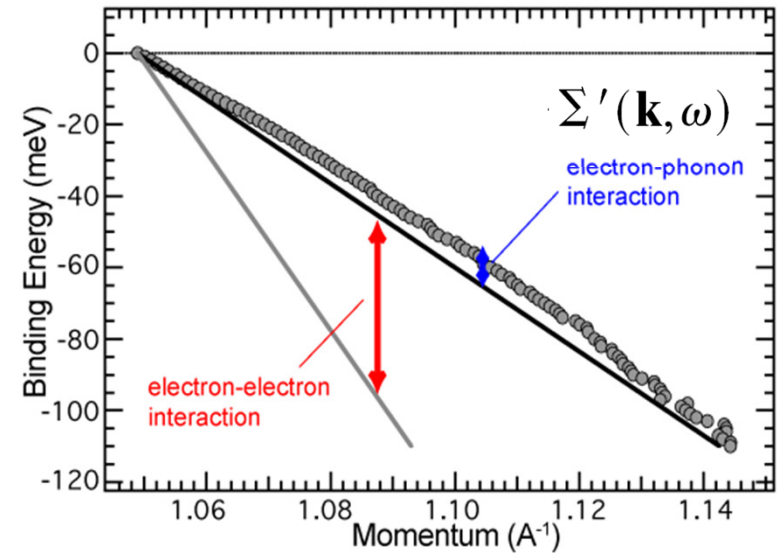
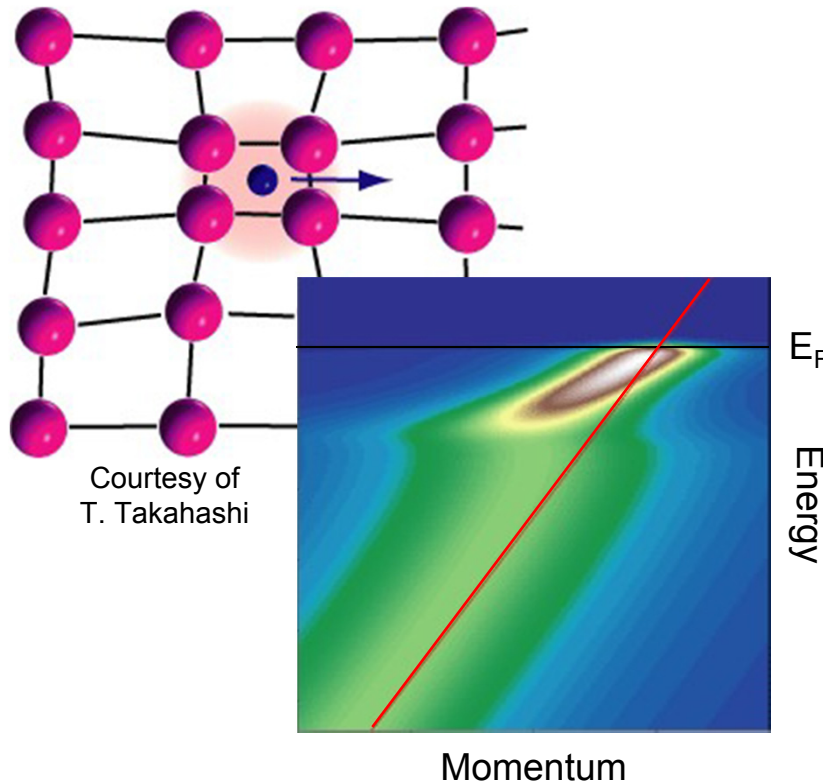


Here electronic correlations are weak: 1 to 1 matching with DFT

# Many-Body Correlation Effects in $\text{Sr}_2\text{RuO}_4$

## Single-particle spectral function

$$A(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\mathbf{k}, \omega)}{[\omega - \epsilon_{\mathbf{k}} - \Sigma'(\mathbf{k}, \omega)]^2 + [\Sigma''(\mathbf{k}, \omega)]^2}$$





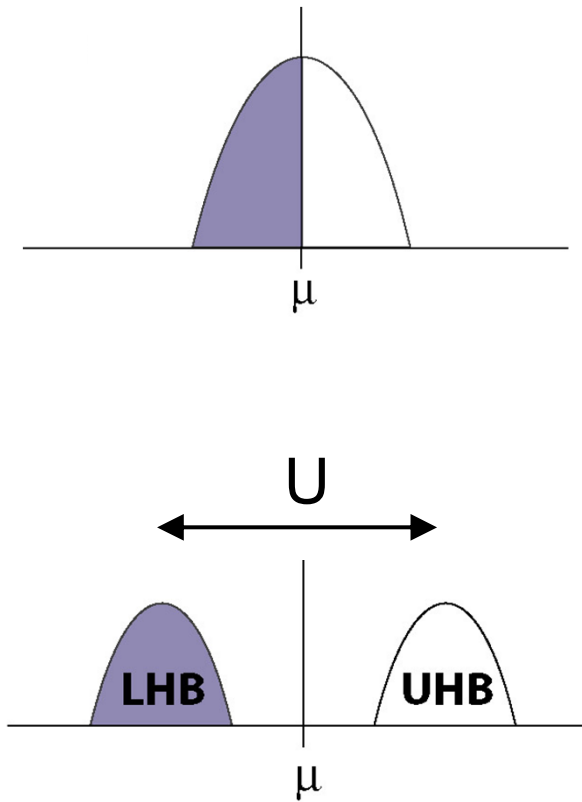


# Outline Part II

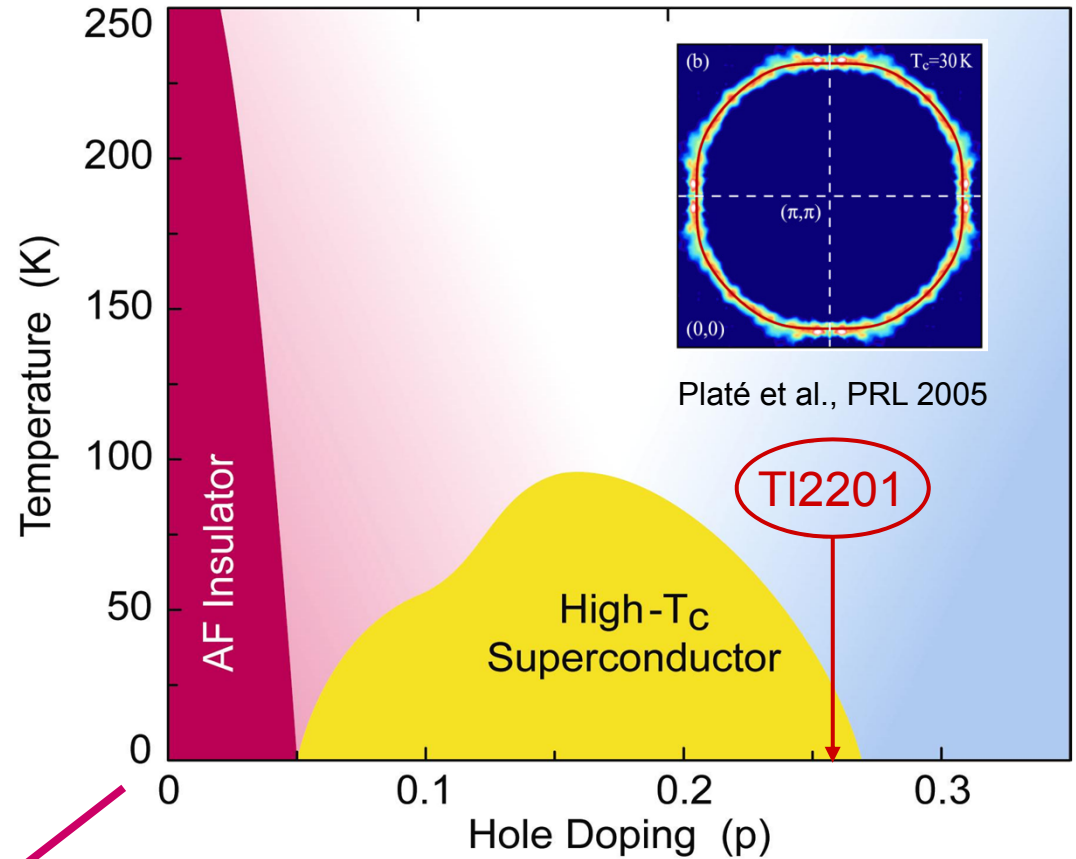
## HTSC: Mott gap and strong correlations

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# From Fermi Liquid to Mott Insulator



Mott insulator

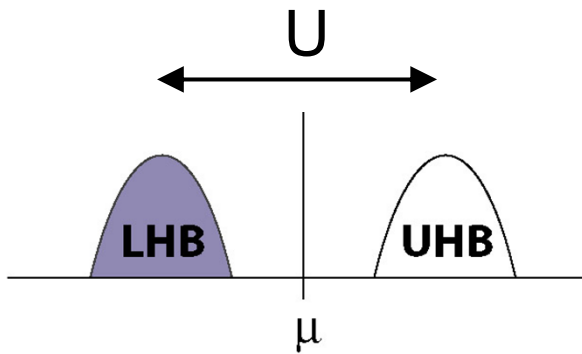
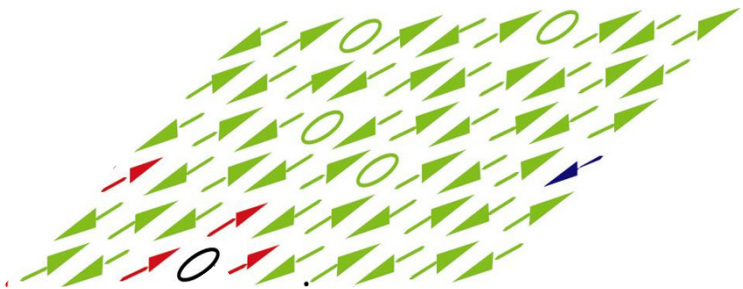


Normal state properties



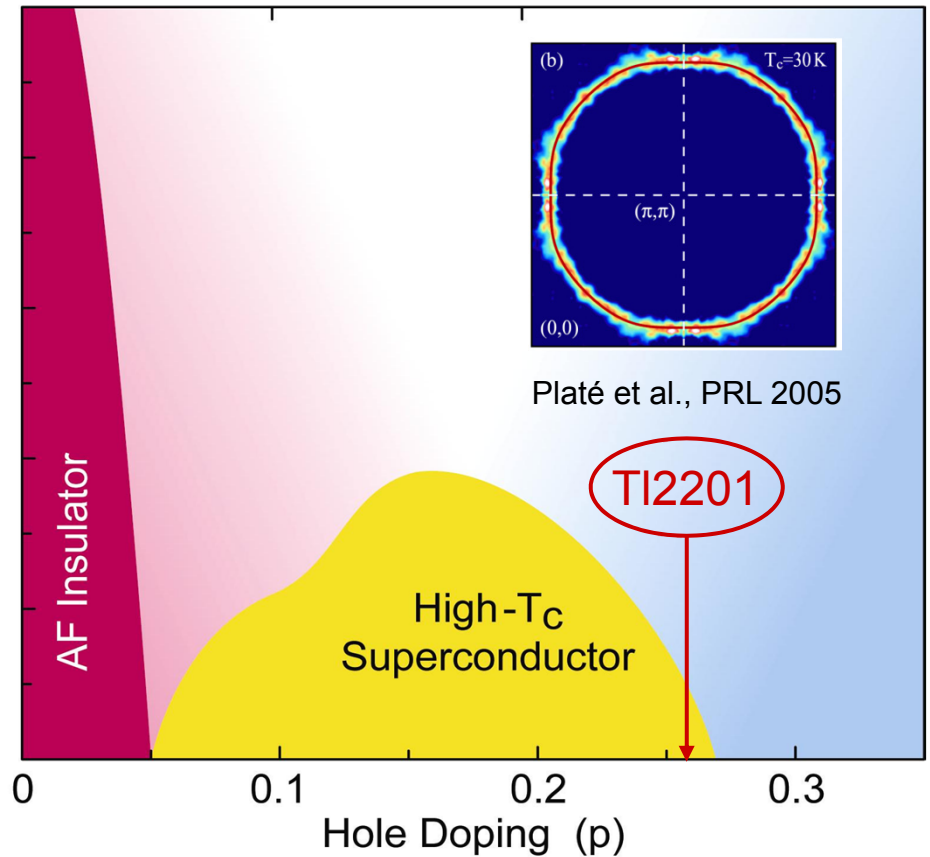
# From Fermi Liquid to Mott Insulator

Correlations suppress  $Z_k$



$$Z \simeq 2p / (p + 1)$$

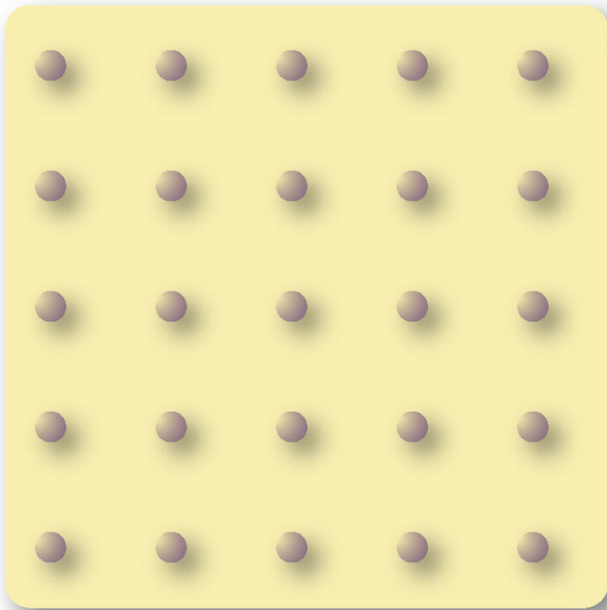
Sawatzky, Anderson, Randeria,  
Paramekanti, Yang, Rice, et al.



Normal state properties

# Mott-Hubbard Insulating Behavior

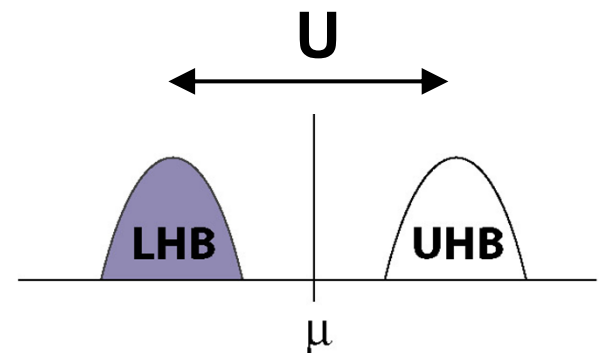
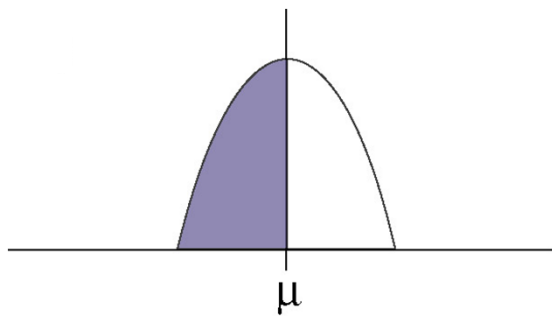
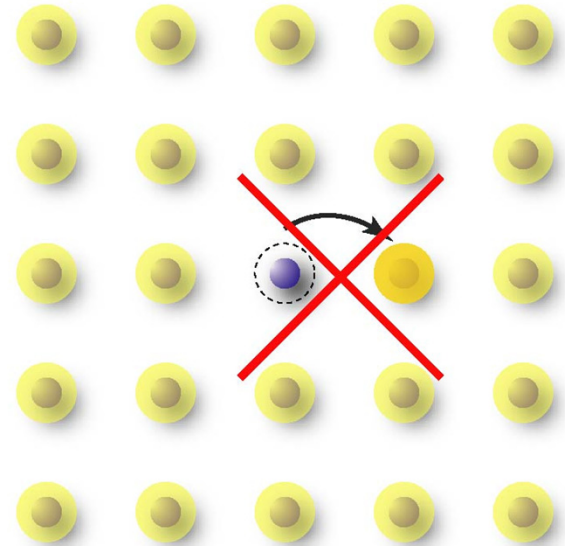
*Half-Filled Metal*



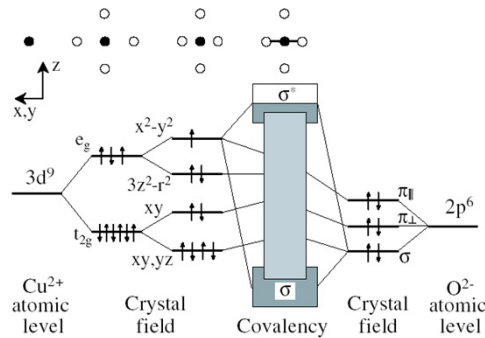
Increase inter-electron  
Coulomb repulsion  
( $U$ )



*Mott Insulator*



# High- $T_c$ Superconductors: A Minimal Model



Density functional theory  
5d Cu orbitals and 3 O orbitals  
8-band model

1987 Anderson: the essential physics of the cuprates is captured by the 1-band Hubbard model

$$H = -t \sum_{\langle ij \rangle, \sigma} (c_{i\sigma}^\dagger c_{j\sigma} + \text{H.c.}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

3-band model

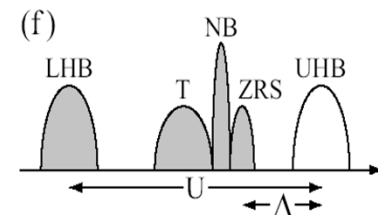
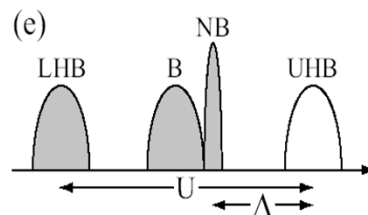
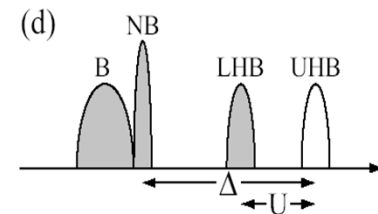
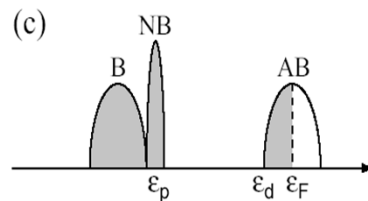
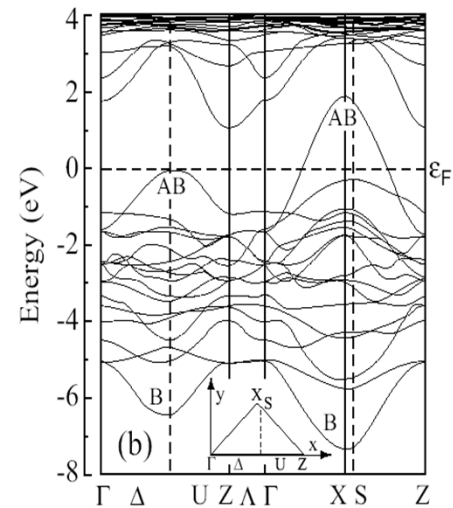
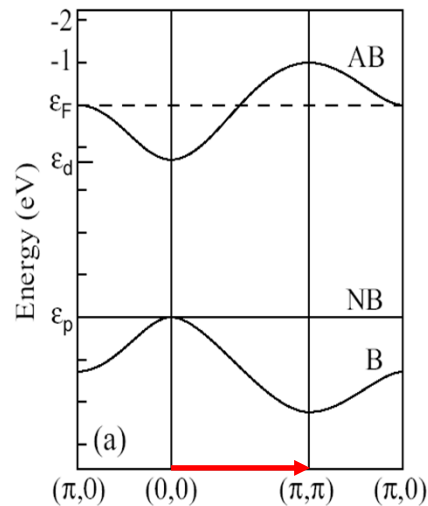
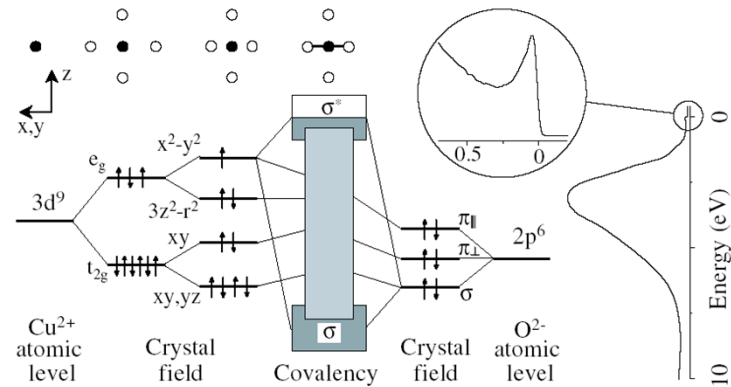
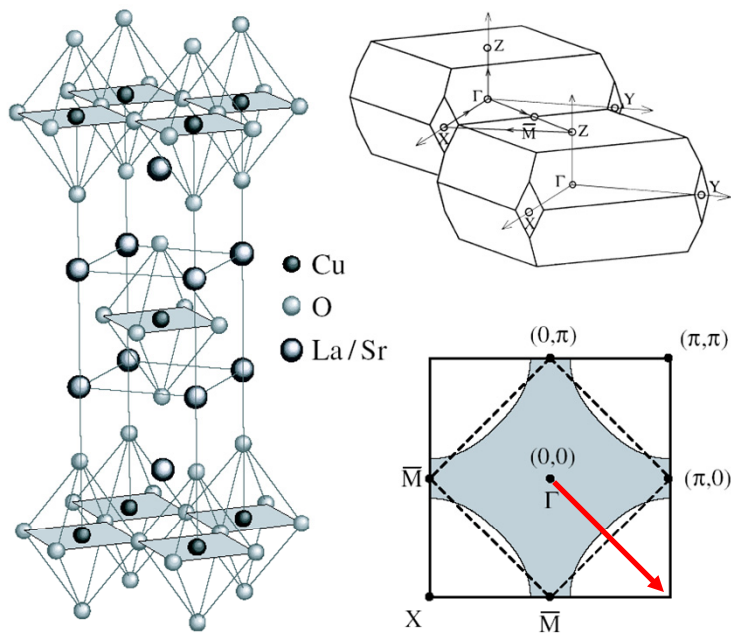
Cu  $3d_{x^2-y^2}$  O  $2p_x$  and  $2p_y$

1987 Emery: since the HTSCs are charge transfer insulators, both O and Cu have to be accounted for

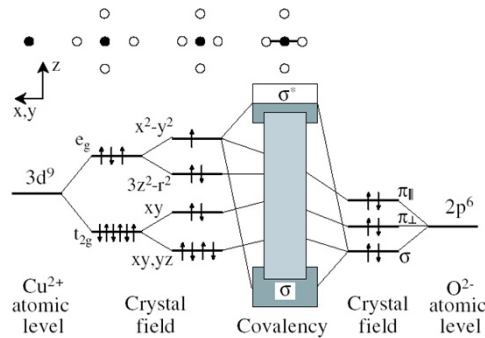
1988 Zhang & Rice: projecting out double occupancy, Cu-O hybridization leads to an effective 1-band model

$$H = -t \sum_{\langle ij \rangle, \sigma} (\tilde{c}_{i\sigma}^\dagger \tilde{c}_{j\sigma} + \text{H.c.}) + J \sum_{\langle ij \rangle} \left( \mathbf{S}_i \cdot \mathbf{S}_j - \frac{n_i n_j}{4} \right)$$

# HTSCs: Charge Transfer Insulators



# High- $T_c$ Superconductors: A Minimal Model



Density functional theory  
5d Cu orbitals and 3 O orbitals  
8-band model

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3-band model

Cu  $3d_{x^2-y^2}$  O  $2p_x$  and  $2p_y$

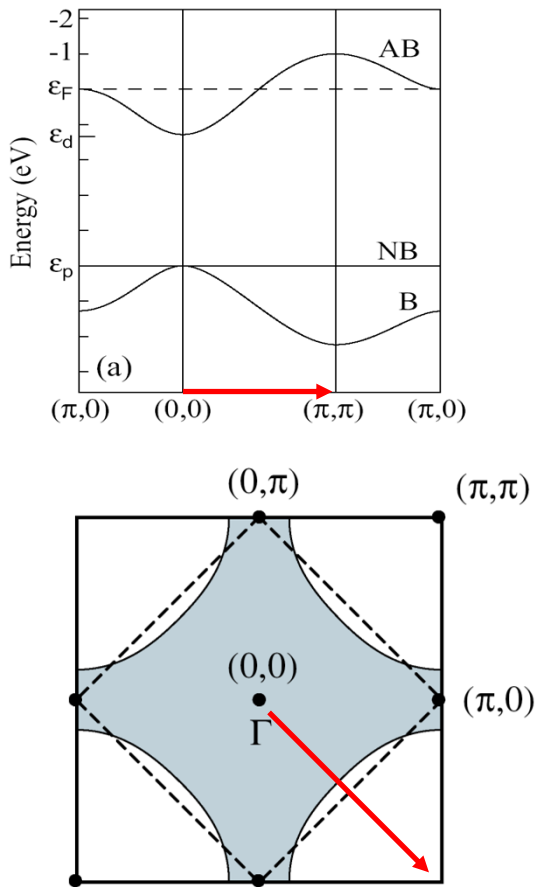
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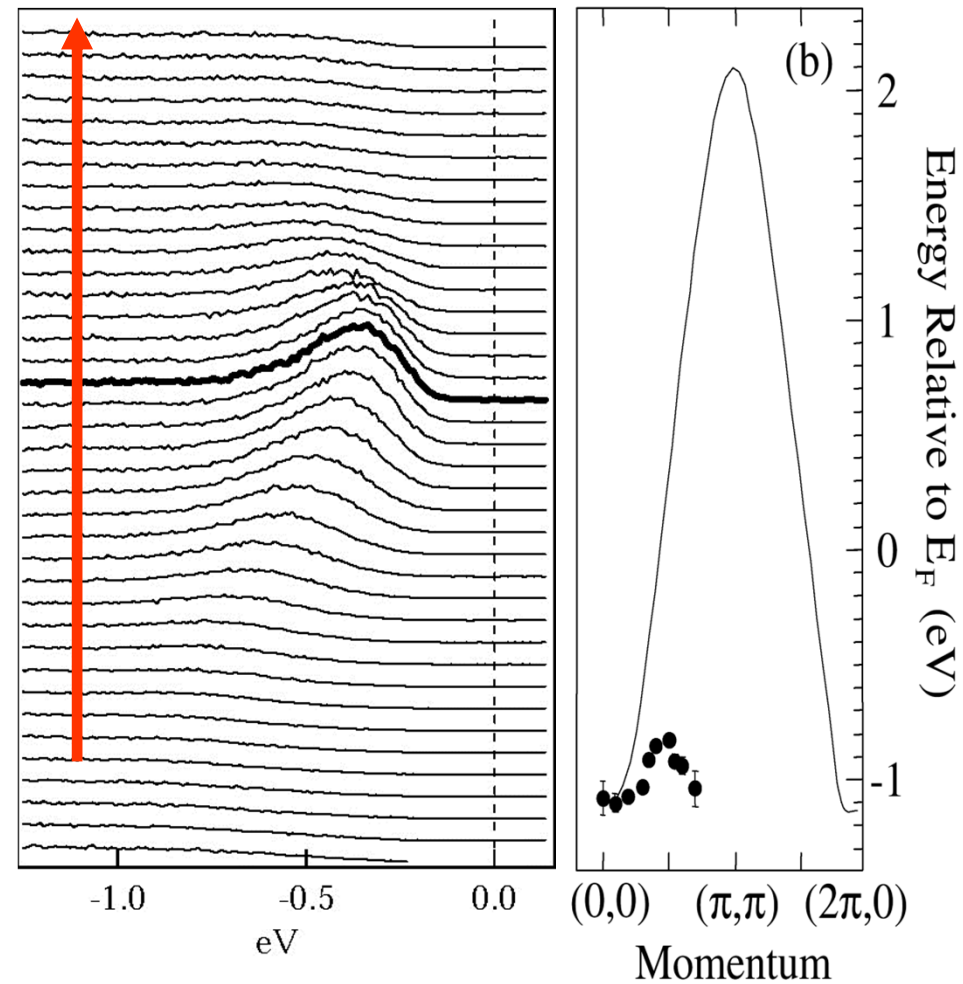
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# HTSCs: Charge Transfer Insulators

$\frac{1}{2}$  Filled Metal



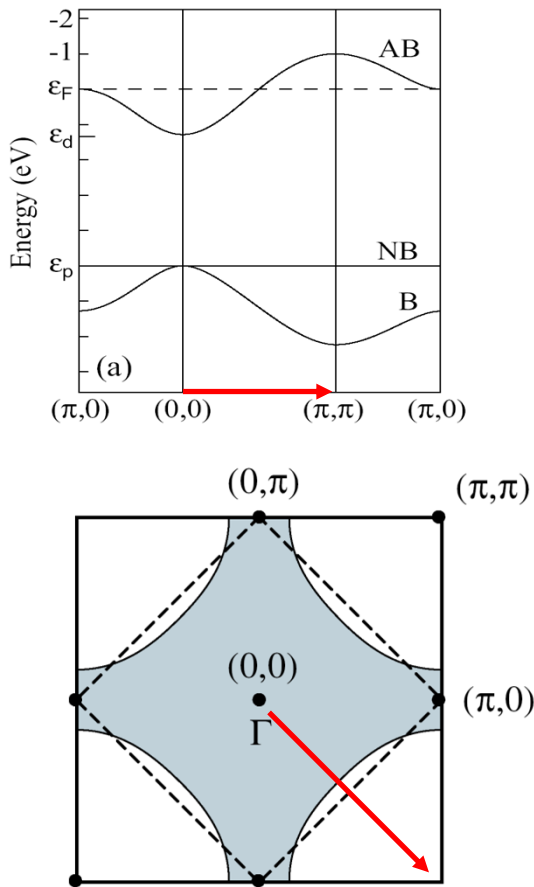
ARPES Spectra of Insulating  $\text{Ca}_2\text{CuO}_2\text{Cl}_2$  along  $(0,0) - (\pi,\pi)$



The dispersion instead of being the 2D tight-binding  $8t$  ( $t \sim 350 \text{ meV}$ ) is  $2.2J$  ( $J \sim 125 \text{ meV}$ )

# HTSCs: Charge Transfer Insulators

1/2 Filled Metal



ARPES Spectra of Insulating  $\text{Sr}_2\text{CuO}_2\text{Cl}_2$

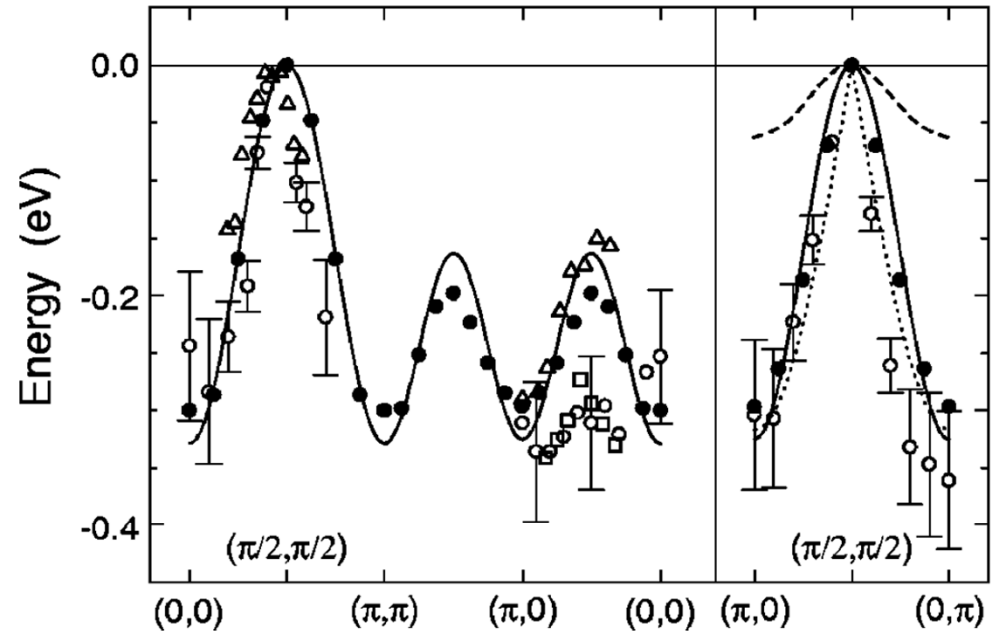


FIG. 17. Electronic dispersion for SCOC ( $E=0$  corresponds to the top of the band). Experimental data:  $\circ$ , Wells *et al.*, 1995;  $\triangle$ , La Rosa *et al.*, 1997;  $\square$ , Kim *et al.*, 1998. Dashed line,  $t$ - $J$  model calculations (Wells *et al.*, 1995);  $\bullet$ , self-consistent Born approximation for the  $t$ - $t'$ - $t''$ - $J$  model ( $t=0.35$  eV,  $t'=-0.12$  eV,  $t''=0.08$  eV, and  $J=0.14$  eV); solid lines, fits of the self-consistent Born approximation data (Tohyama and Maekawa, 2000); dotted line along  $(\pi,0)$ - $(0,\pi)$ , spinon dispersion (Laughlin, 1997).

The dispersion instead of being the 2D tight-binding  $8t$  ( $t \sim 350$  meV) is  $2.2J$  ( $J \sim 125$  meV)



# HTSCs: Charge Transfer Insulators

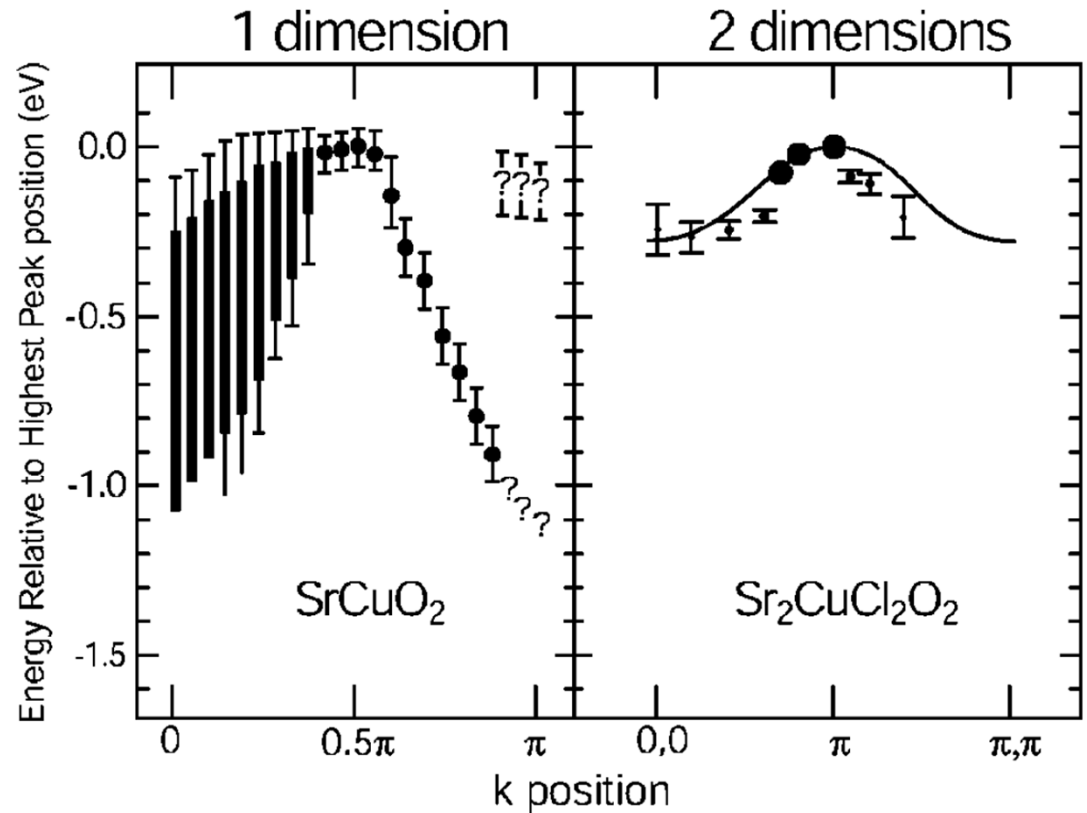
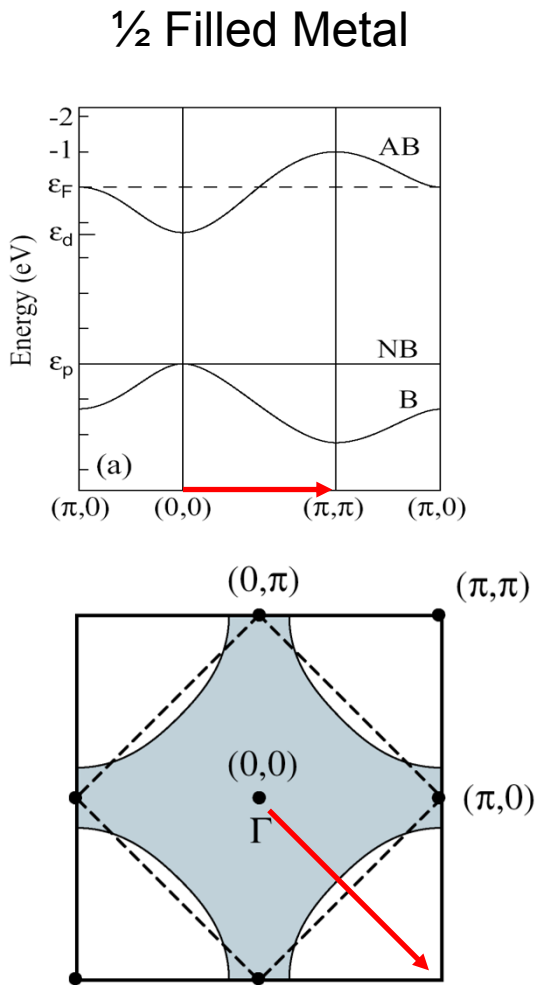
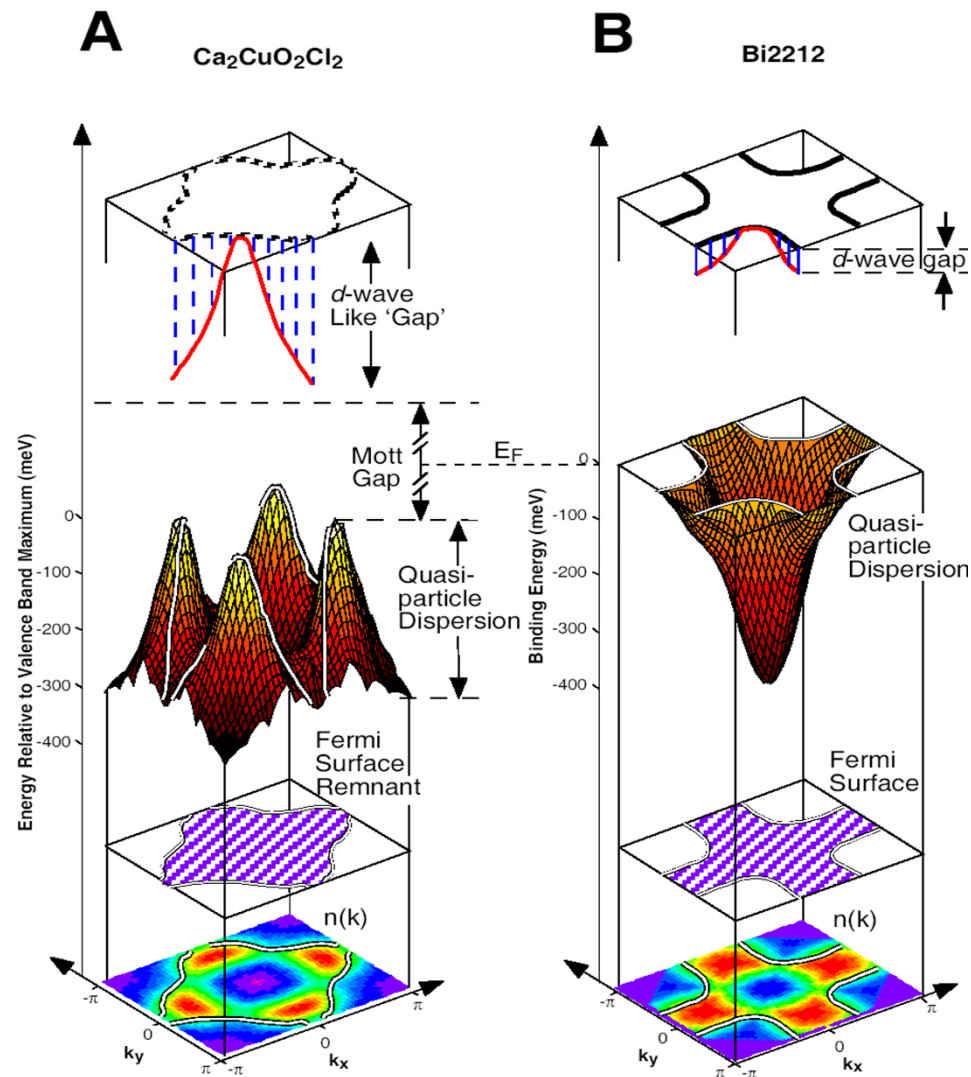
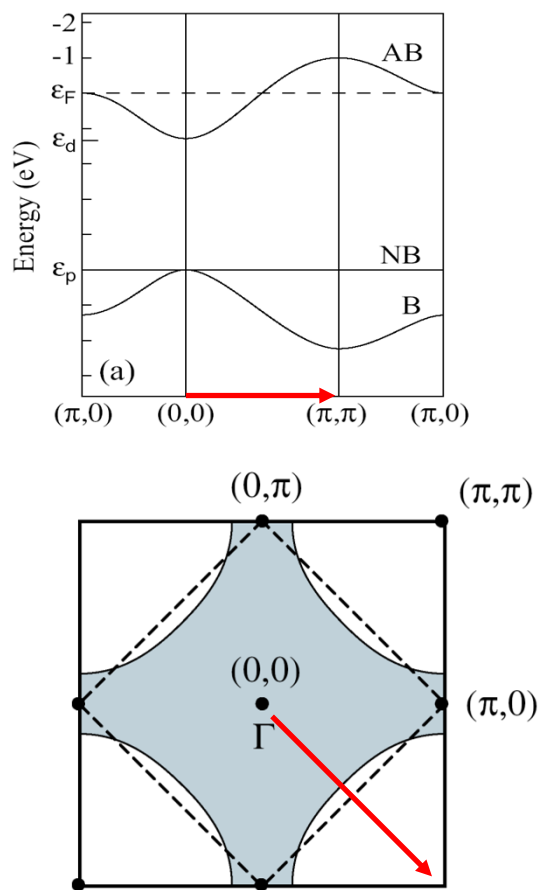


FIG. 18. Experimental dispersion for quasi-1D (Kim *et al.*, 1996) and quasi-2D (Wells *et al.*, 1995) insulating systems.

The dispersion instead of being the 2D tight-binding  $8t$  ( $t \sim 350 \text{ meV}$ ) is  $2.2J$  ( $J \sim 125 \text{ meV}$ )

# High- $T_c$ Superconductors: Electronic Structure

## $\frac{1}{2}$ Filled Metal



# How Can One Measure the Mott Gap?

## Definition of Conductivity Gap

$$\begin{aligned} E_{\text{gap}} &= (E_{\text{gr}}^{N-1} - E_{\text{gr}}^N) + (E_{\text{gr}}^{N+1} - E_{\text{gr}}^N) \\ &= E_{\text{gr}}^{N-1} + E_{\text{gr}}^{N+1} - 2 E_{\text{gr}}^N \end{aligned}$$

$E_{\text{gr}}$   $\longrightarrow$  Ground state

# How Can One Measure the Mott Gap?

## Optics

- photon in – photon out
- electric dipole transition
- particle-hole excitations
- collective modes  
(phonons, magnons, plasmons)
- number of particles is conserved

## Electron transition

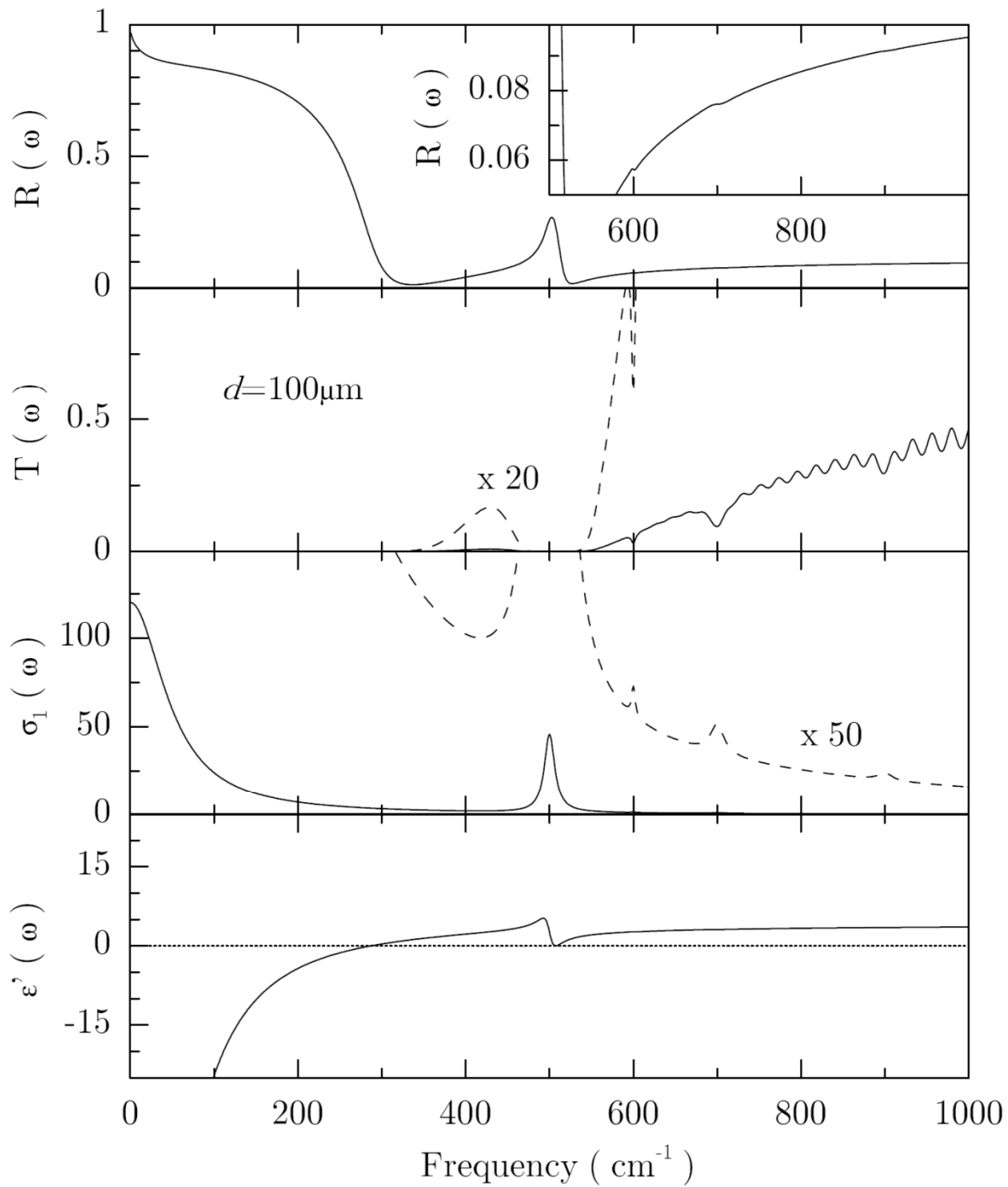
Particle-hole excitations  
of the N-particle system

## Photoemission

- photon in – electron out
- electric dipole transition
- electron removal excitations
- collective modes?  
only as dressing of quasiparticles
- number of particles not conserved

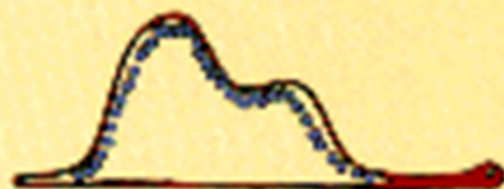
## Electron removal

Single-particle excitations  
of the (N-1)-particle system



Optics

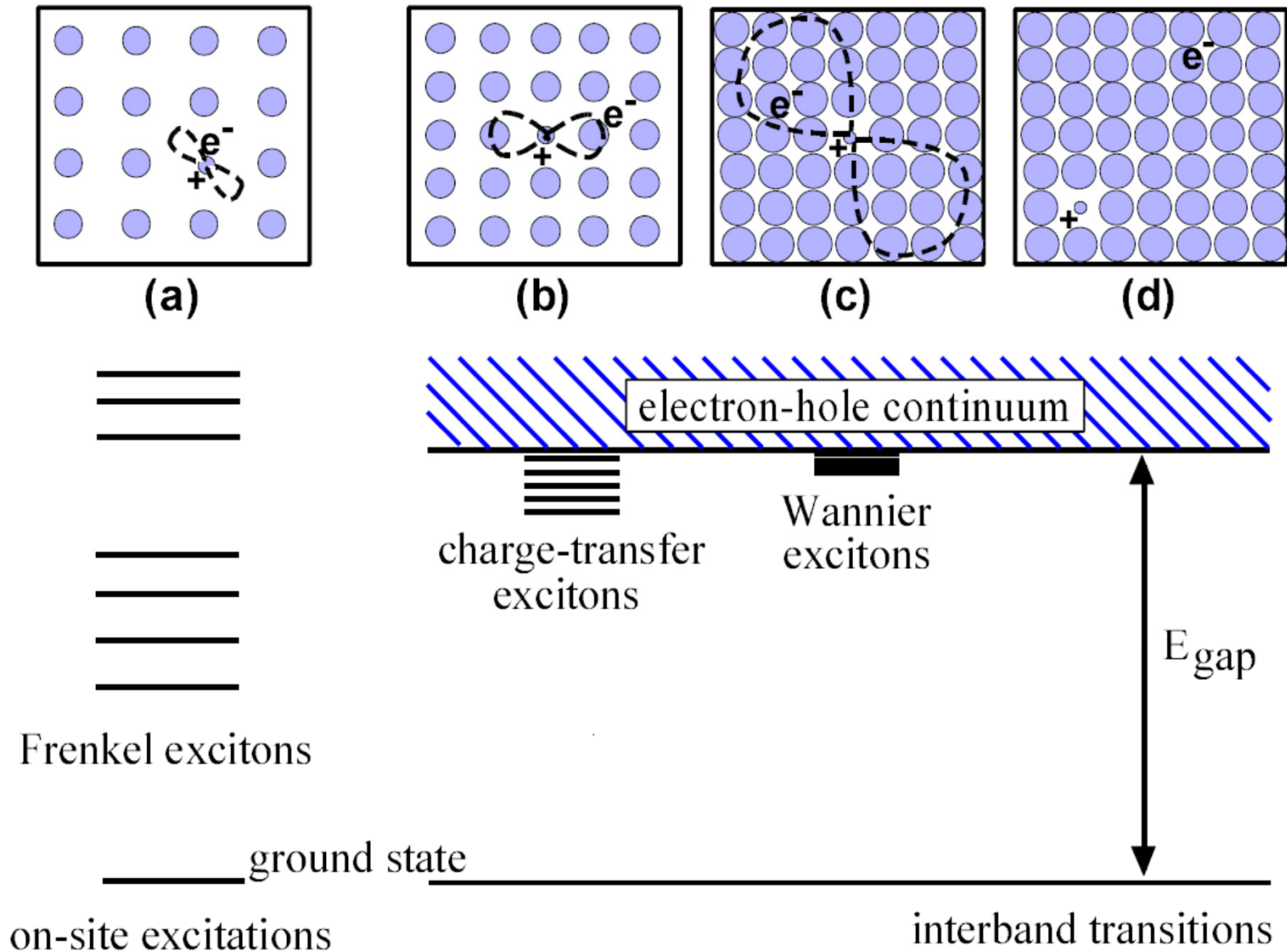
Second-Harmonic Generation,  
a Selective Probe for Excitons



Anna-Maria Janner



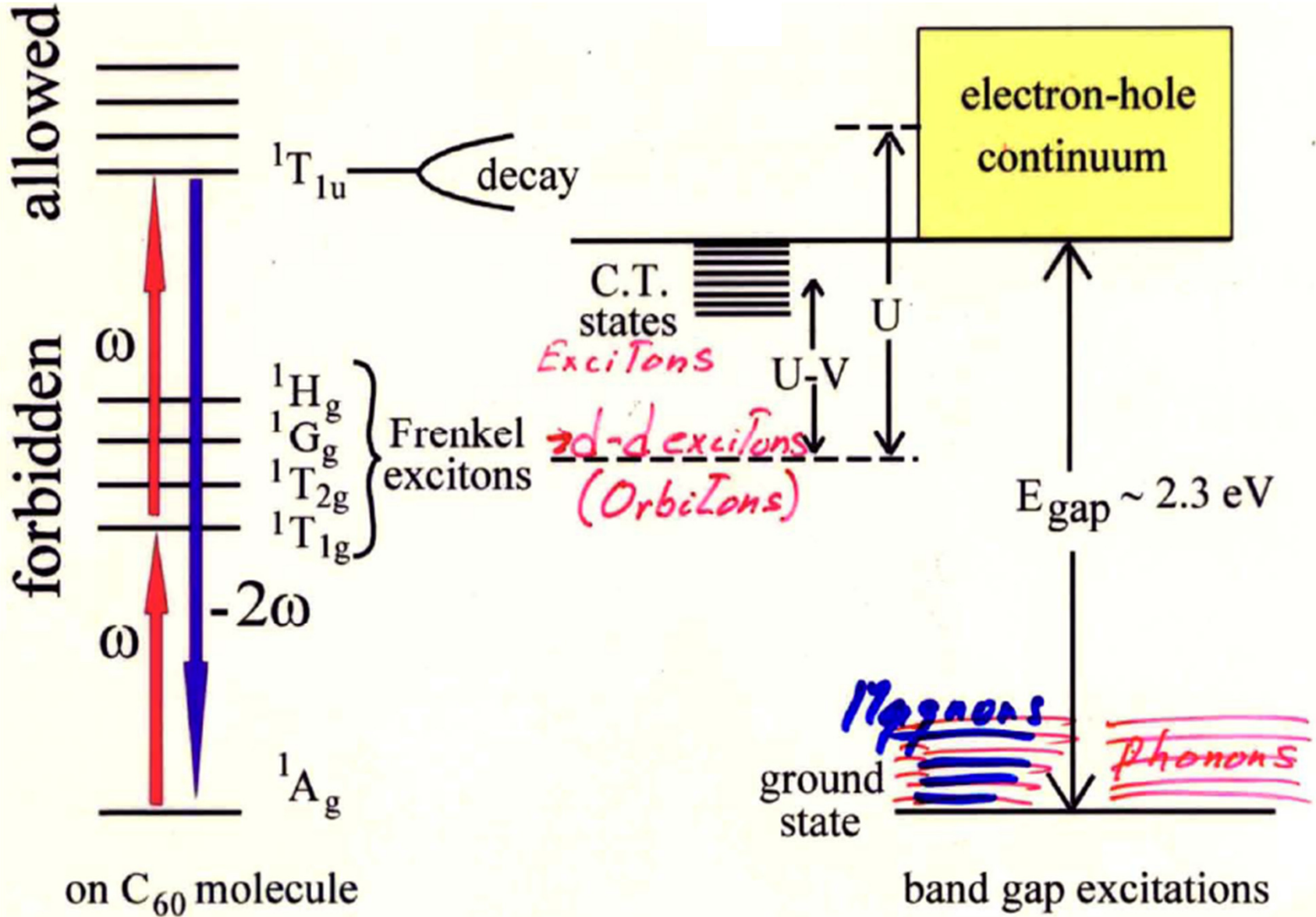
# General Elementary Excitations?



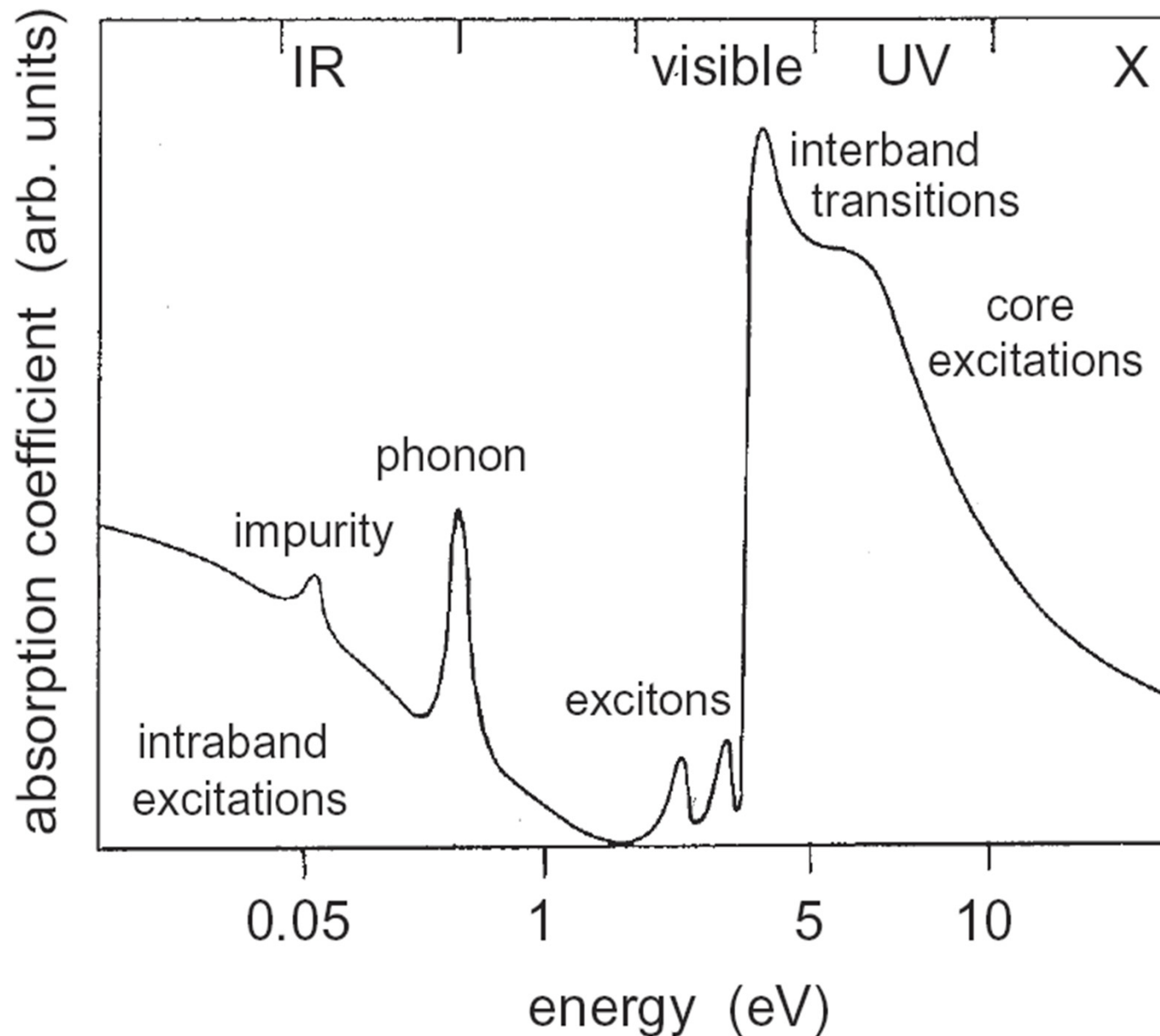
Courtesy of George Sawatzky



# General Elementary Excitations?



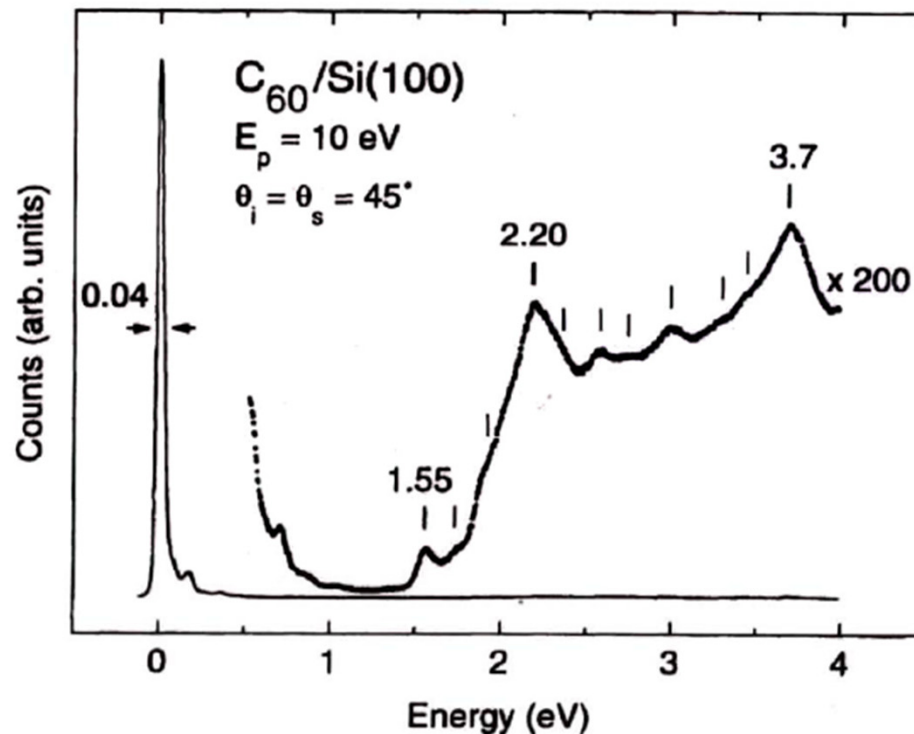
# Absorption Coefficient in a Semiconductor

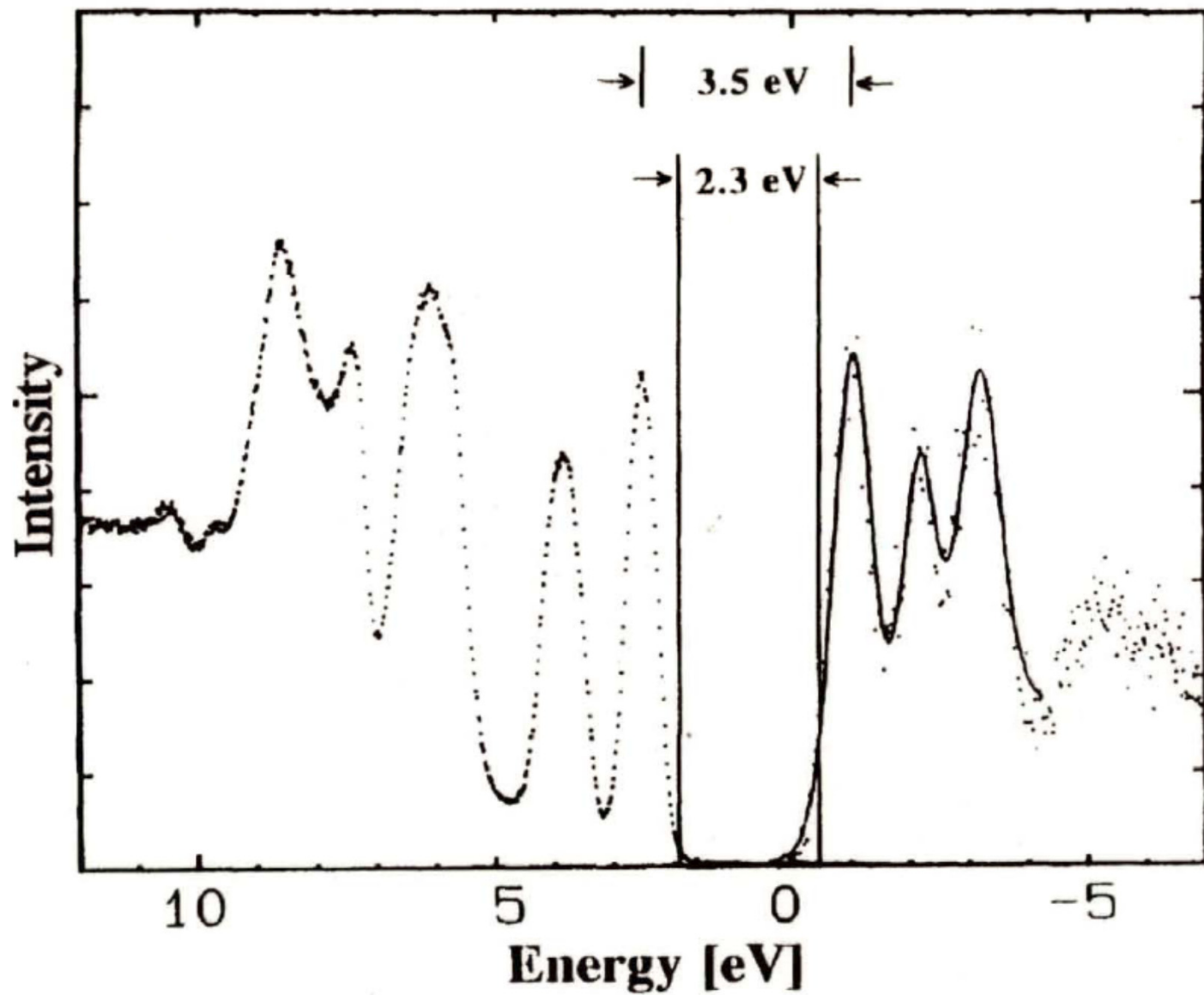


# Excitons versus Band Gap

The 1.55 eV excitations which agrees with the DFT band gap was thought to be the conductivity gap

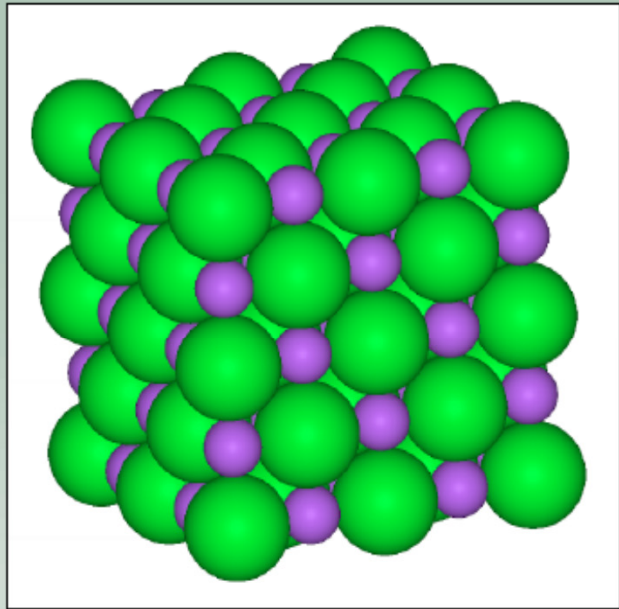
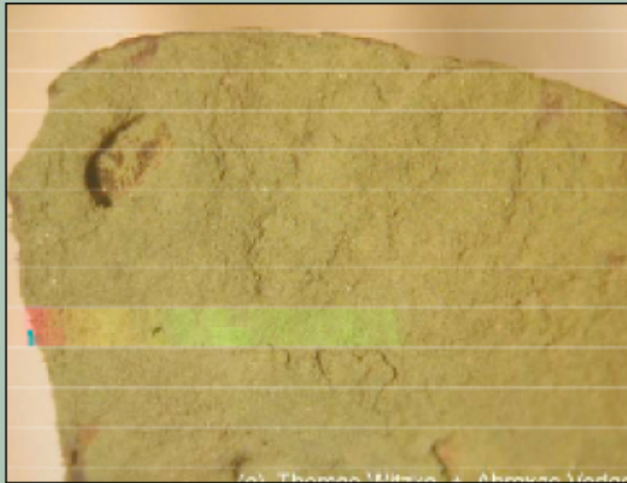
## Electron Energy Loss Spectroscopy





# NiO - Bunsenite

Courtesy of  
Jan Kuneš



- rock-salt structure ( $T_m = 2261$  K)  
bulk modulus: 209 GPa  
(CoO 194, MnO 148, diamond 462, Li 11)
- type II AFM ( $T_N = 532$  K)
- charge gap: 3.7 eV
- Formal valency: Ni<sup>2+</sup>:  $d^8s^0$  O<sup>2-</sup>:  $p^6$
- $U \sim 9$  eV

## Transition-Metal Monoxides: Band or Mott Insulators

K. Terakura<sup>(a)</sup> and A. R. Williams

*IBM Thomas J. Watson Research Center, Yorktown Heights, New York 10598*

and

T. Oguchi

*Institute for Solid State Physics, The University of Tokyo, Roppongi, Minato-ku, Tokyo, Japan*

and

J. Kübler

*Fachgebiet Theoretische Physik, Institut für Festkörperphysik, D-6100 Darmstadt, West Germany*

(Received 24 February 1984)

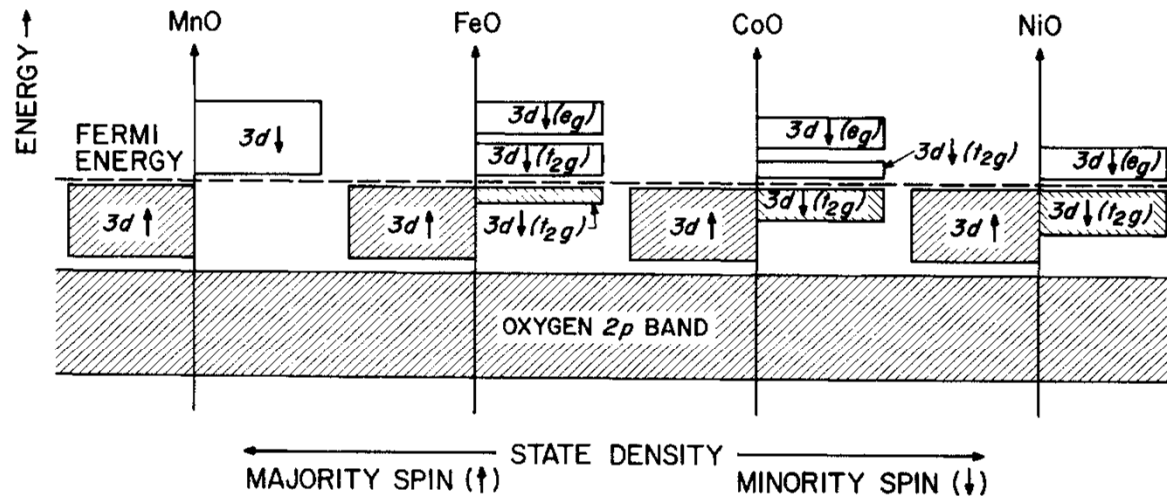


FIG. 1. Band picture of the monoxides. The qualitative difference between this picture and the commonly accepted one is the energy position of the empty  $d$  states. To quantify the state-density information, we find the width of the Mn  $3d$  and the O  $2p$  bands to be 3 eV and 5 eV, respectively. The band centers are separated by  $\sim 5$  eV. The gaps in MnO and NiO are 0.4 and 0.3 eV, respectively.



## Optical Properties of Nickel Oxide\*

R. NEWMAN† AND R. M. CHRENKO  
*General Electric Research Laboratory, Schenectady, New York*  
 (Received January 28, 1959)

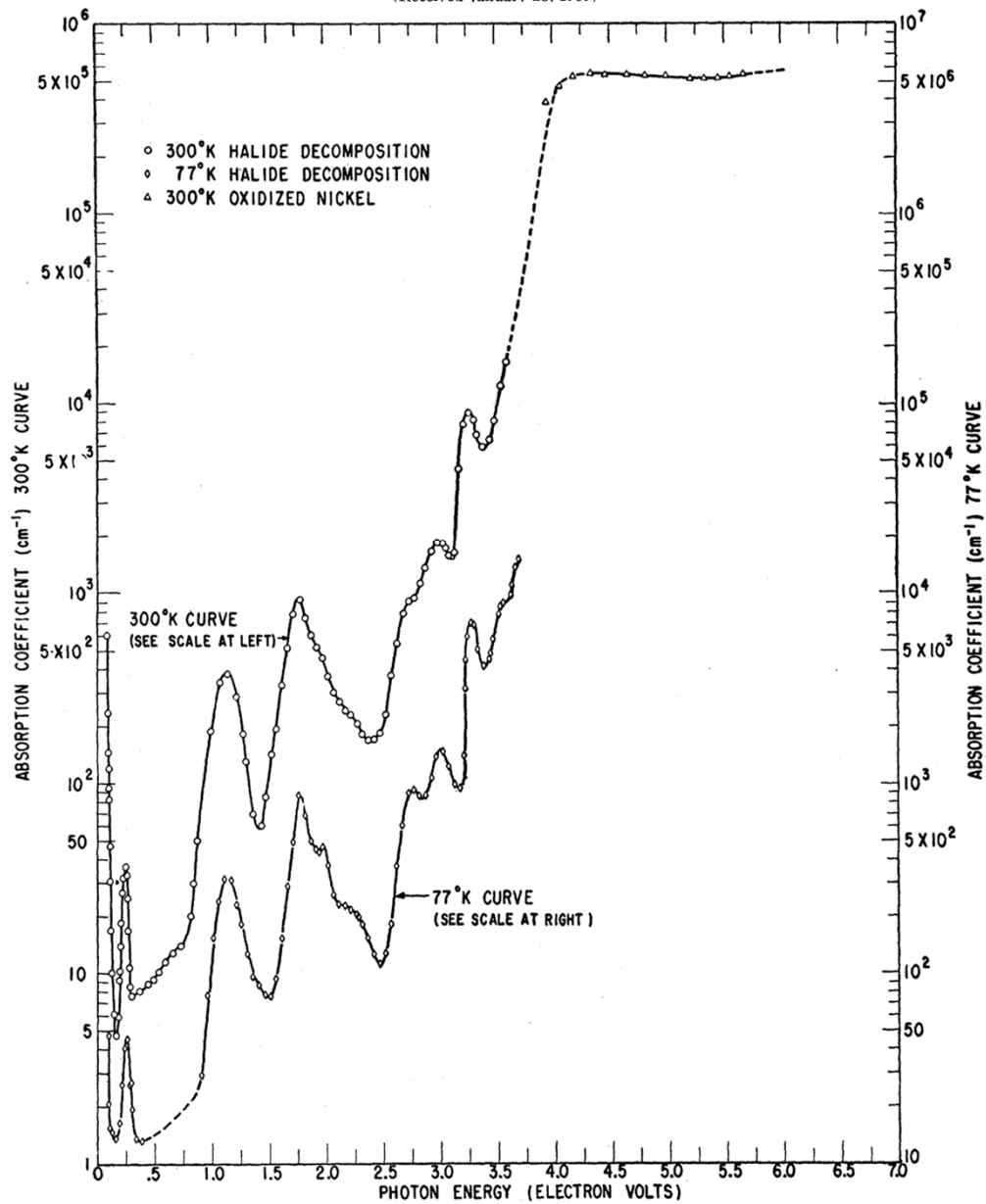


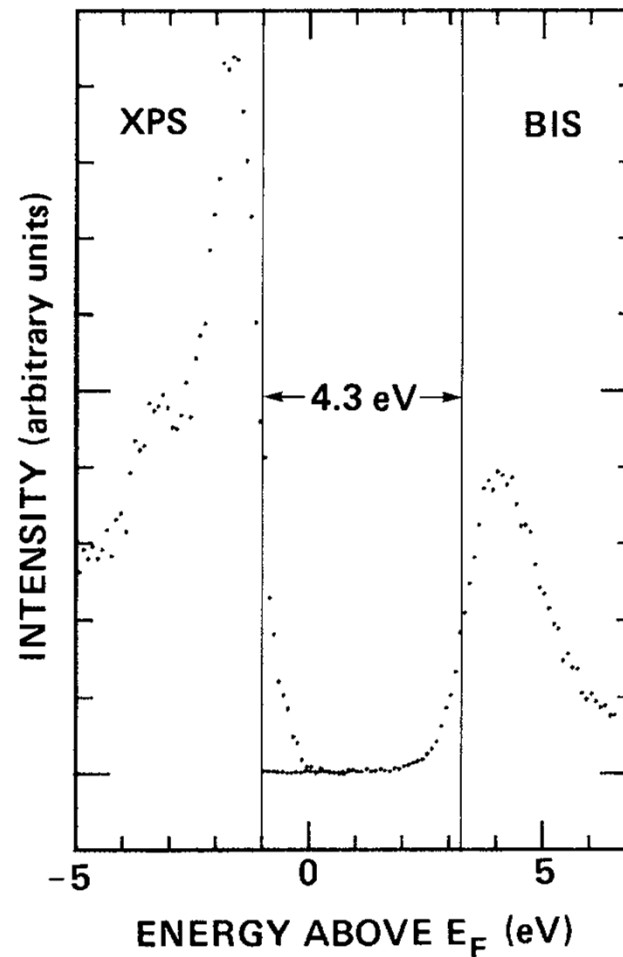
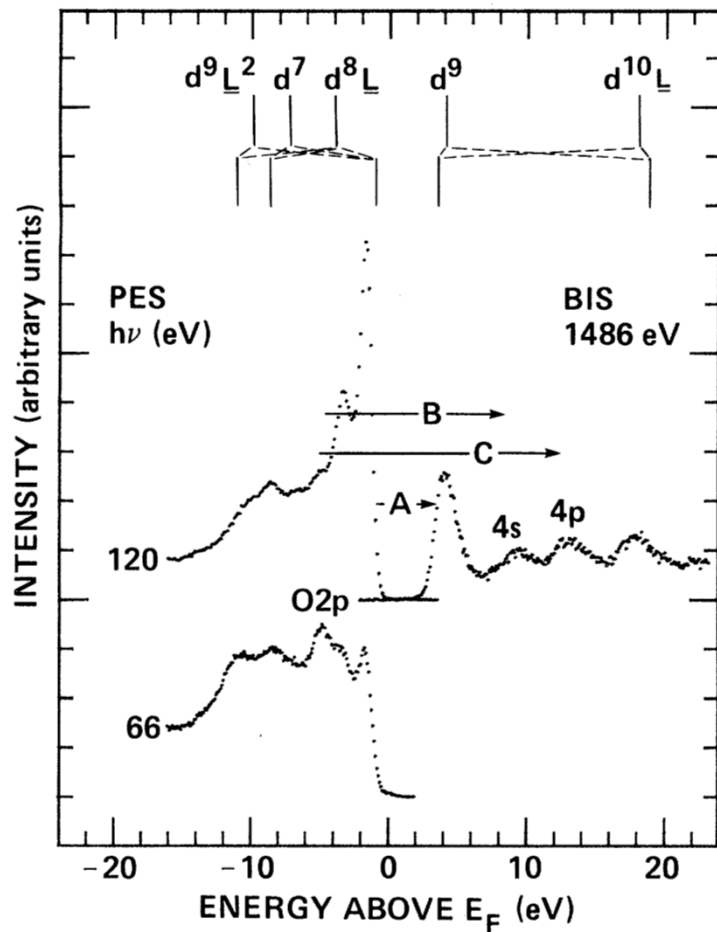
FIG. 2. Absorption spectrum of NiO at 300°K, 77°K. Dashed lines are interpolations.

# Magnitude and Origin of the Band Gap in NiO

G. A. Sawatzky<sup>(a)</sup> and J. W. Allen

*Xerox Palo Alto Research Center, Palo Alto, California 94304*

(Received 5 July 1984)

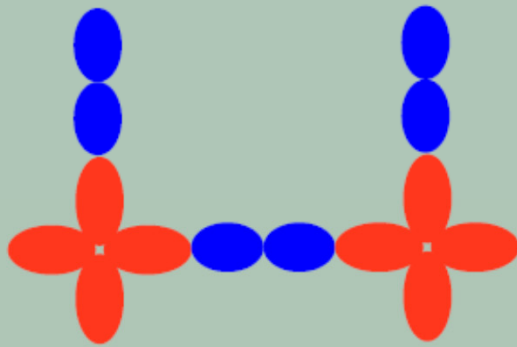


**NiO is a charge transfer insulator**

# Transition metal oxides: ZSA scheme



Courtesy of  
Jan Kuneš

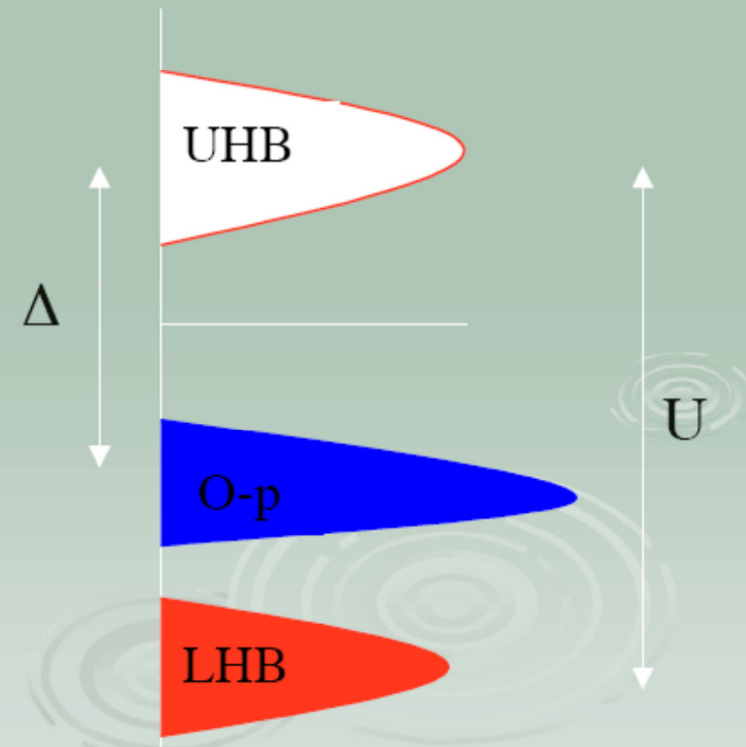
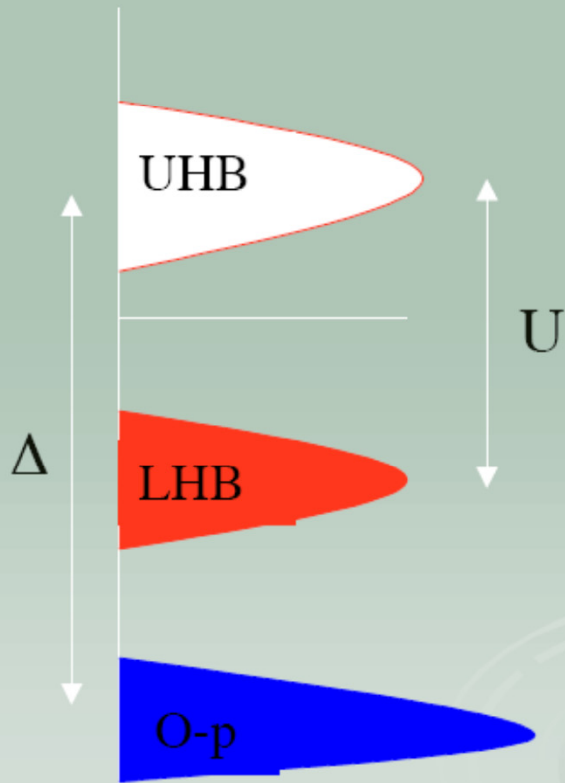


*O - 2p*

*Transition metal - 3d*

Mott-Hubbard type (Ti-O, V-O)

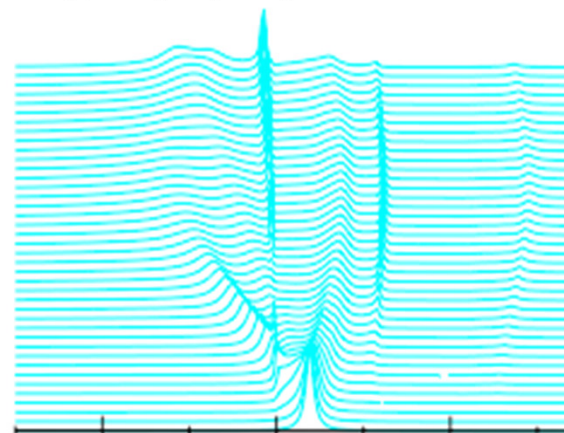
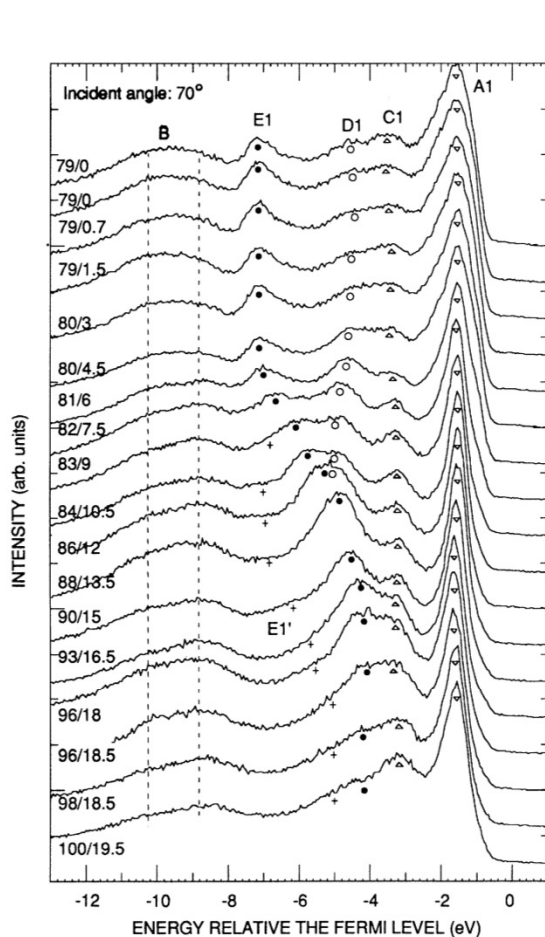
charge-transfer type (Ni-O, Cu-O)



# Electronic structure of NiO: Correlation and band effects

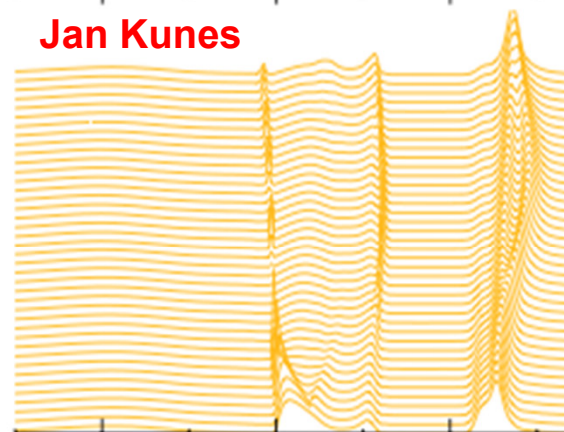
Z.-X. Shen

*Stanford Electronics Laboratory, Stanford University, Stanford, California 94305*



O - 2p

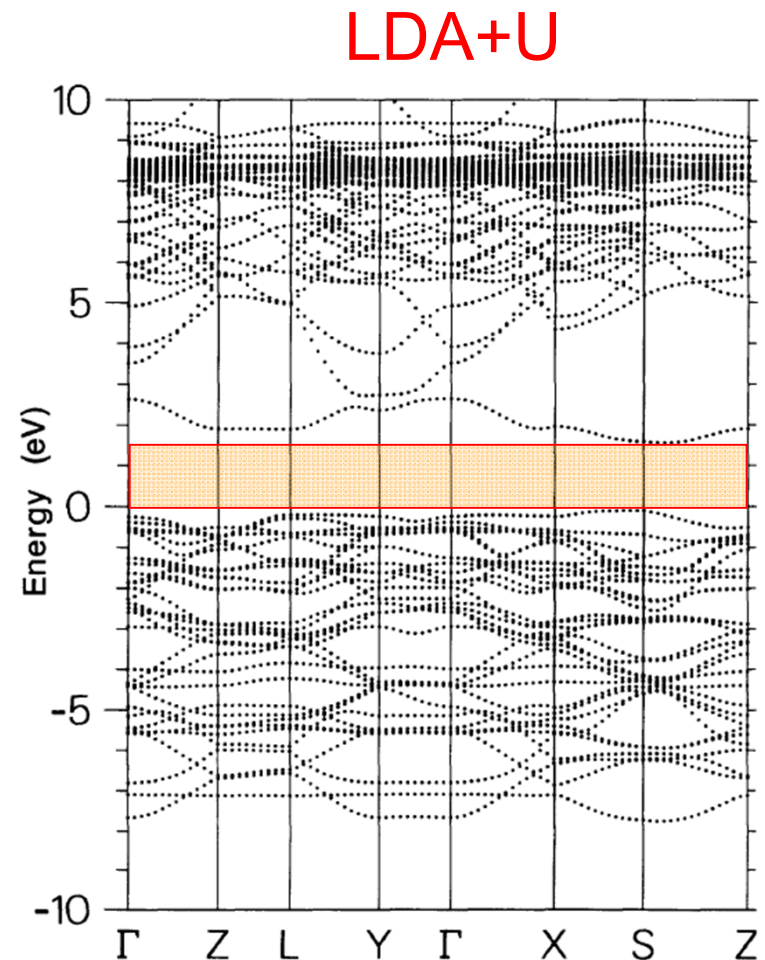
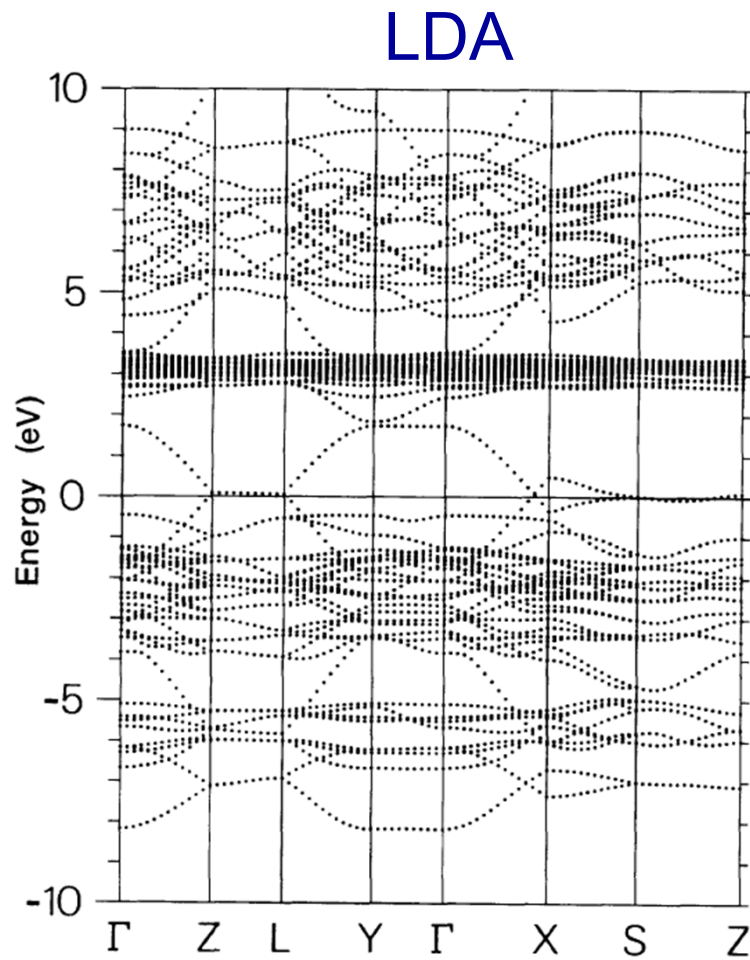
Jan Kunes



Ni - 3d(e<sub>g</sub>)

**NiO is a charge transfer insulator**

# Electronic Structure of a Mott Insulator: LDA+U



LDA+U can describe the Mott insulator with a gap, BUT:

- It works only for truly insulating systems with no open shells (1/2-filled)
- It does not include many body states such as the Zhang-Rice singlet



# Electronic Structure of a Mott Insulator: LDA+U

## Zhang-Rice Singlet

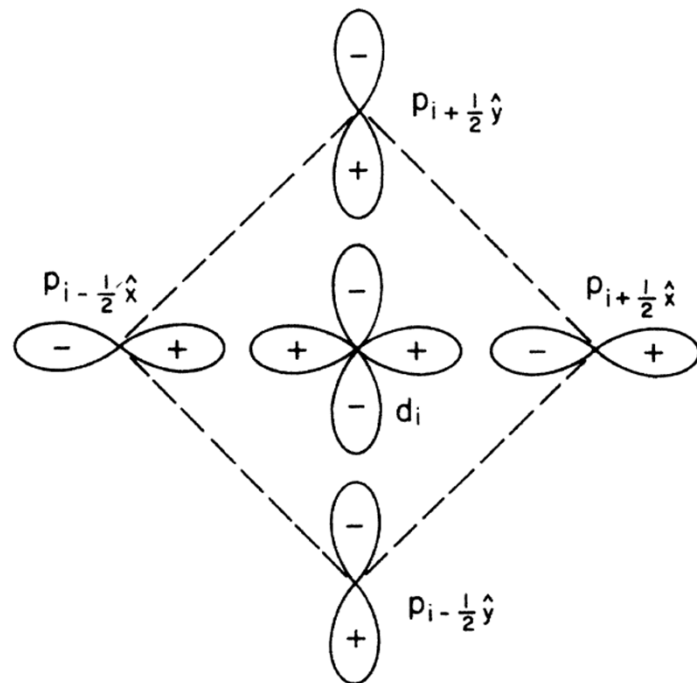
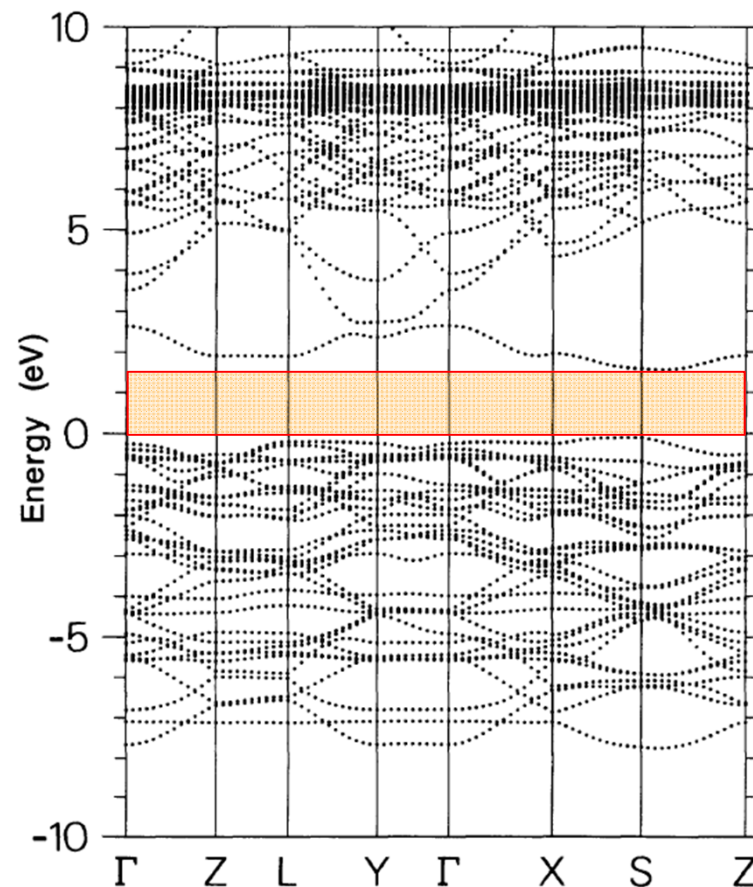


FIG. 1. Schematic diagram of the hybridization of the O hole ( $2p^5$ ) and Cu hole ( $3d^9$ ). The signs + and - represent the phase of the wave functions.

Zhang and Rice, Phys. Rev. B 37, 3759 (1988)

## LDA+U



- ZR singlets are truly many body states (1 Cu hole + 1 hole in ligand orbitals)
- They can be probed by photoemission because they can be reached by a one-particle excitation from the ground state with 1 hole per Cu site



# Doping a Mott Insulator: Spectral Weight Transfer

PHYSICAL REVIEW B

VOLUME 48, NUMBER 6

1 AUGUST 1993-II

## **Spectral-weight transfer: Breakdown of low-energy-scale sum rules in correlated systems**

M. B. J. Meinders

*Materials Science Centre, Department of Solid State and Applied Physics, University of Groningen, Nijenborgh 4, 9747 AG Groningen, The Netherlands*

H. Eskes

*Max-Planck-Institut für Festkörperforschung, Heisenbergstrasse 1, D-7000 Stuttgart 80, Federal Republic of Germany*

G. A. Sawatzky

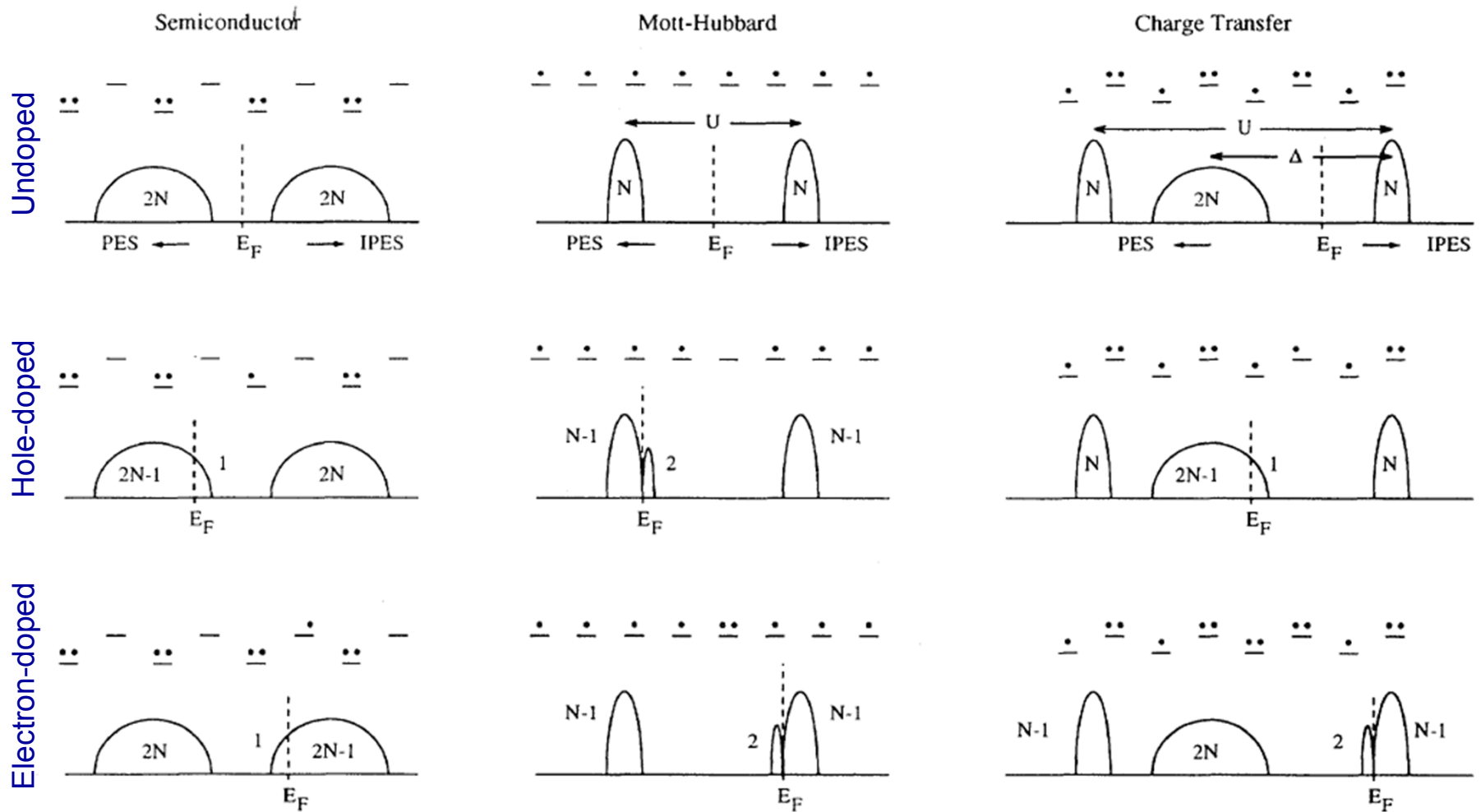
*Materials Science Centre, Department of Solid State and Applied Physics, University of Groningen, Nijenborgh 4, 9747 AG Groningen, The Netherlands*

(Received 4 March 1993)

In this paper we study the spectral-weight transfer from the high- to the low-energy scale by means of exact diagonalization of finite clusters for the Mott-Hubbard and charge-transfer model. We find that the spectral-weight transfer is very sensitive to the hybridization strength as well as to the amount of doping. This implies that the effective number of low-energy degrees of freedom is a function of the hybridization and therefore of the volume and temperature. In this sense it is not possible to define a Hamiltonian which describes the low-energy-scale physics unless one accepts an effective nonparticle conservation.

It is the connection between low and high energy scales that distinguishes the Mott gap from a more conventional gap (i.e., semiconductor, CDW, etc.)

# Doping a Mott Insulator: Spectral Weight Transfer



It is the connection between low and high energy scales that distinguishes the Mott gap from a more conventional gap (i.e., semiconductor, CDW, etc.)

# Doping a Mott Insulator: Spectral Weight Transfer

Meinders, Eskes, Sawatzky, PRB 48, 3916 (1993)

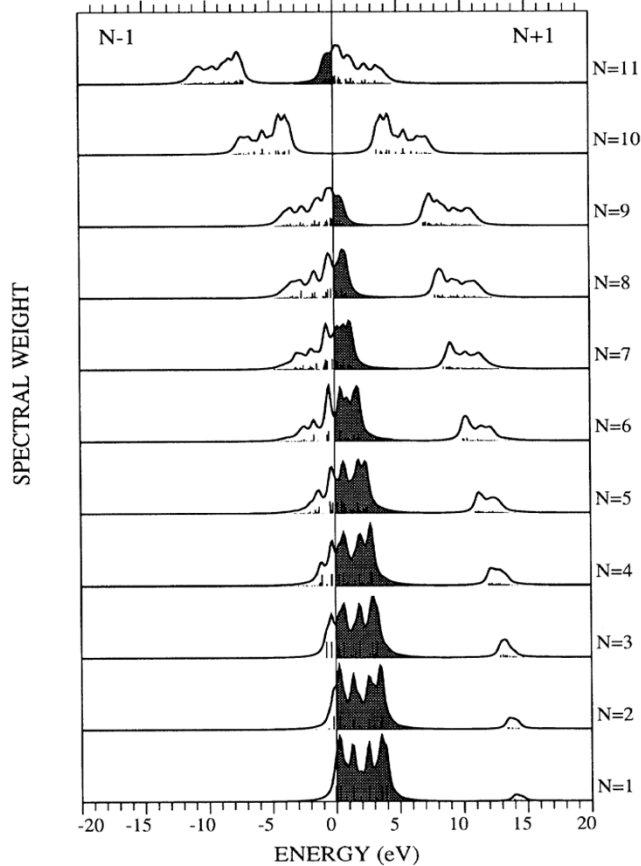


FIG. 2. One-particle Green's function for a one-dimensional Hubbard-ring of  $N = 10$  sites for  $U = 10$  eV and  $t = 1$  eV. The number of electrons in the ground state  $N$  are indicated. The low-energy electron-addition spectral weight is obtained by integration over the shaded area.

C.T. Chen et al., PRL 66, 104 (1991)

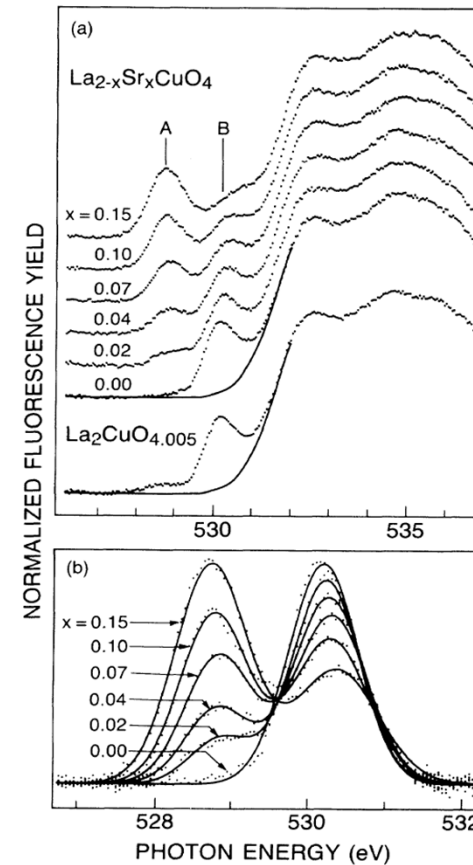


FIG. 1. (a) Normalized fluorescence yield at the O K edge of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_{4+\delta}$ . The solid curves are the common background described in the text. (b) The difference between the data of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  and the common background. The solid lines are the fitted curves using two Gaussian line shapes.

It is the connection between low and high energy scales that distinguishes the Mott gap from a more conventional gap (i.e., semiconductor, CDW, etc.)



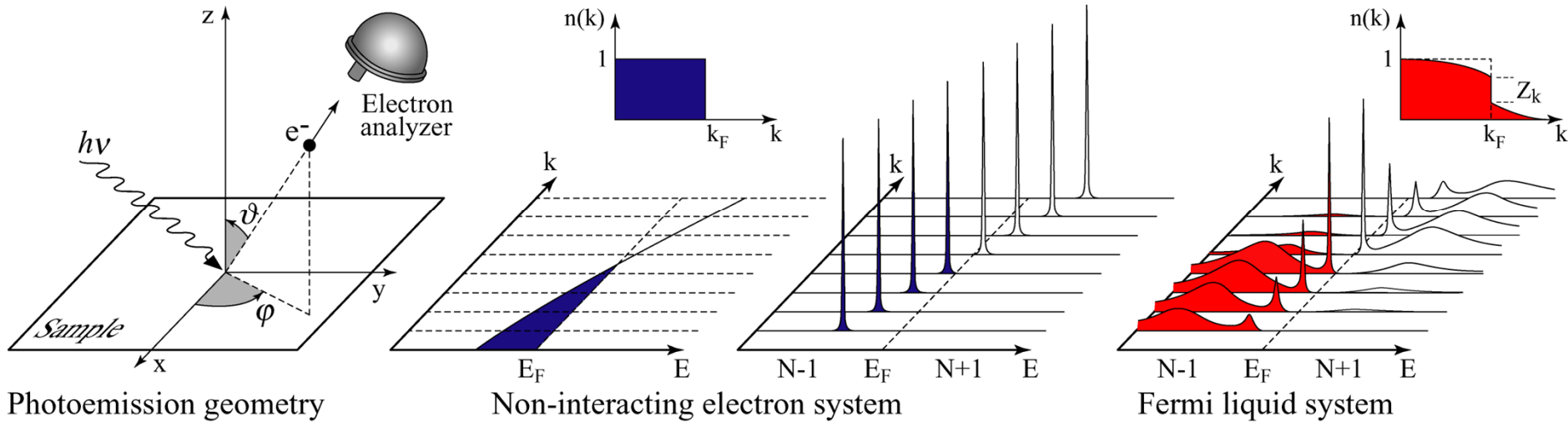
## Outline Part II

# Sudden approximation and quasiparticle renormalization

CUSO Lecture – Lausanne 02/2011

# ARPES: Interacting Systems

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



**Photoemission intensity:**  $I(\mathbf{k}, E_{kin}) = \sum_{f,i} w_{f,i}$

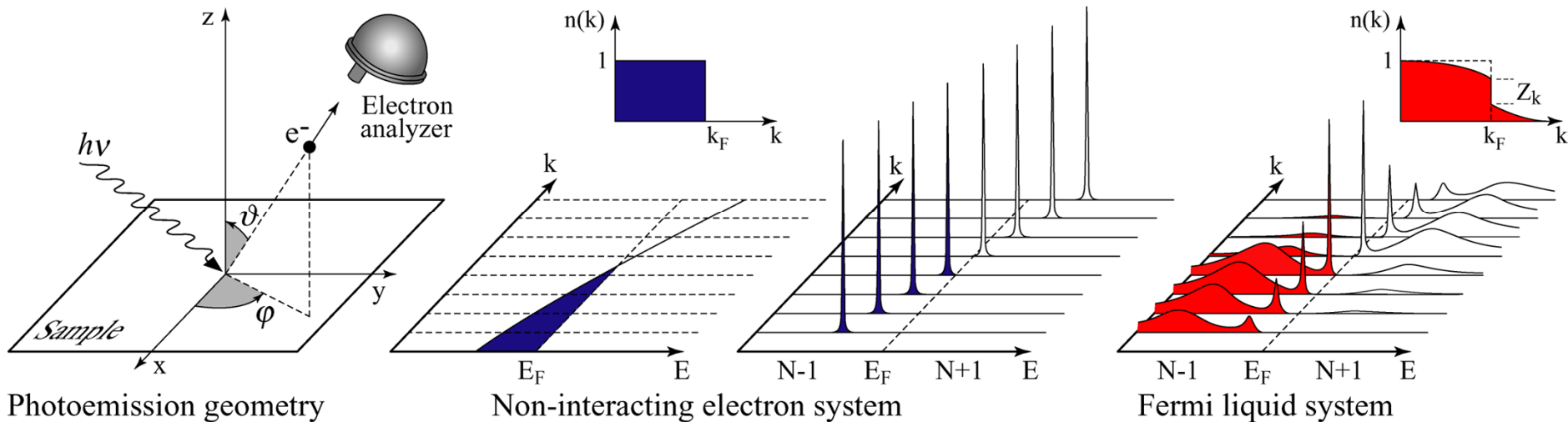
$$I(\mathbf{k}, E_{kin}) \propto \sum_{f,i} |M_{f,i}^{\mathbf{k}}|^2 \sum_m |c_{m,i}|^2 \delta(E_{kin} + E_m^{N-1} - E_i^N - h\nu)$$

$$|M_{f,i}^{\mathbf{k}}|^2 \equiv |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle|^2 \quad |c_{m,i}|^2 = |\langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2$$

**In general**  $\Psi_i^{N-1} = c_{\mathbf{k}} \Psi_i^N$  **NOT orthogonal**  $\Psi_m^{N-1}$

# ARPES: Interacting Systems

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



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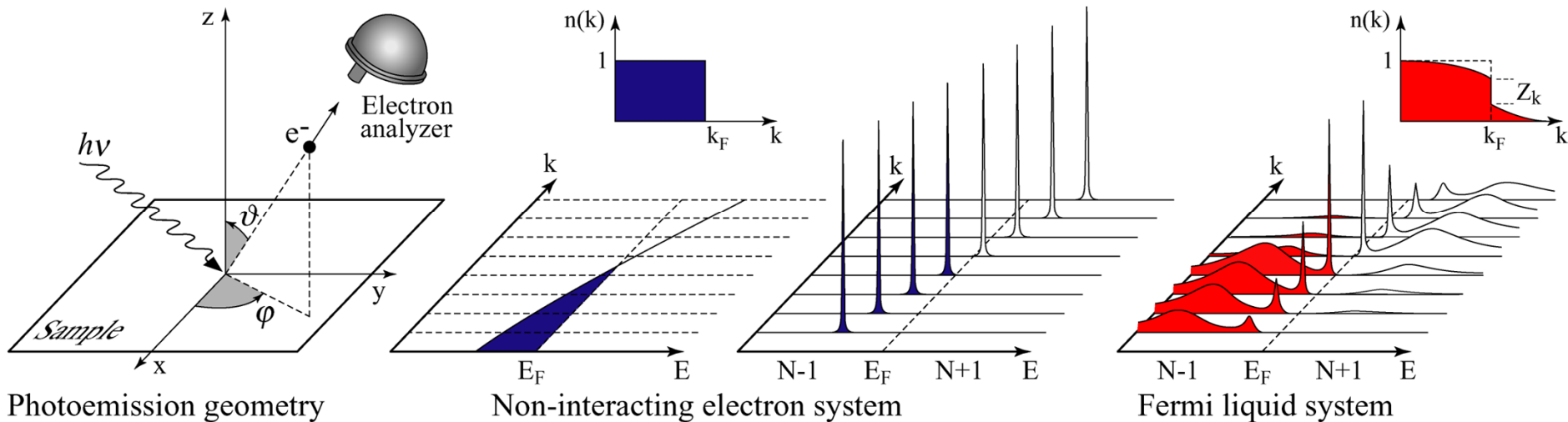
$$|M_{f,i}^{\mathbf{k}}|^2 \equiv |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle|^2 \quad |c_{m,i}|^2 = |\langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2$$

**“Like removing a stone from a water bucket”**



# ARPES: Fermi Liquid Description

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



**Photoemission intensity:**  $I(\mathbf{k}, \omega) = I_0 |M(\mathbf{k}, \omega)|^2 f(\omega) A(\mathbf{k}, \omega)$

**Non-interacting**

$$A(\mathbf{k}, \omega) = \delta(\omega - \epsilon_{\mathbf{k}})$$

No Renormalization  
Infinite lifetime

**Fermi Liquid**

$$A(\mathbf{k}, \omega) = Z_{\mathbf{k}} \frac{\Gamma_{\mathbf{k}}/\pi}{(\omega - \epsilon_{\mathbf{k}})^2 + \Gamma_{\mathbf{k}}^2} + A_{inc}$$

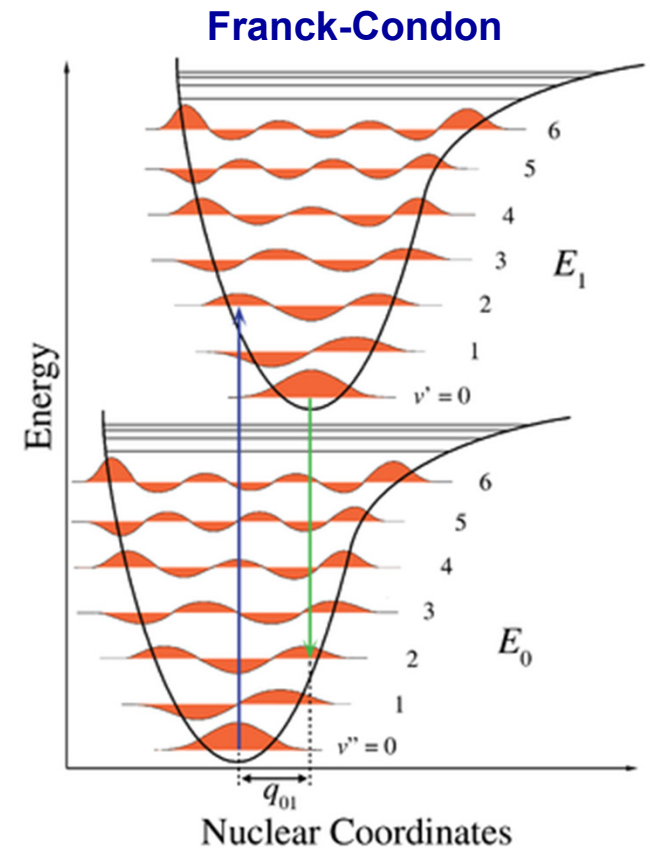
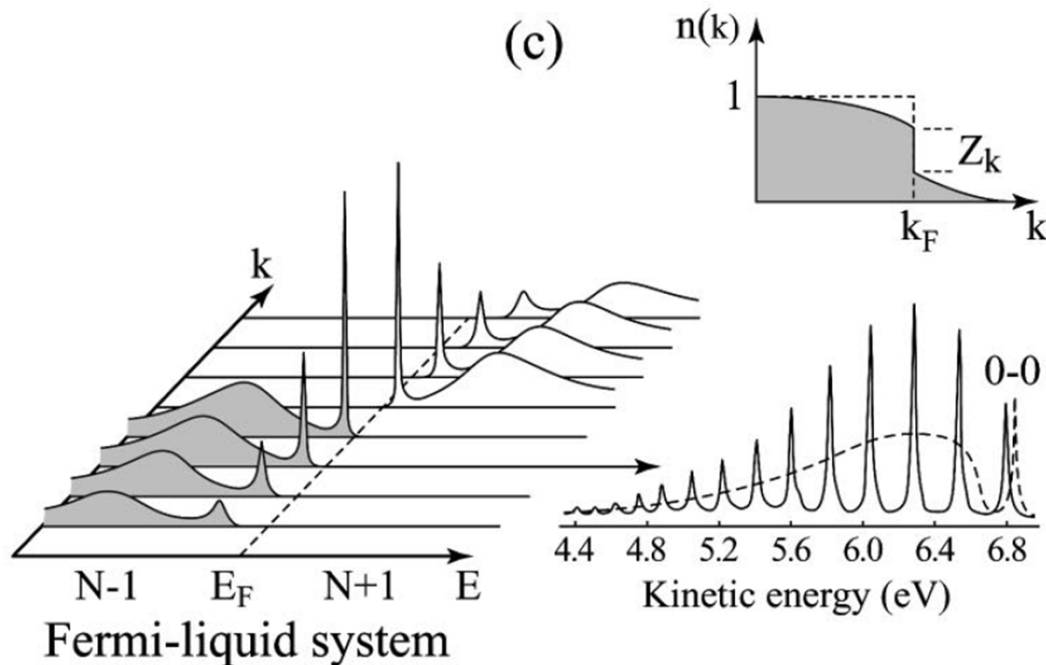
$$m^* > m \quad |\epsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$

$\Sigma(\mathbf{k}, \omega)$  : the “self-energy” captures the effects of interactions

# Testing Fermi-liquid models

G.A. Sawatzky



“In gaseous hydrogen, the equilibrium bond length is dependent on the degree of occupation of that level. The electrons are dressed by interatomic displacements. The intensities are given by the Franck-Condon factors, the molecular equivalent of the sudden approximation. The ARPES spectrum of solid hydrogen, developed from the molecular spectrum, will be angle dependent but for some angle will resemble the broken line. The fundamental transition (0-0) becomes the solid state quasiparticle peak. The phonon excitations develop into a broad, incoherent quasicontinuum.”

# Development of Low-Energy LASER-ARPES

PRL 94, 057001 (2005)

PHYSICAL REVIEW LETTERS

week ending  
11 FEBRUARY 2005

## Photoemission Spectroscopic Evidence of Gap Anisotropy in an $f$ -Electron Superconductor

T. Kiss,<sup>1,\*</sup> F. Kanetaka,<sup>1</sup> T. Yokoya,<sup>1,†</sup> T. Shimojima,<sup>1</sup> K. Kanai,<sup>1</sup> S. Shin,<sup>1,2</sup> Y. Onuki,<sup>3,4</sup> T. Togashi,<sup>2</sup> C. Zhang,<sup>5</sup>  
C. T. Chen,<sup>5</sup> and S. Watanabe<sup>1</sup>

<sup>1</sup>*Institute for Solid State Physics (ISSP), University of Tokyo, Kashiwa, Chiba 277-8581, Japan*

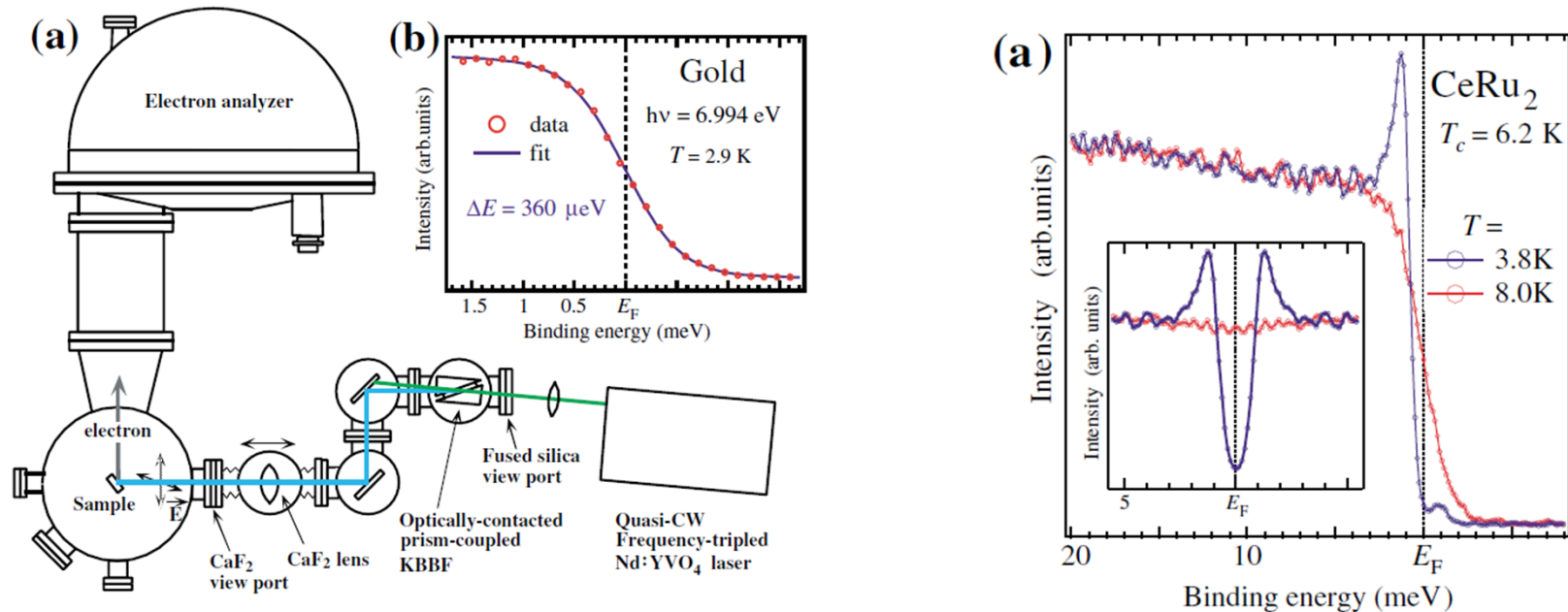
<sup>2</sup>*The Institute of Physical and Chemical Research (RIKEN), Sayo-gun, Hyogo 679-5143, Japan*

<sup>3</sup>*Graduate School of Science, Osaka University, Toyonaka, Osaka 560-0043, Japan*

<sup>4</sup>*Advanced Science Research Center, JAERI, Tokai Ibaraki 319-1195, Japan*

<sup>5</sup>*Beijing Center for Crystal R&D, Chinese Academy of Science, Zhongguancun, Beijing 100080, China*

(Received 5 June 2004; published 7 February 2005)



# Development of Low-Energy LASER-ARPES

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C. T. Chen,<sup>5</sup> and S. Watanabe<sup>1</sup>

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<sup>2</sup>*The Institute of Physical and Chemical Research (RIKEN), Sayo-gun, Hyogo 679-5143, Japan*

<sup>3</sup>*Graduate School of Science, Osaka University, Toyonaka, Osaka 560-0043, Japan*

<sup>4</sup>*Advanced Science Research Center, JAERI, Tokai Ibaraki 319-1195, Japan*

<sup>5</sup>*Beijing Center for Crystal R&D, Chinese Academy of Science, Zhongguancun, Beijing 100080, China*

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Low energy ARPES is now becoming popular as a new tool for spectroscopy

Advantages: Higher bulk sensitivity: material specific, depending on relaxations  
Narrow excitation linewidth: higher energy resolution  
Smaller light spot: higher angular resolution

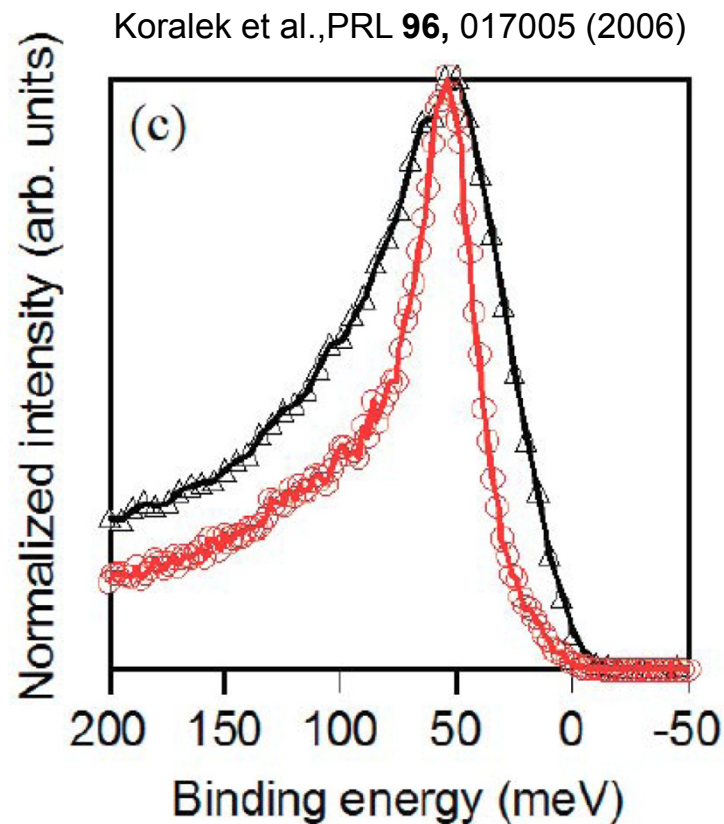
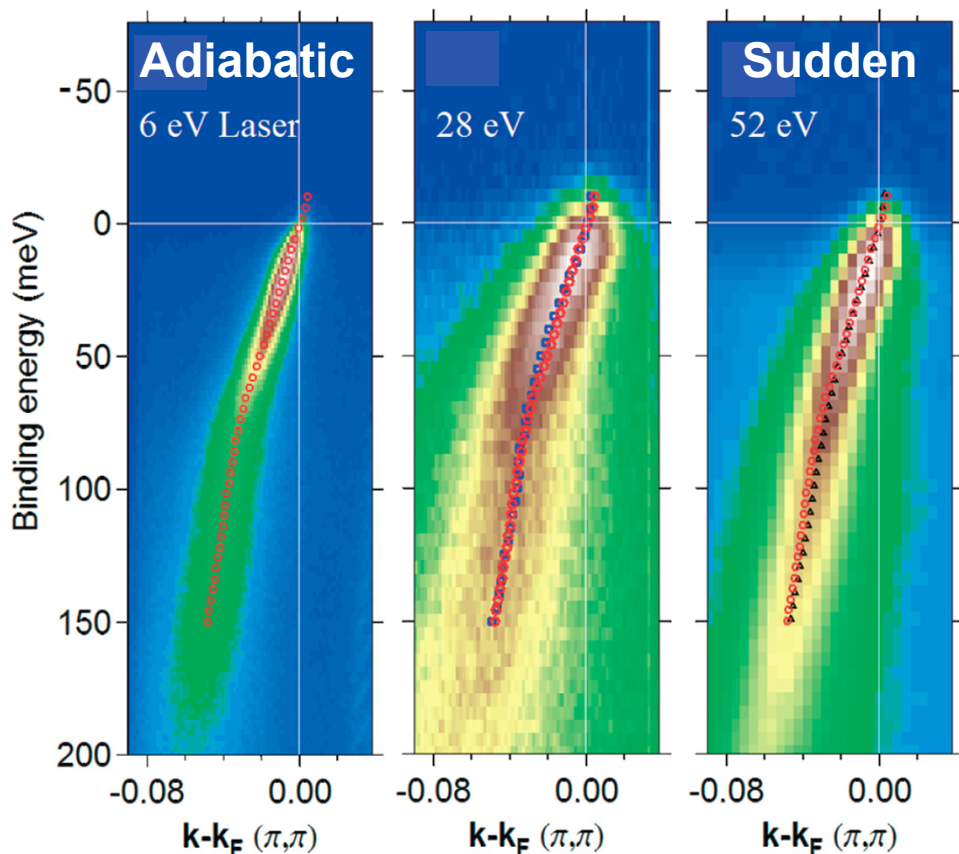
Drawbacks: Breakdown of sudden approximation?  
Higher sensitivity to final state effects  
Smaller amount of k-space accessible

# Sudden approximation

$$w_{fi} \propto \left| \langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle \right|^2 \delta(\omega - h\nu)$$

The N-1 system eigenstates don't change

But the projection of final on initial states does!



The intensity changes but not the dispersion!

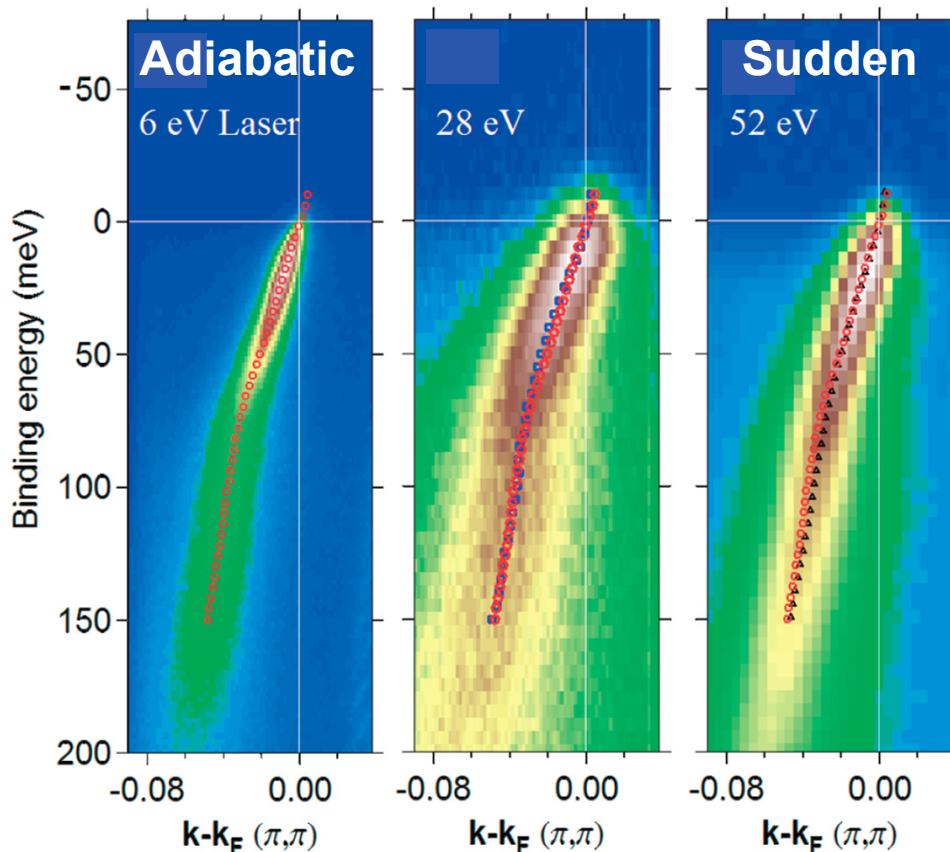


# Sudden approximation

$$w_{fi} \propto |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2 \delta(\omega - h\nu)$$

The N-1 system eigenstates don't change

But the projection of final on initial states does!



If the sudden approximation breaks down, the electron will be emitted with the highest possible kinetic energy and most of its spectral weight will be in a sharp line since the incoherent continuum is suppressed).

This does NOT prevent detecting features in the experiments due to correlation effects, because the (many-body) eigenstates of the N-1 particle system remain the same.

However, the ratio of intensity between coherent and incoherent parts of the spectral function will change, which WILL prevent a determination of Z from the evolution of the spectral weight detected by ARPES.

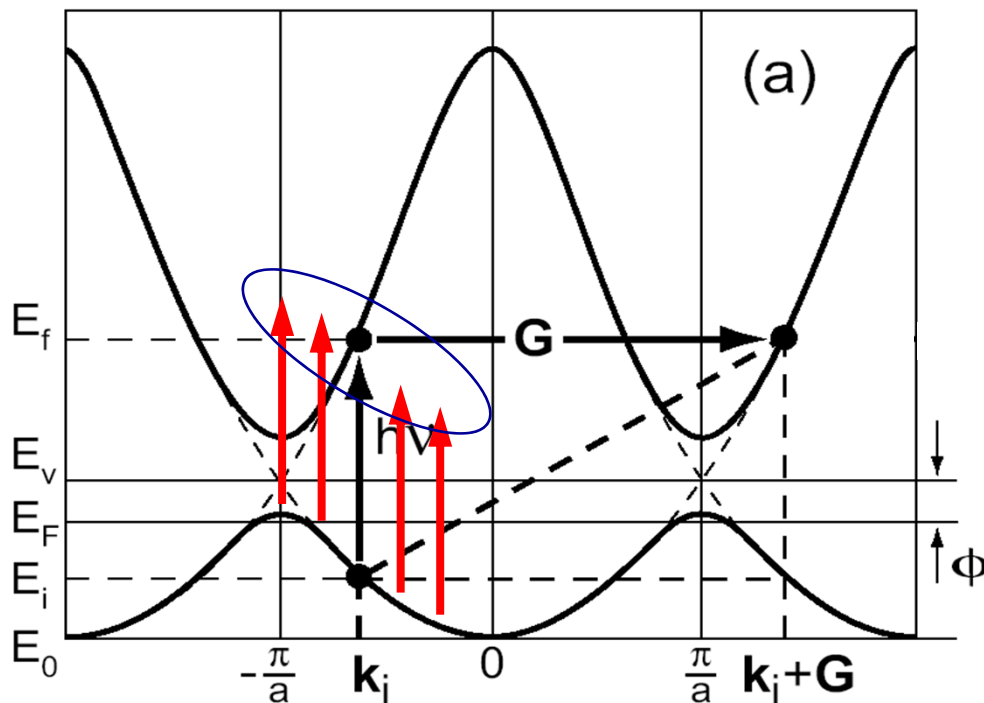
**The intensity changes but not the dispersion!**



# Low-Energy ARPES and Final State Effects

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(k, \omega) \end{array} \right\} w_{fi} \propto |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2 \delta(\omega - h\nu)$$

Excitation in the solid



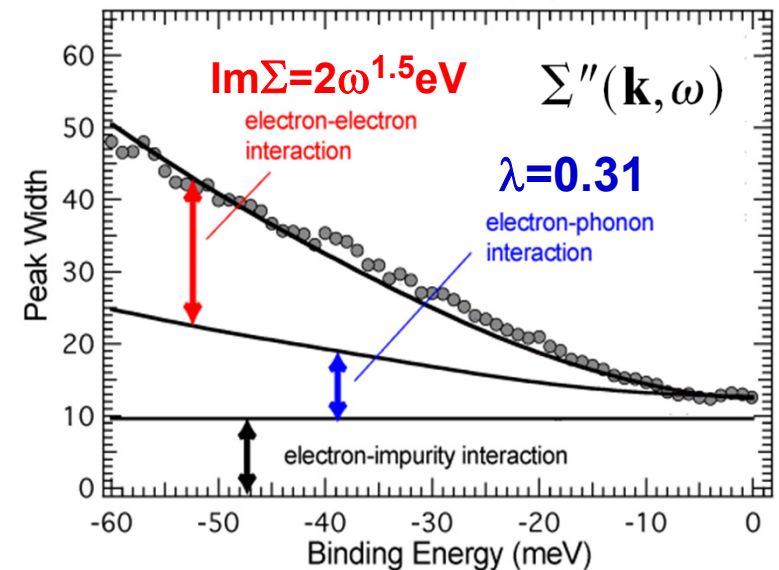
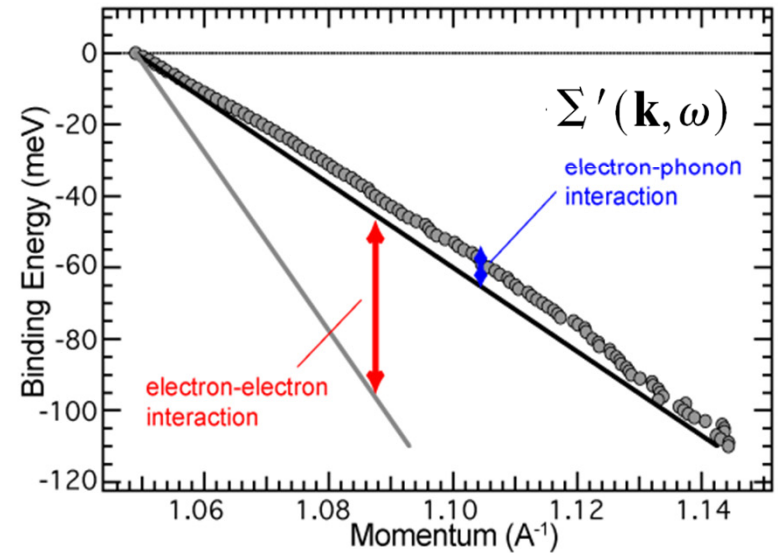
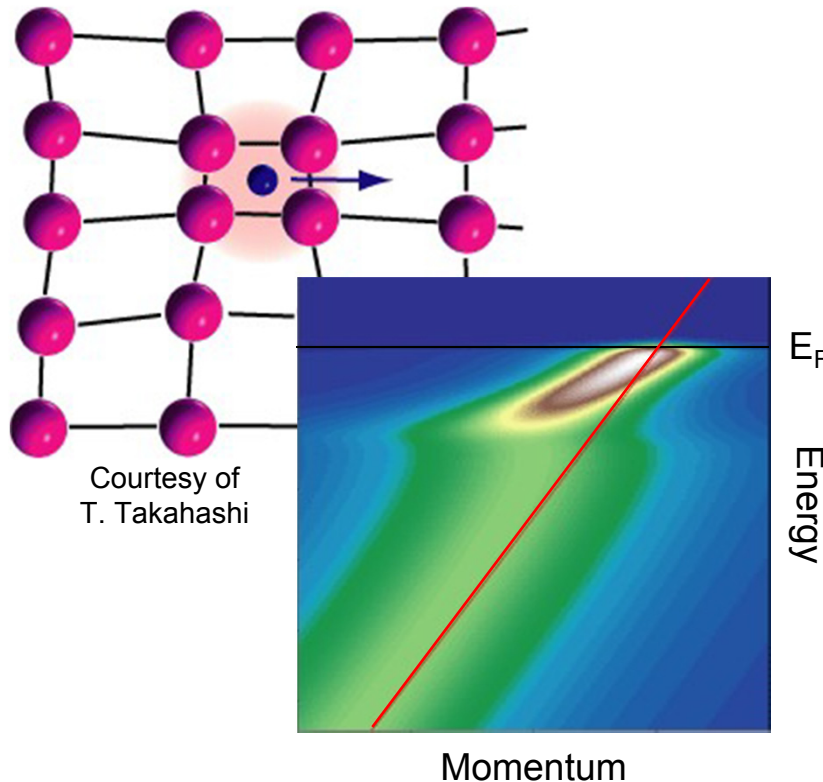
Working at high photon energies the electron is excited in a continuum of high-energy states; a final state is always available and the photoemission process can take place (with intensity still dependent on matrix elements).

At low photon energy photoemission is affected by the kinematic constrain deriving from energy and momentum conservation, and the  $k$ -dependent structure of the final states. For some initial state there is no final state that can be reached at a given photon energy and the intensity vanishes.

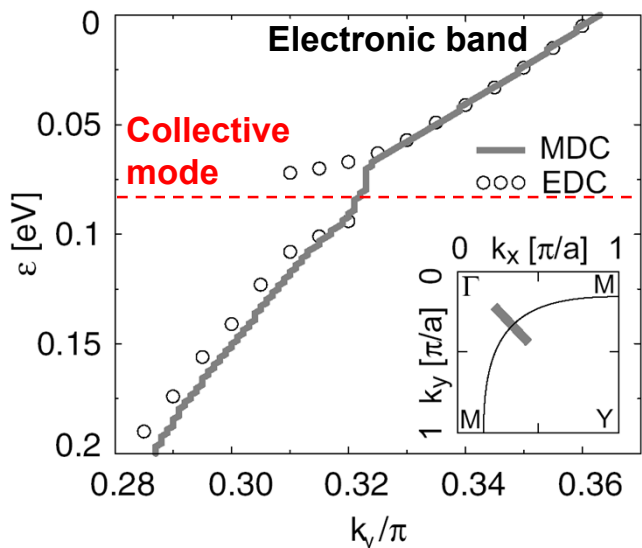
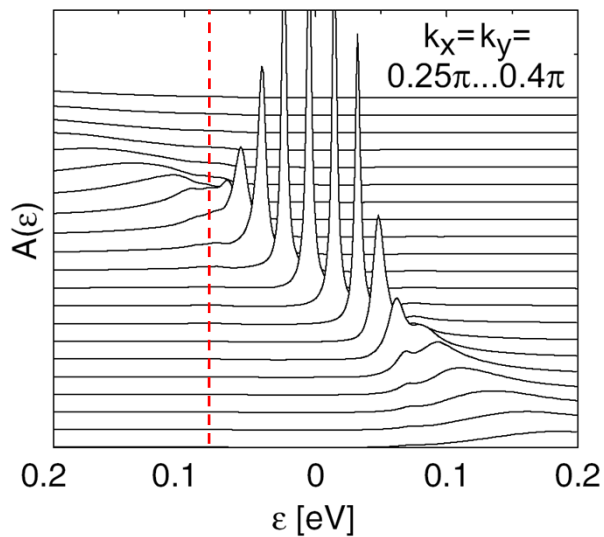
# Many-Body Correlation Effects in $\text{Sr}_2\text{RuO}_4$

## Single-particle spectral function

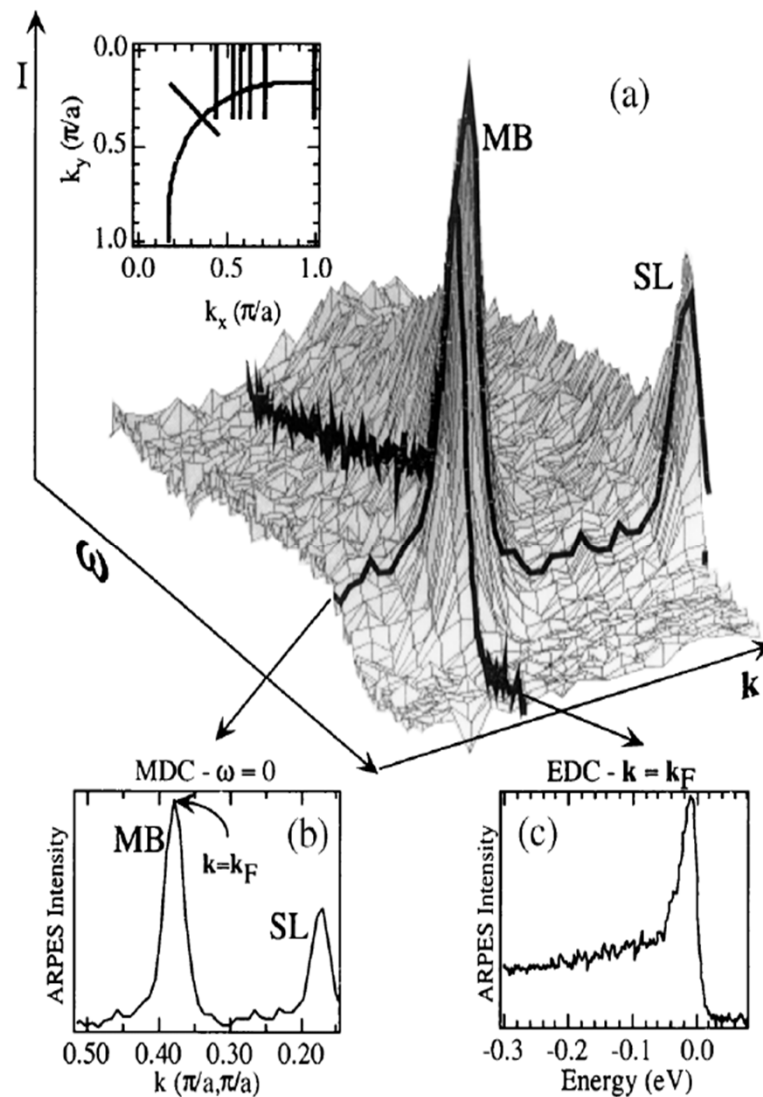
$$A(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\mathbf{k}, \omega)}{[\omega - \epsilon_{\mathbf{k}} - \Sigma'(\mathbf{k}, \omega)]^2 + [\Sigma''(\mathbf{k}, \omega)]^2}$$



# Many-Body Effects: Electron-Boson Coupling

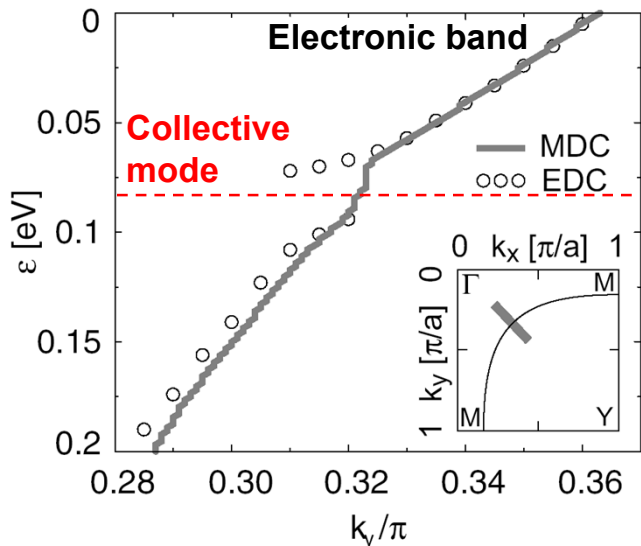
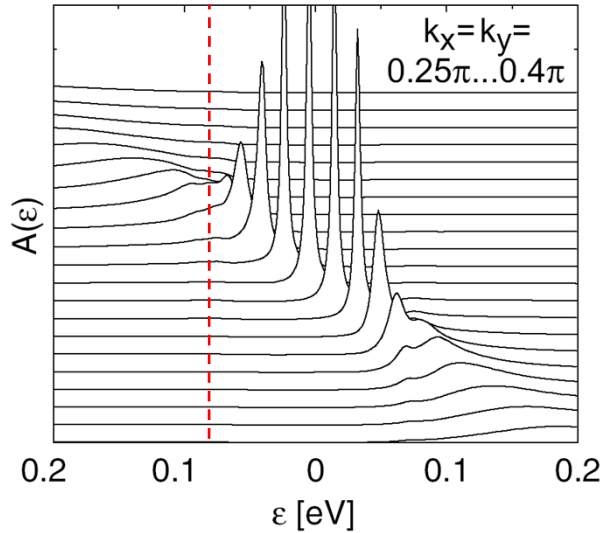


Eschrig, Norman, PRB **67**, 144503 (2003)



Kaminski et al., Phys. Rev. Lett. **86**, 1070 (2001)

# Many-Body Effects: Electron-Phonon Coupling

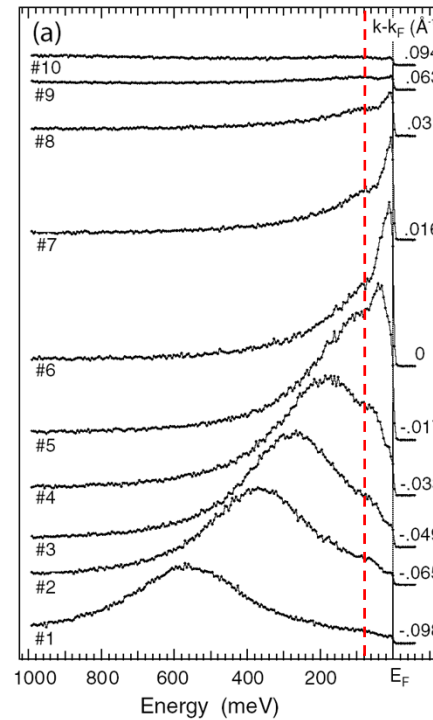


Eschrig, Norman, PRB **67**, 144503 (2003)

## Single-particle spectral function

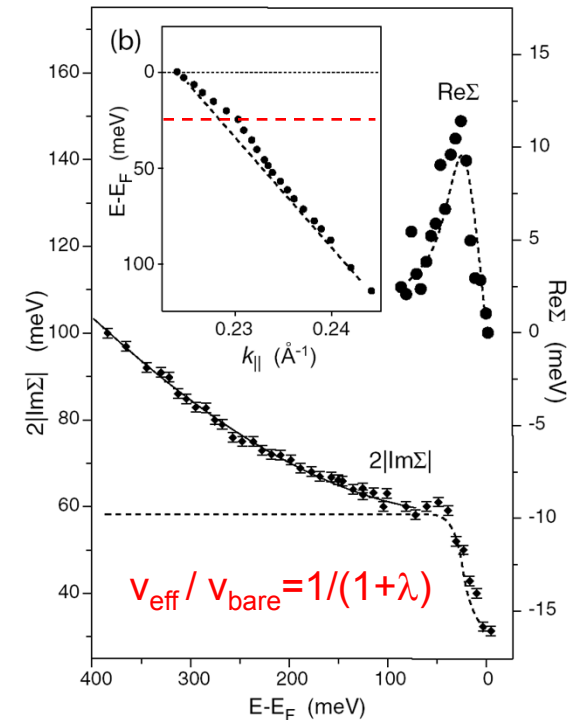
$$A(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\mathbf{k}, \omega)}{[\omega - \epsilon_{\mathbf{k}} - \Sigma'(\mathbf{k}, \omega)]^2 + [\Sigma''(\mathbf{k}, \omega)]^2}$$

## Be(0001)



Hengsberger *et al.*, PRL **83**, 592 (1999)

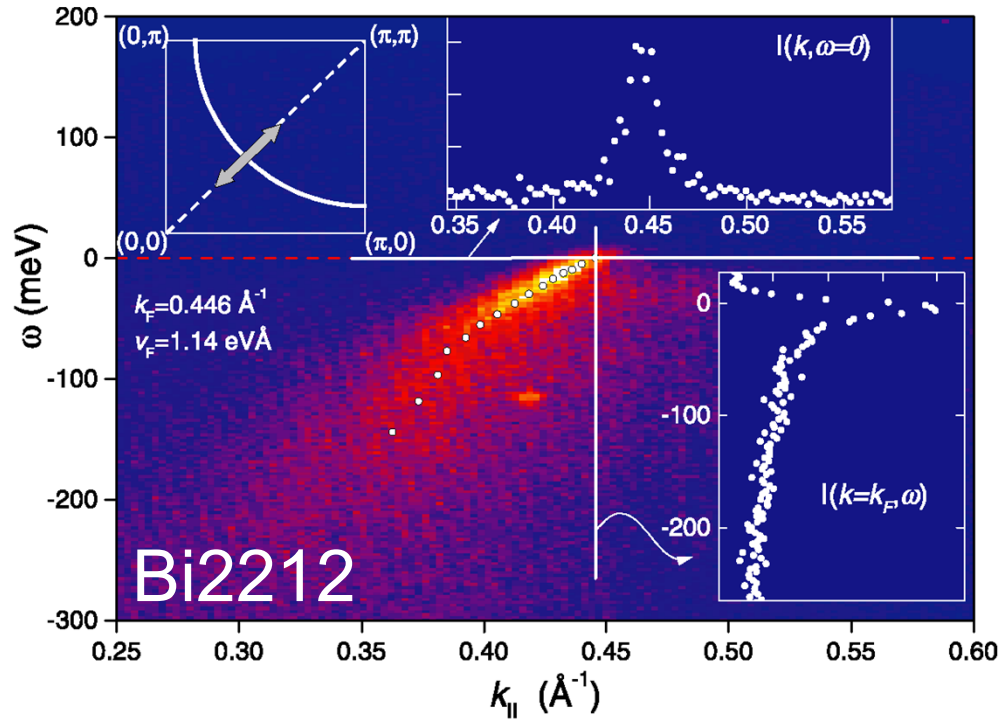
## Mo(110)



Valla *et al.*, PRL **83**, 2085 (1999)

# Many-Body effects in the High- $T_c$ Cuprates

Valla *et al.*, Science **285**, 2110 (1999)

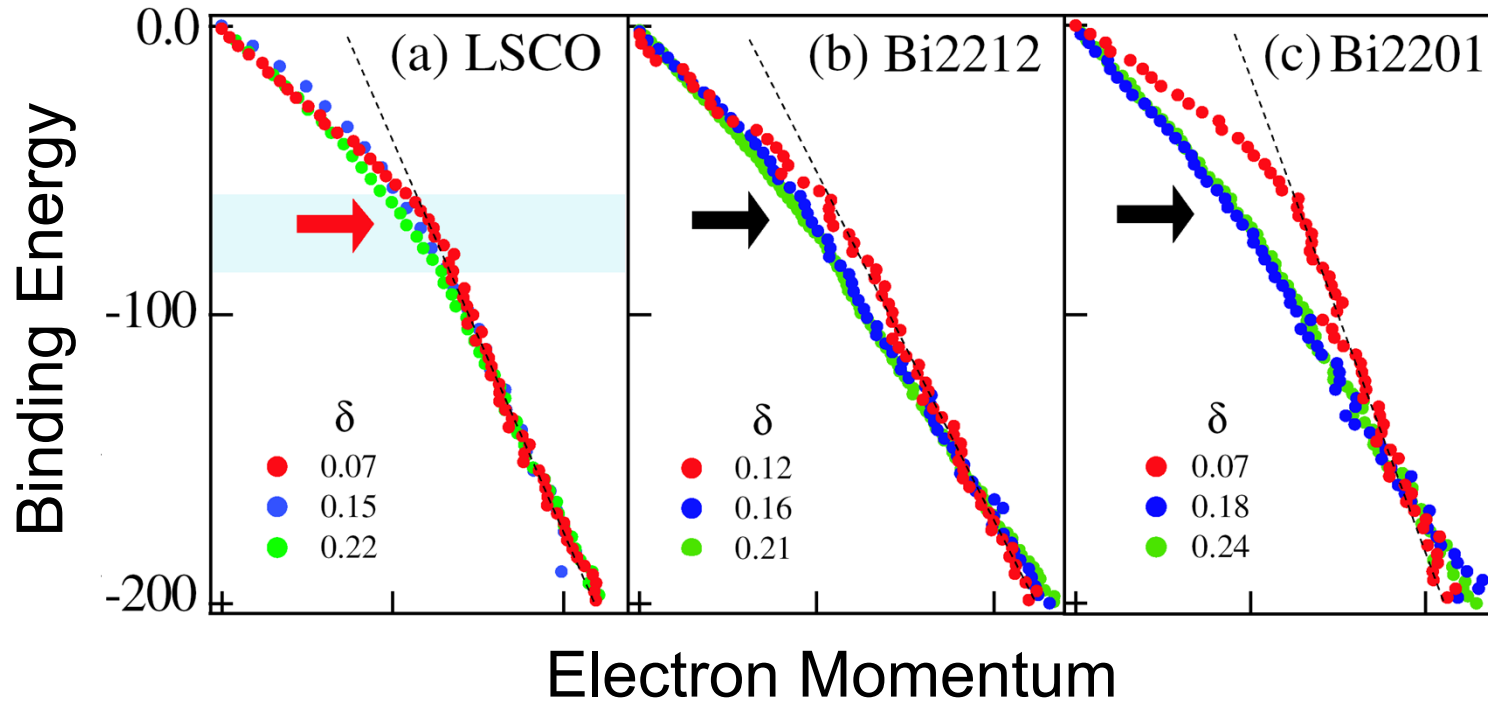


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Mechanism for High- $T_c$  { **Magnetic fluctuations ?**  
**Electron-phonon coupling ?**

# Many-Body effects in the High- $T_c$ Cuprates

Lanzara *et al.*, Nature **412**, 510 (2001)



Mechanism for High- $T_c$  { **Magnetic fluctuations ?**  
**Electron-phonon coupling ?**



# Many-Body effects in the High- $T_c$ Cuprates

Devereaux et al., Phys. Rev. Lett. **93**, 117004 (2004)

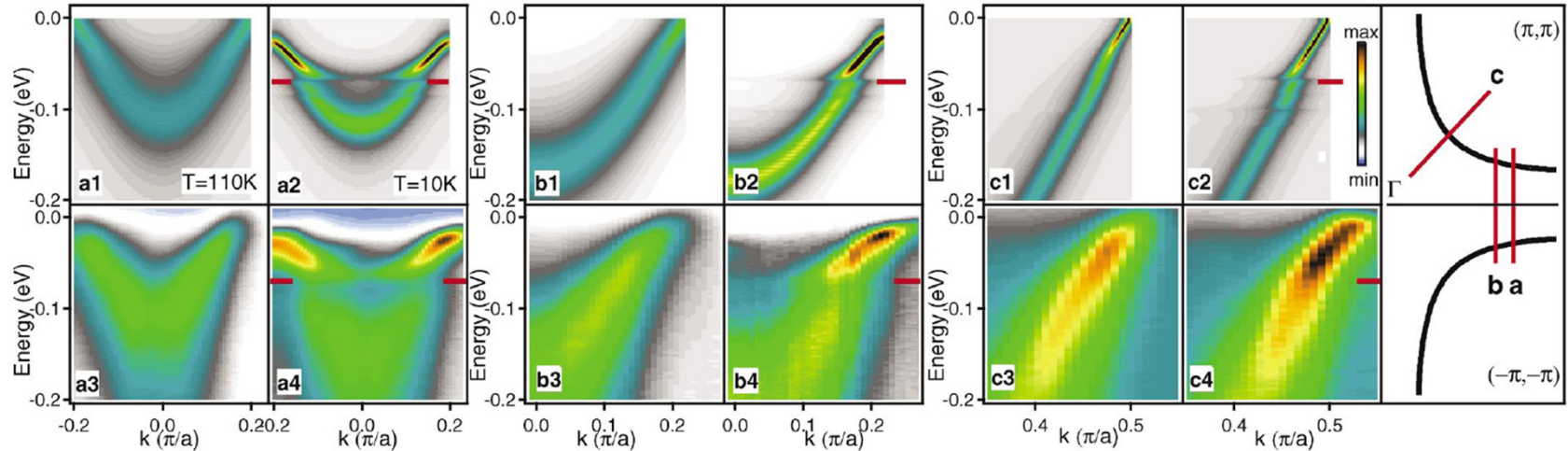
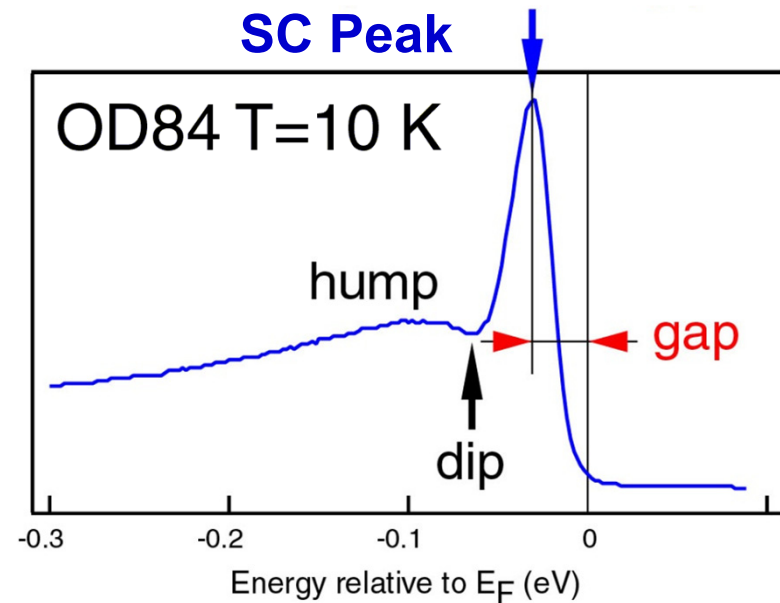
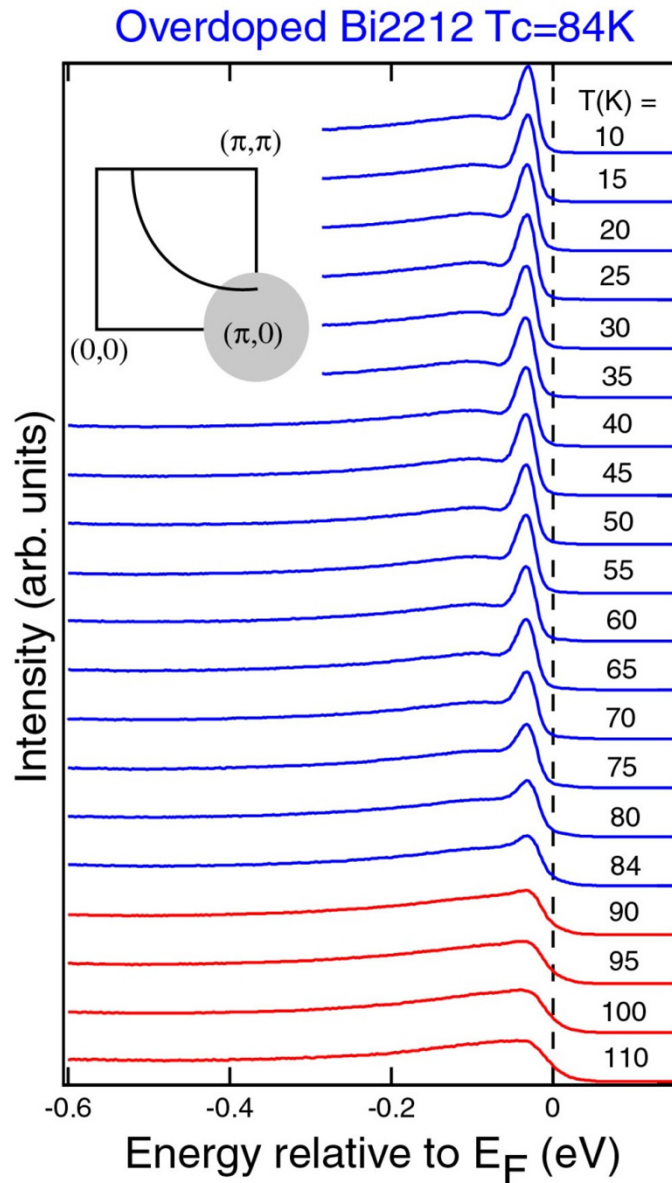


FIG. 3 (color). Image plots of the calculated spectral functions in the normal (a1,b1,c1) and superconducting (a2,b2,c2) states compared to the spectral functions in the normal (a3,b3,c3) and superconducting (a4,b4,c4) states measured in  $\text{Bi}_2\text{Sr}_2\text{Ca}_{0.92}\text{Y}_{0.08}\text{Cu}_2\text{O}_{8+\delta}$  (Bi-2212) [6] for momentum cuts  $a, b, c$  shown in the rightmost panel and in Fig. 2. The same color scale is used for the normal or superconducting pairs within each cut, but the scaling for the data and the calculation are separate. The red markers indicate 70 meV in the superconducting state.

Mechanism for High- $T_c$  { **Magnetic fluctuations ?**  
**Electron-phonon coupling ?**



# Many-body signatures in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

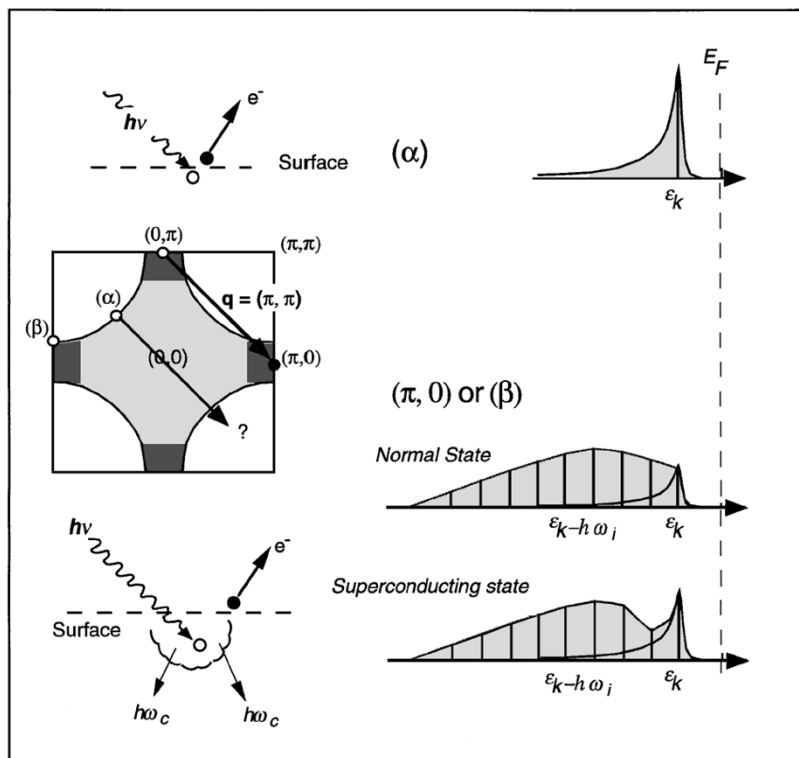


**Pairing**  
**d-wave SC Gap**

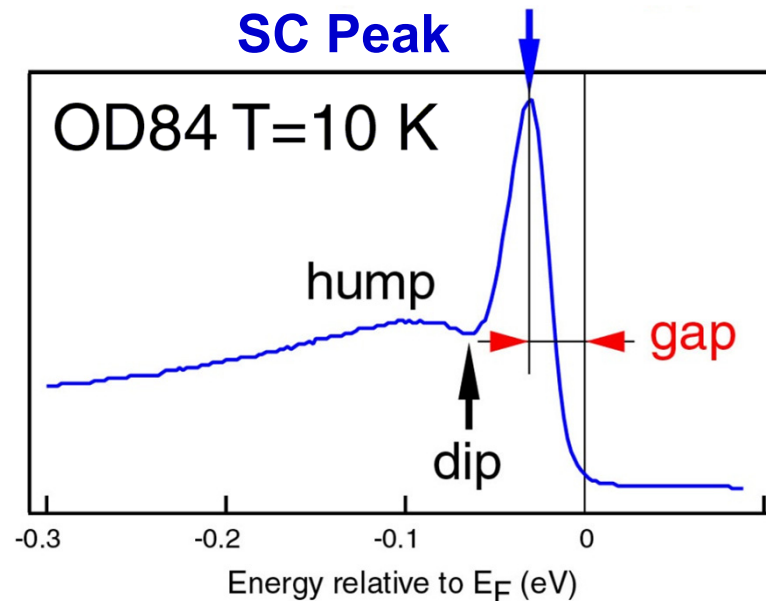
**Phase coherence**  
**Coherent QP weight**

# Many-body signatures in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

Electron-boson coupling?  
With a  $(\pi, \pi)$  collective mode?



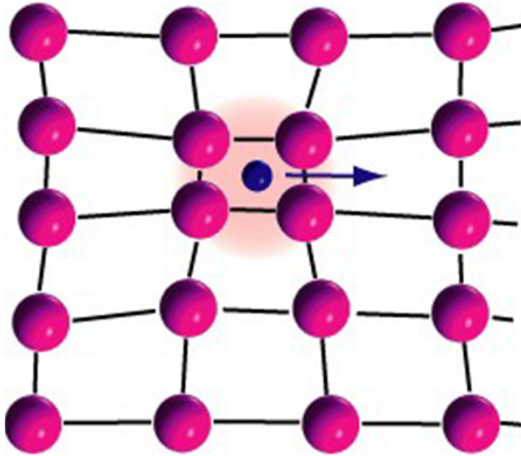
Shen and Schrieffer, Phys. Rev. Lett. **78**, 1771 (1997).



**Pairing**  
**d-wave SC Gap**  
**Phase coherence**  
**Coherent QP weight**

# Renormalization of Polaronic Quasiparticles

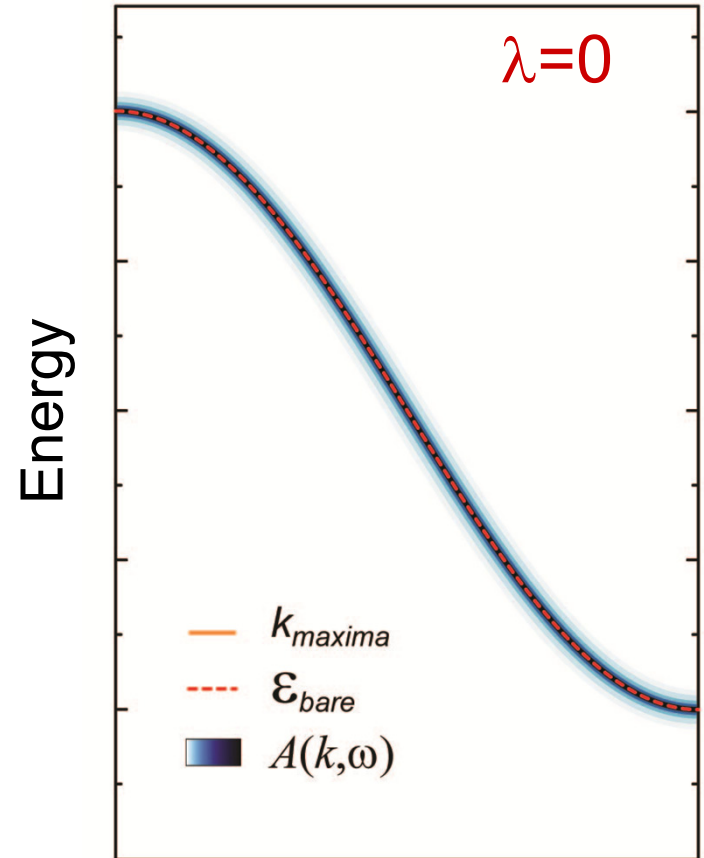
$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$



$$A(\mathbf{k}, \omega) = Z_{\mathbf{k}} \frac{\Gamma_{\mathbf{k}}/\pi}{(\omega - \varepsilon_{\mathbf{k}})^2 + \Gamma_{\mathbf{k}}^2} + A_{inc}$$

$$m^* > m \quad |\varepsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

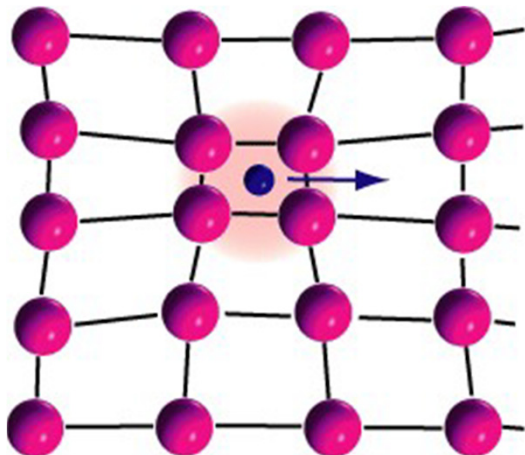
$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$



Momentum

# Renormalization of Polaronic Quasiparticles

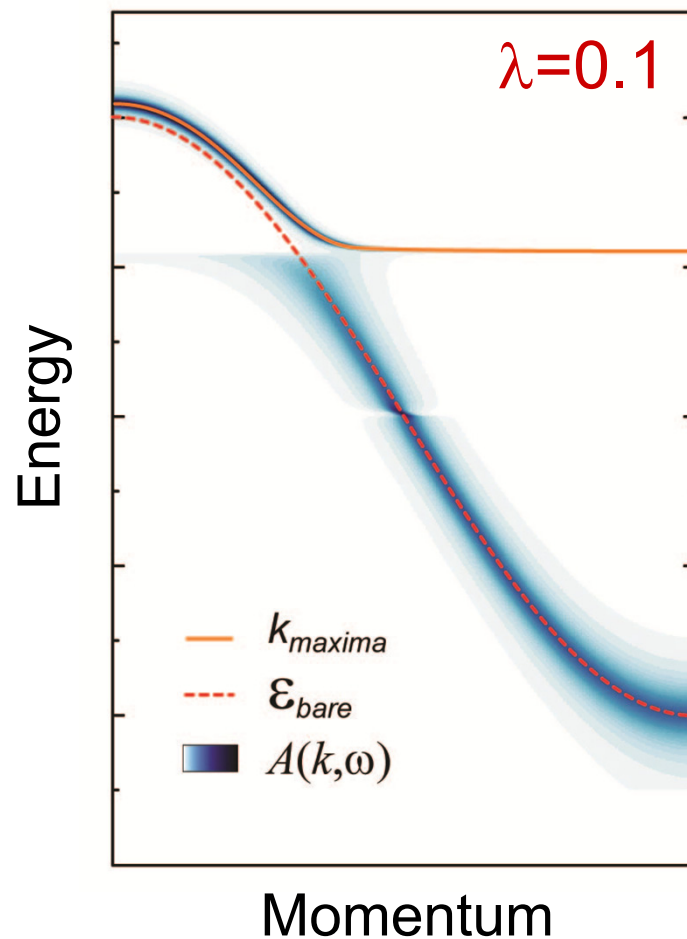
$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$



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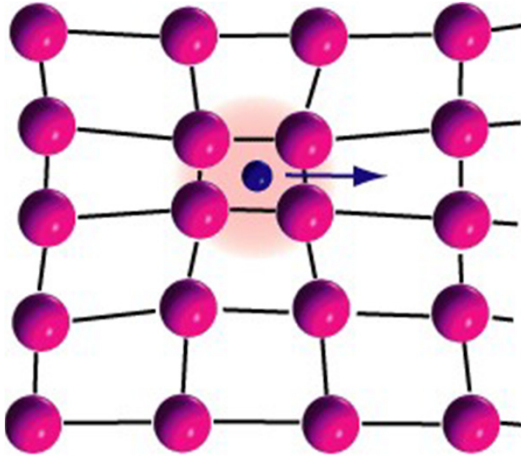
$$m^* > m \quad |\varepsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$



# Renormalization of Polaronic Quasiparticles

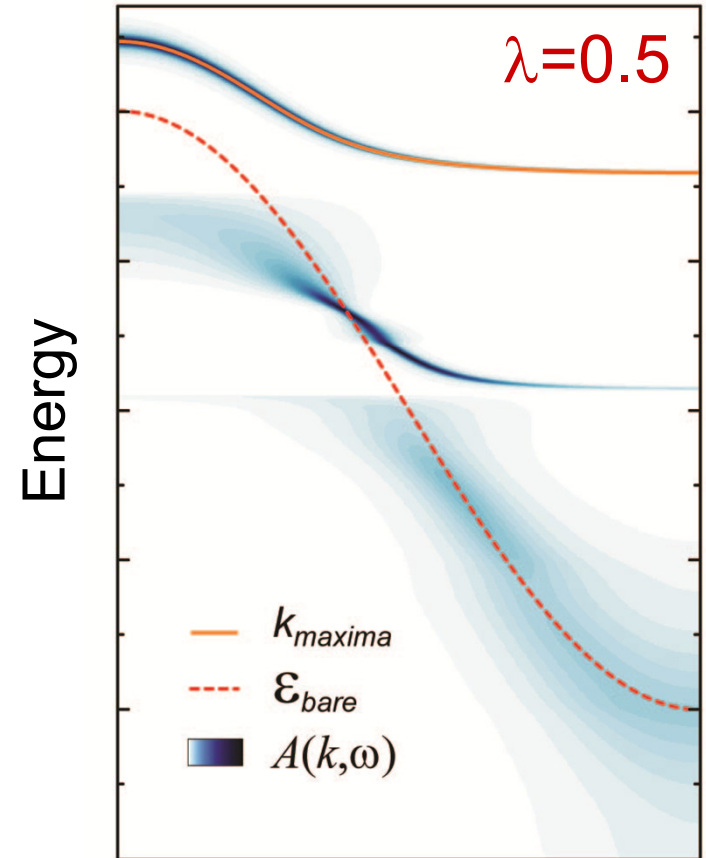
$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$



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$$m^* > m \quad |\varepsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

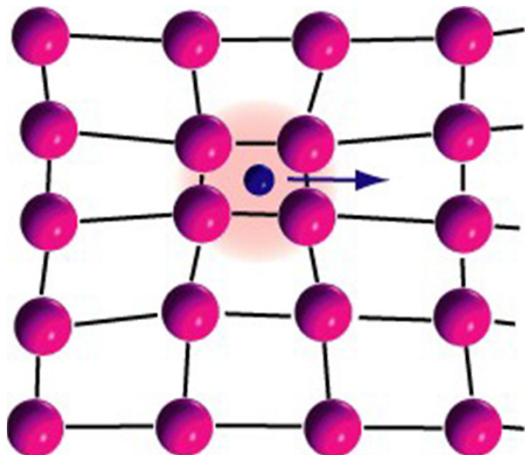
$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$



Momentum

# Renormalization of Polaronic Quasiparticles

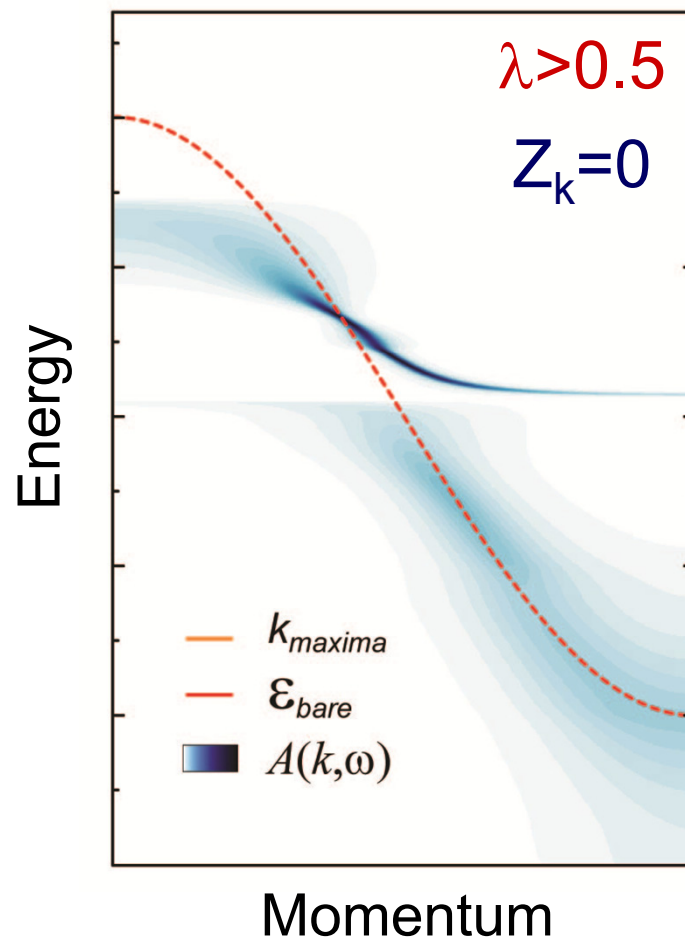
$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$



$$A(\mathbf{k}, \omega) = Z_{\mathbf{k}} \frac{\Gamma_{\mathbf{k}}/\pi}{(\omega - \varepsilon_{\mathbf{k}})^2 + \Gamma_{\mathbf{k}}^2} + A_{inc}$$

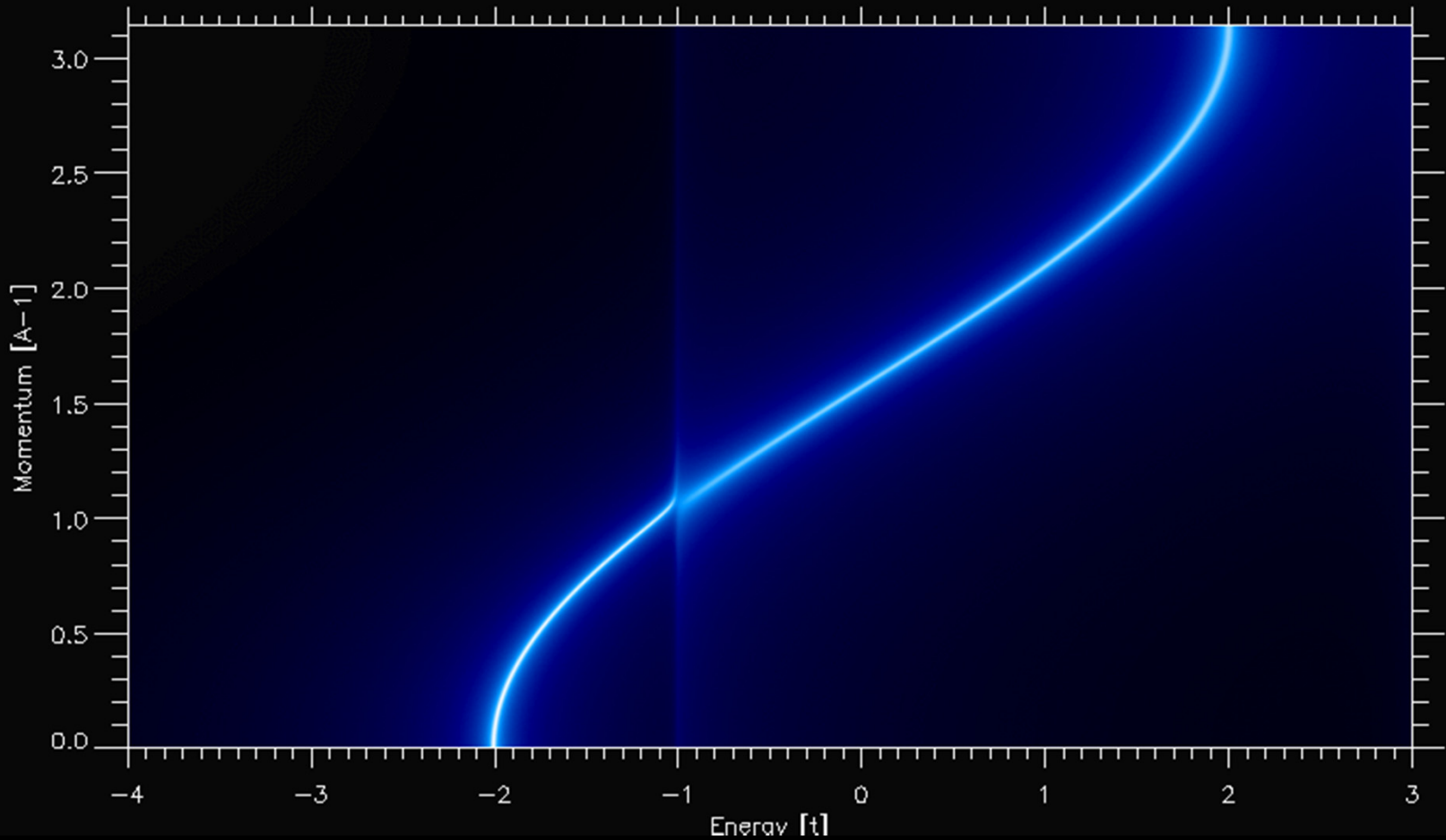
$$m^* > m \quad |\varepsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$





$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$



Veenstra, Goodvin, Berciú, Damascelli, PRB **82**, 012504 (2010)

# Renormalization of Polaronic Quasiparticles

$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$

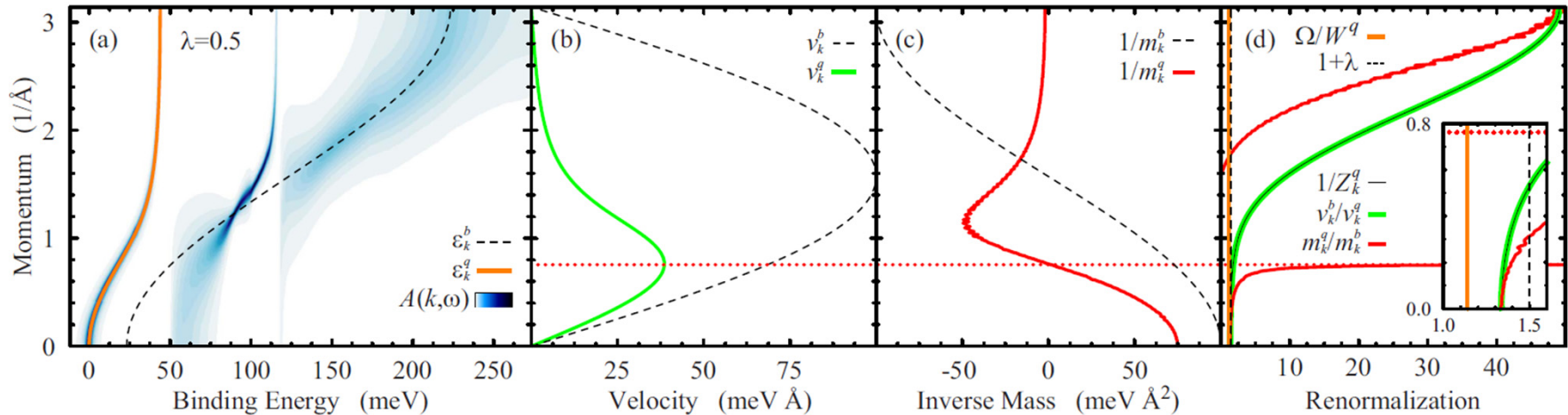
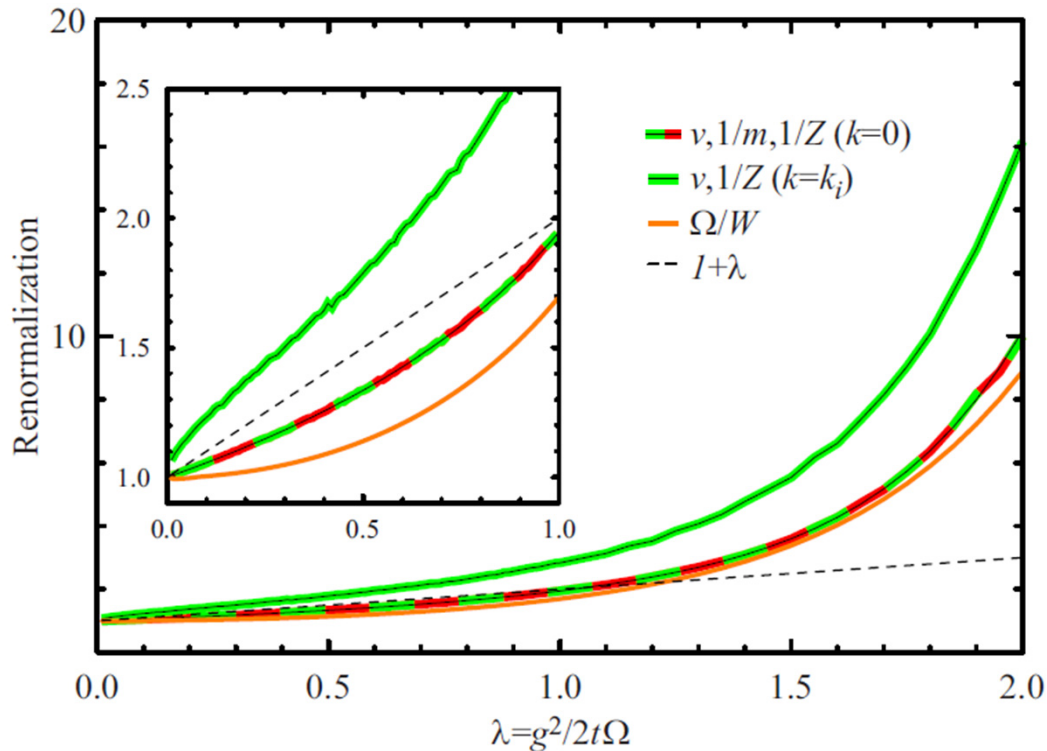


FIG. 1. (Color online) (a)  $A(k, \omega)$  calculated within MA<sup>(1)</sup> for  $\Omega=50$  meV and  $\lambda=0.5$ ; the quasiparticle dispersion  $\varepsilon_k^q$  and the bare band  $\varepsilon_k^b$  are also shown. (b) Quasiparticle and bare-band velocities,  $v_k^q$  and  $v_k^b$ , and (c) corresponding inverse masses,  $1/m_k^q$  and  $1/m_k^b$ , according to the definitions  $v_k = \partial \varepsilon_k / \partial k$  and  $1/m_k = \partial^2 \varepsilon_k / \partial k^2$ . (d) Momentum-dependent quasiparticle renormalization as obtained from  $v_k^b/v_k^q$ ,  $m_k^q/m_k^b$ , and the inverse quasiparticle coherence  $1/Z_k^q$ , where  $Z_k^q = \int^q A(k, \omega) d\omega$  is the quasiparticle-only integrated spectral weight; in the inset, these quantities are compared near  $k=0$  to the renormalization factors  $\Omega/W^q$  and  $(1+\lambda)$ , obtained from quasiparticle bandwidth  $W^q$  and dimensionless coupling  $\lambda = g^2/2t\Omega$  in our model.

Far from the Migdal limit ( $\Omega \ll E_F$  for a parabolic band), the effective coupling parameters deduced from the renormalization of quasiparticle mass, velocity, and spectral weight are momentum dependent and, in general, distinct from the true microscopic coupling; the latter is thus not readily accessible in the quasiparticle dispersion revealed by ARPES through the mass enhancement factor  $1/(1+\lambda)$ .

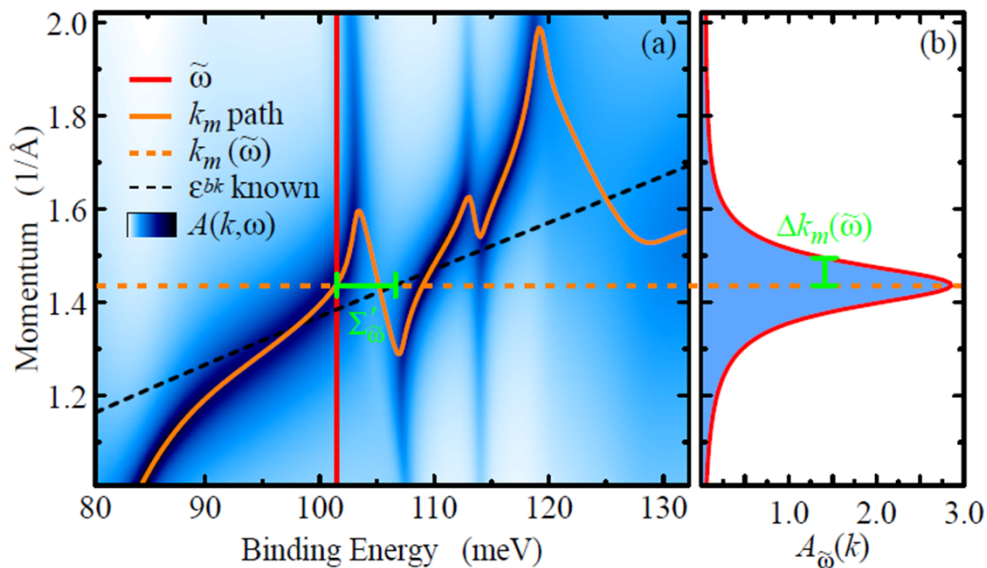
# Renormalization of Polaronic Quasiparticles

$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$

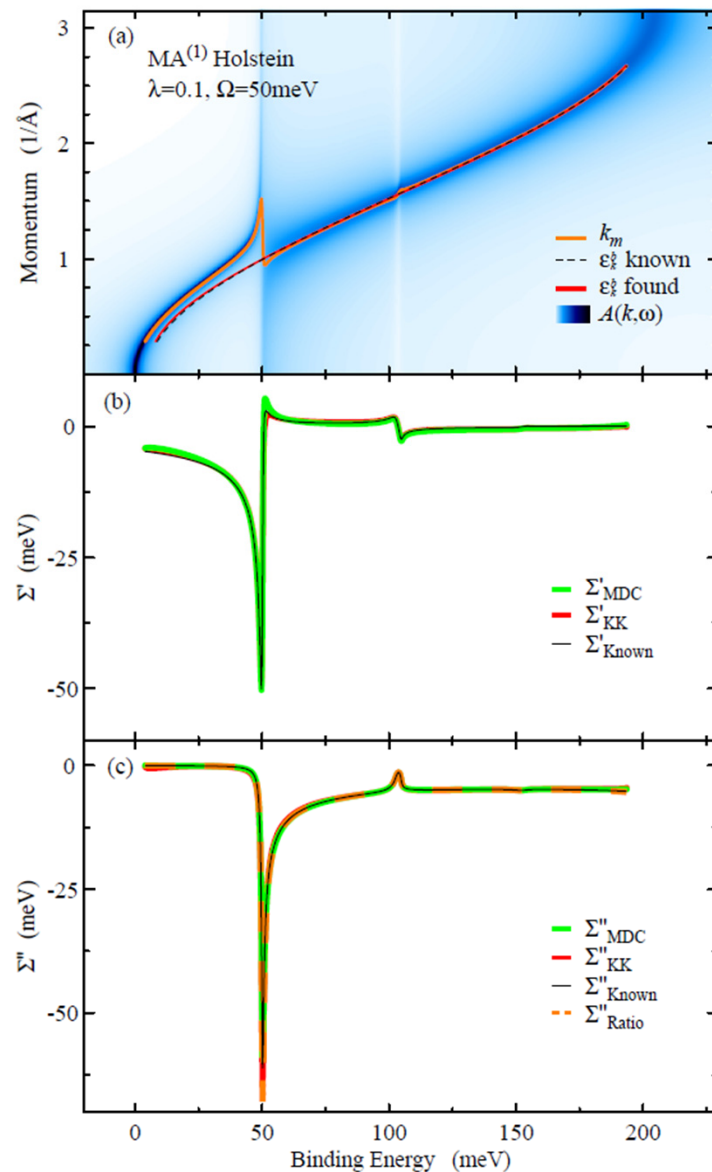


Based on the renormalization parameters and the mass enhancement factor  $1/(1+\lambda)$ , one can overestimate the true electron phonon microscopic coupling even by a factor of 10.

# Renormalization of Polaronic Quasiparticles



Instead of extracting directly  $\lambda$ , one can estimate real and imaginary part of the self energy through bare-band fitting and Kramers-Kronig analysis.





## Outline Part II

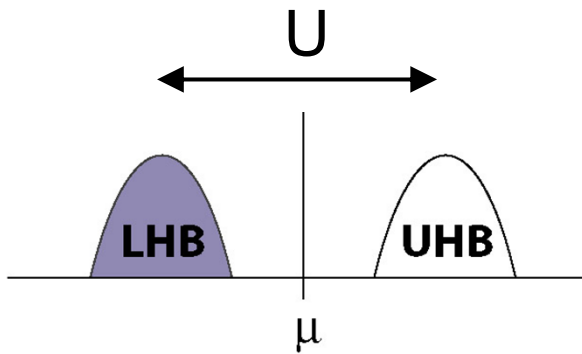
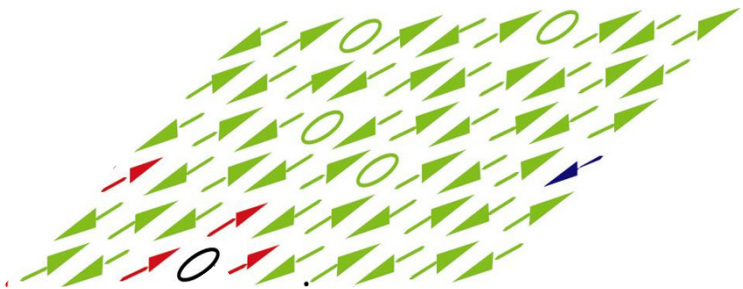
# HTSC: The fate of quasiparticle strength

CUSO Lecture – Lausanne 02/2011



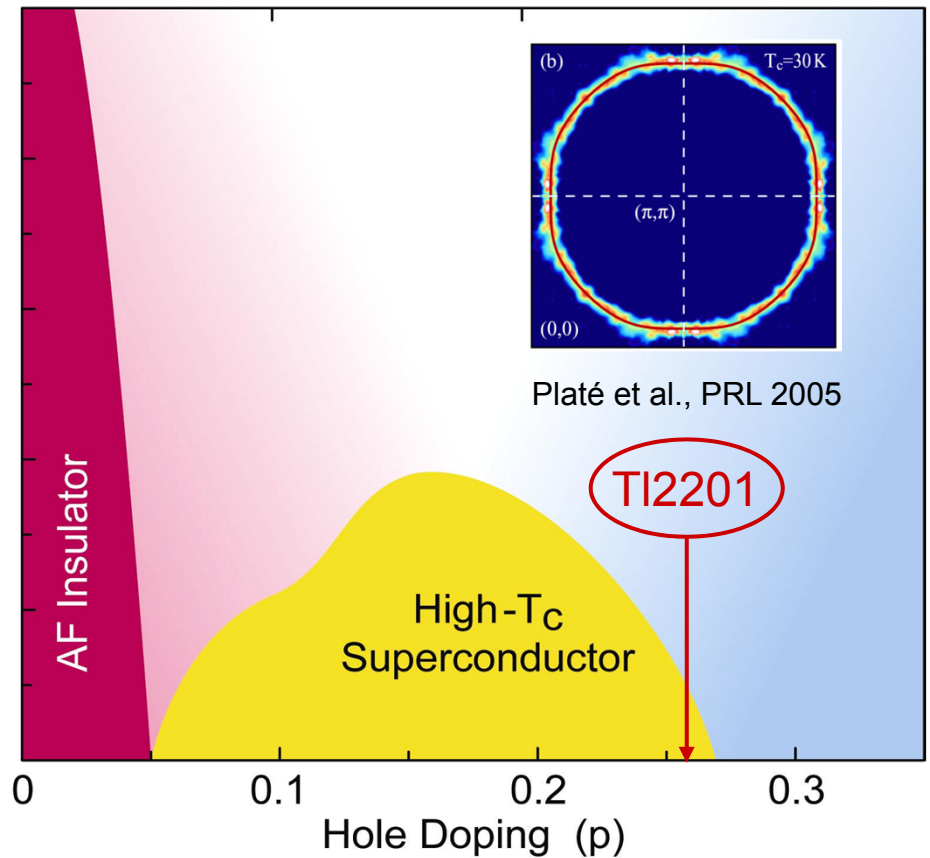
# From Fermi Liquid to Mott Insulator

Correlations suppress  $Z_k$



$$Z \simeq 2p / (p + 1)$$

Sawatzky, Anderson, Randeria,  
Paramekanti, Yang, Rice, et al.

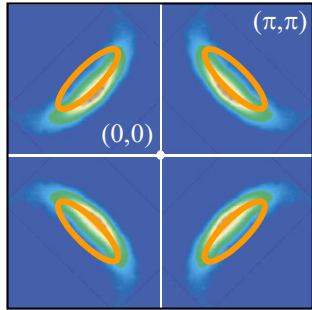


Normal state properties



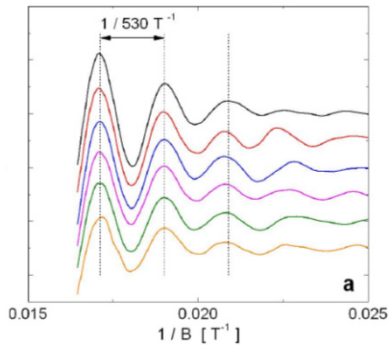
# Fermiology across the Cuprate Phase Diagram

## CCOC - $x=0.12$



ARPES – Shen (05)

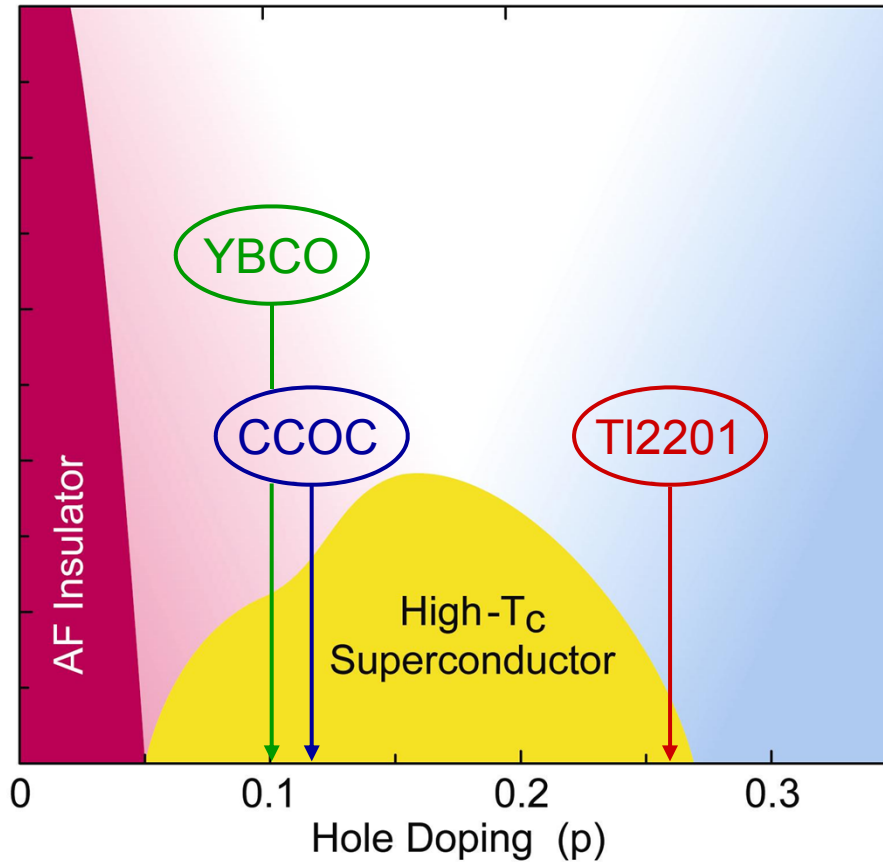
## YBCO - $x=0.10$



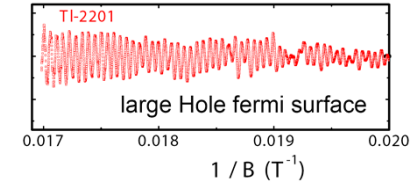
QO – Doiron-Leyraud (07)

## Overdoped TI2201

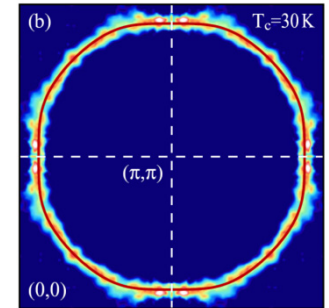
Quantitative agreement between single-particle and transport probes



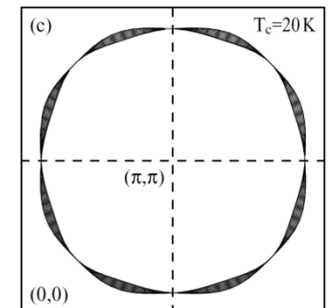
## TI2201 - $x=0.26$



dHvA – Vignolle (08)



ARPES – Platé (05)

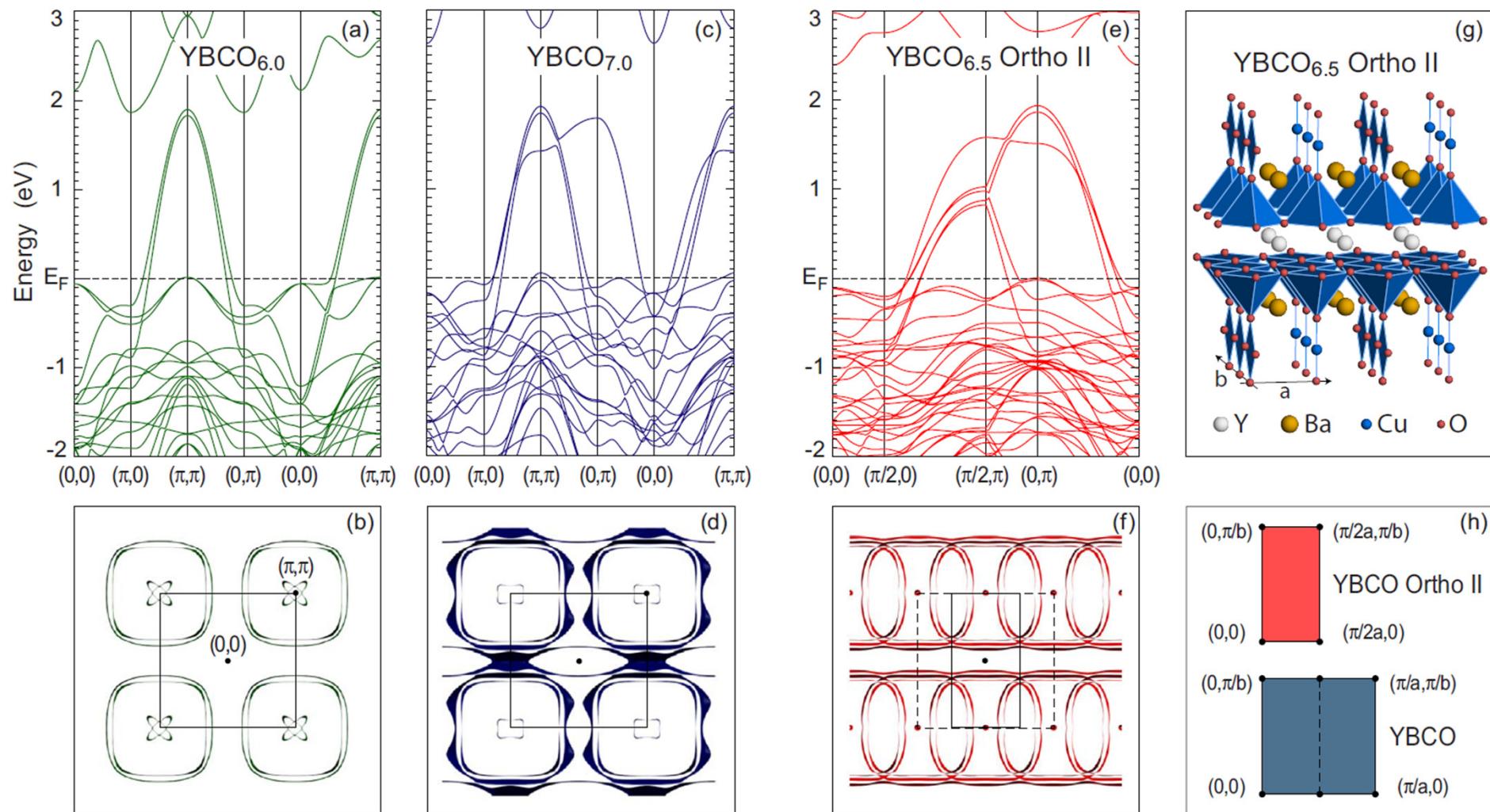


AMRO – Hussey (03)

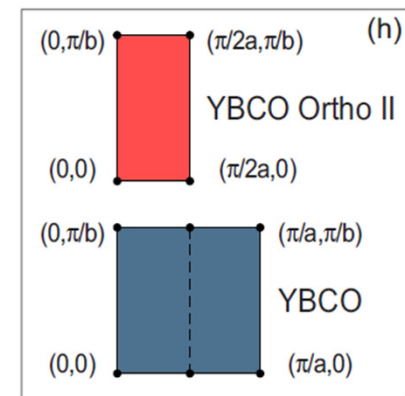
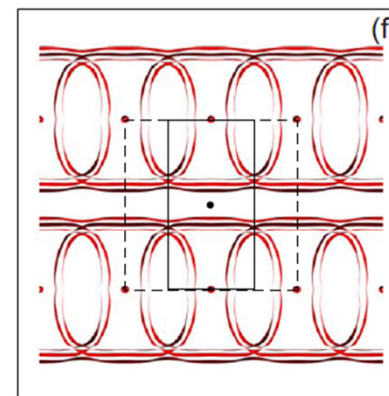
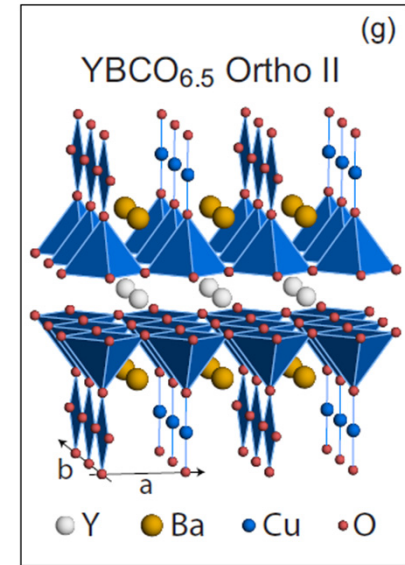
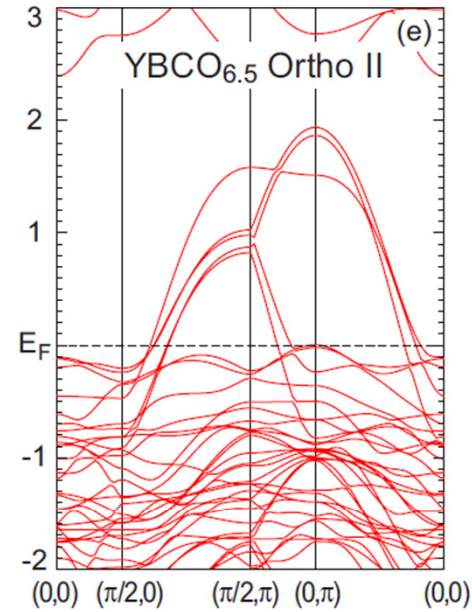
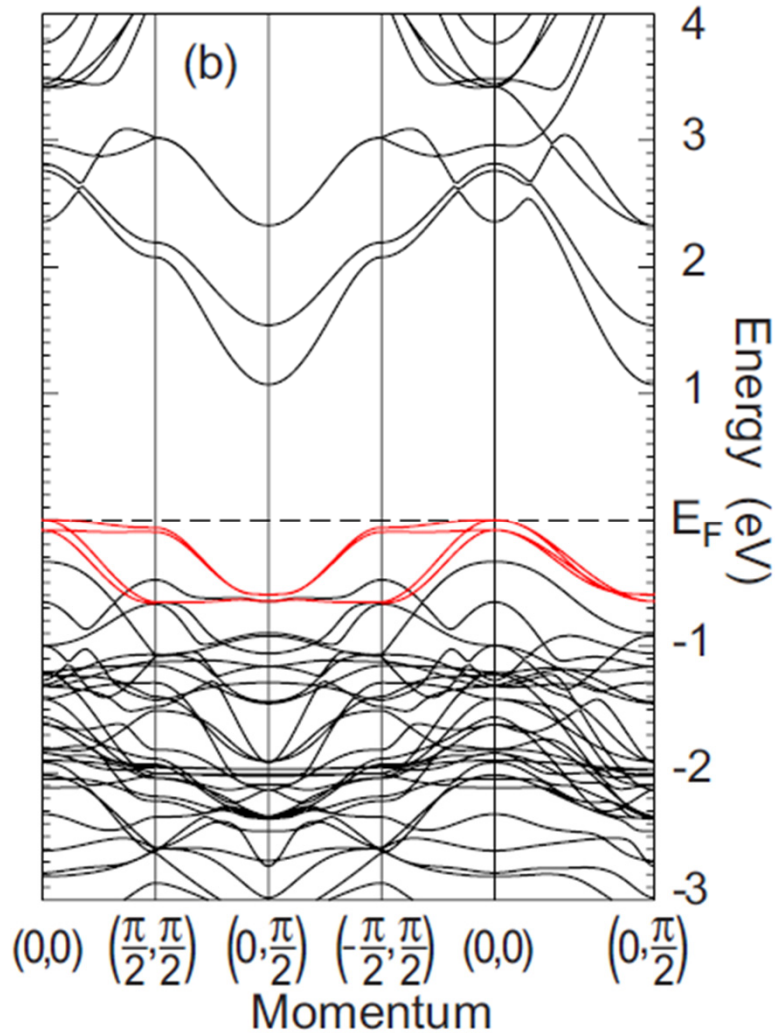
Can this be the gateway to a unified picture for underdoped cuprates?

## ARPES on YBCO6.5

# Electronic Structure of YBCO: Hole Pockets

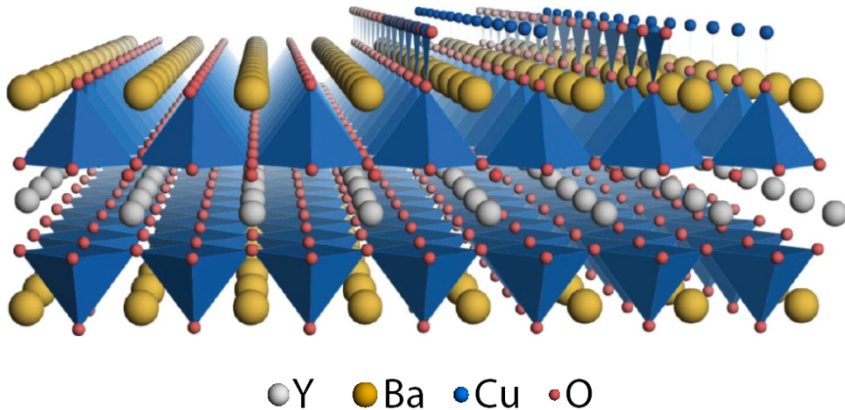


# Electronic Structure of YBCO: Hole Pockets

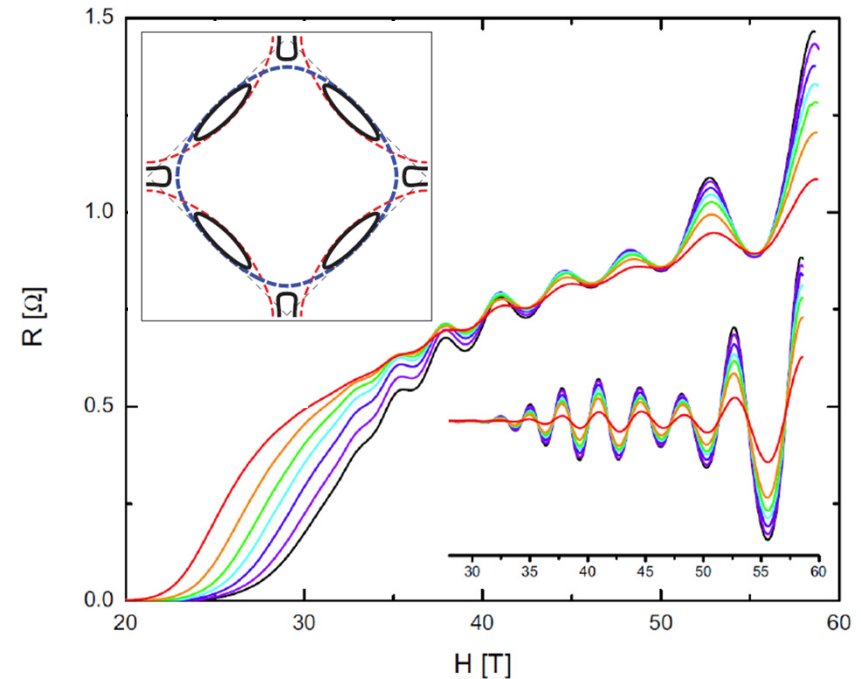
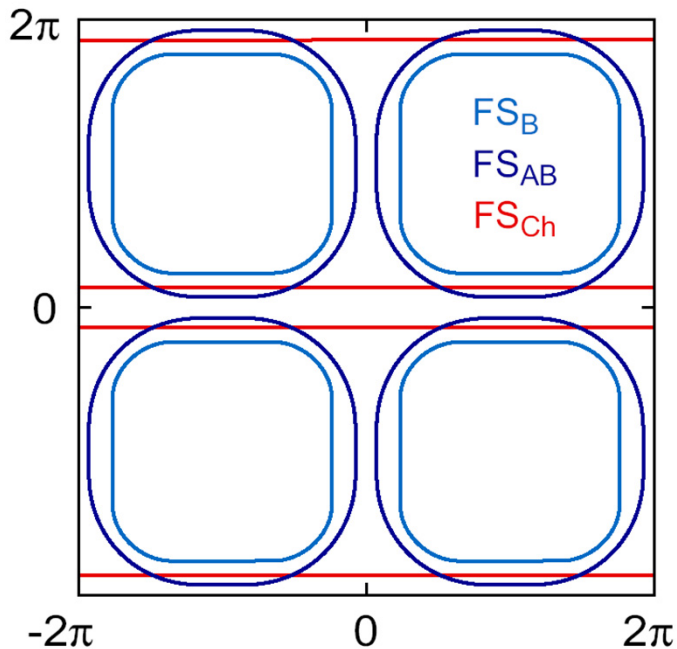




# Fermiology of Underdoped YBCO



Elfimov, Sawatzky, Damascelli PRB **77**, 060504 (2008)



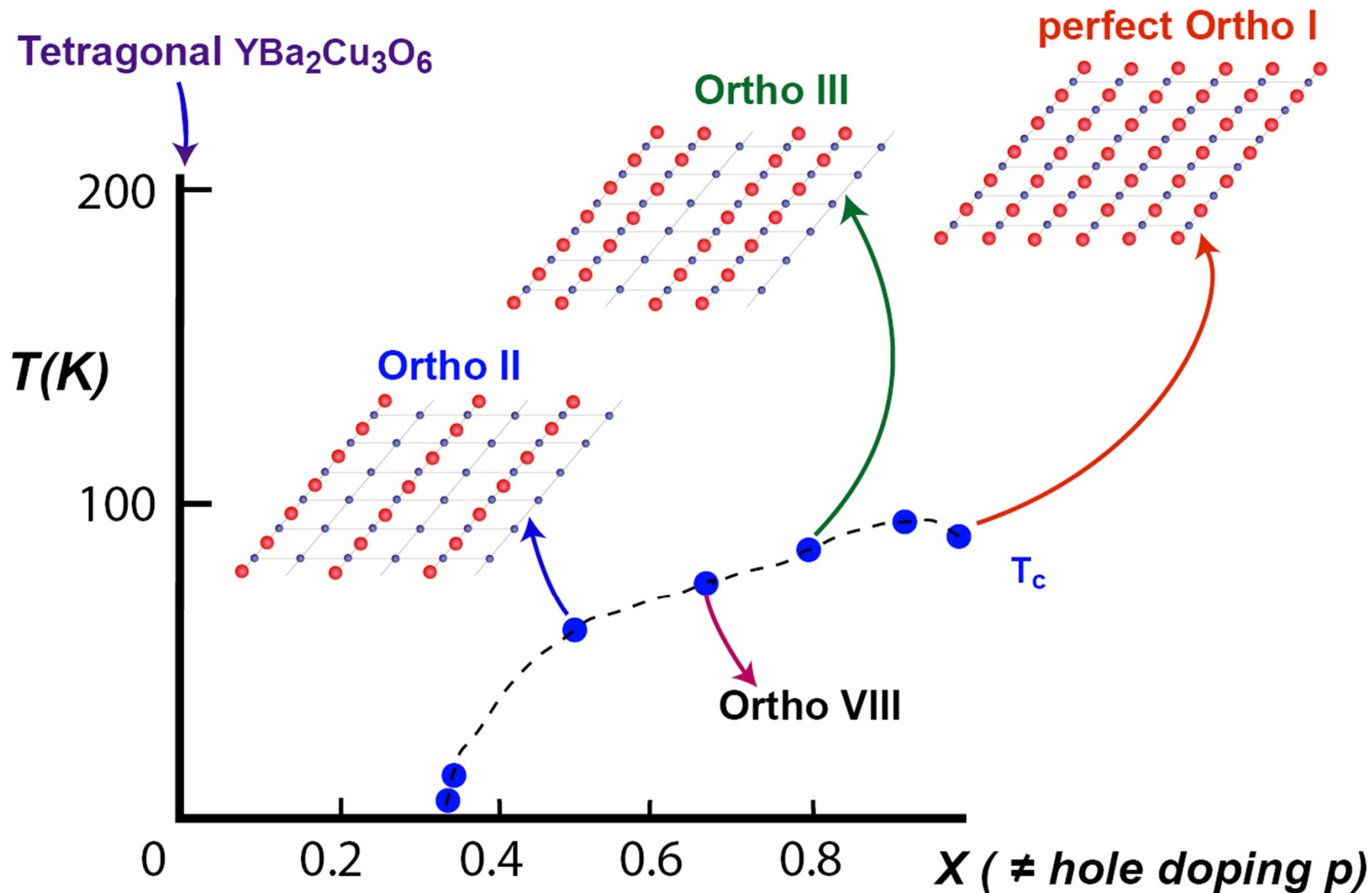
QO suggest Fermi liquid behavior  
in the very underdoped regime

Small pockets are also not in LDA

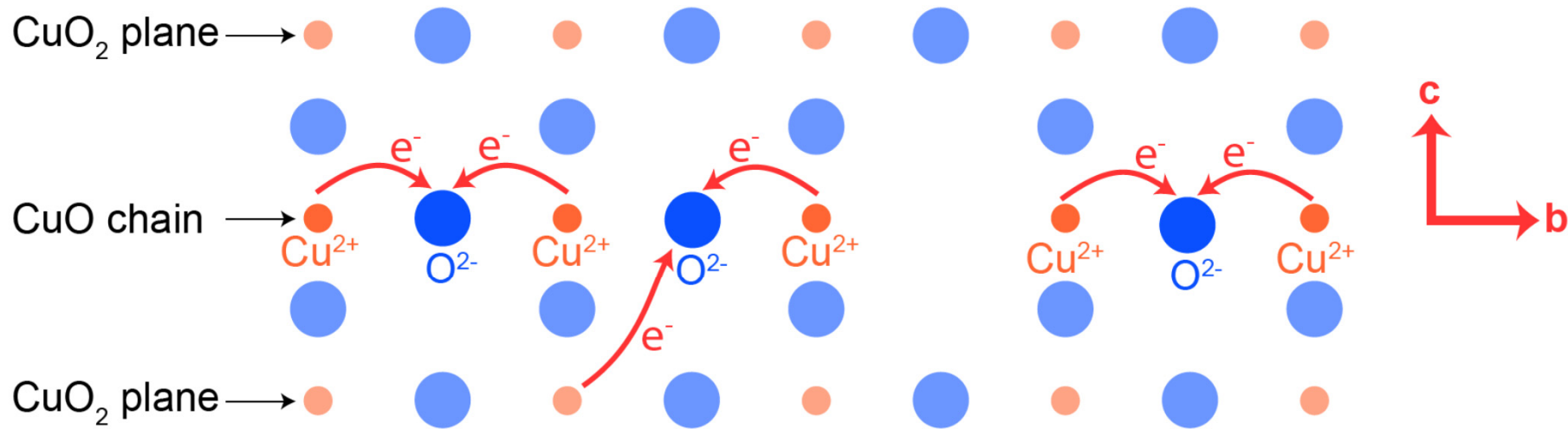
Competing ordering?

B.J. Ramshaw et al., Nature Physics (2010)

# Ordered Phases of CuO Chain Layer in YBCO



# Hole Doping by CuO Chain Oxygen in YBCO



**Chainlets of  $\text{CuO}_x$  are required for doping of holes on the  $\text{CuO}_2$  planes.**

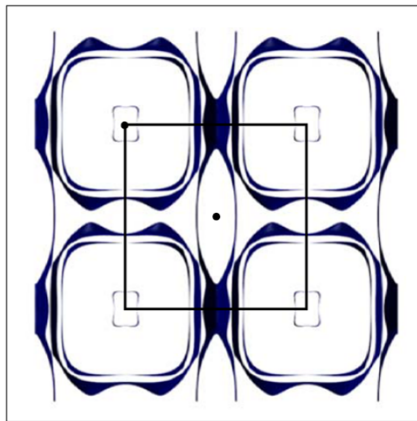
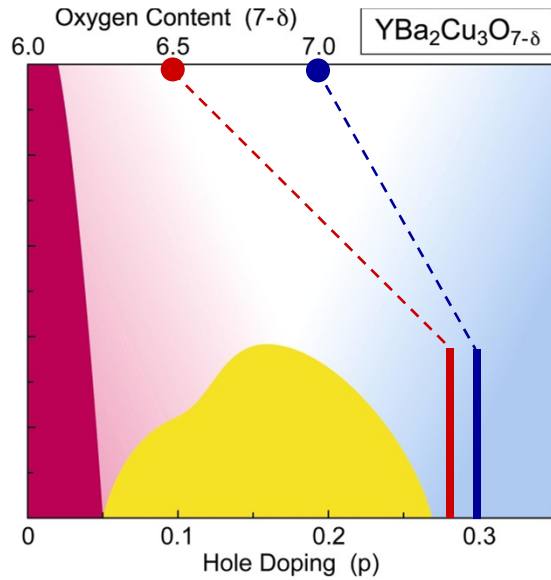
**Problem:** Hole doping  $p$  depends on the average chain length as well as the oxygen content  $x$ .

**Advantage:**  $\text{CuO}_x$  chain oxygen ions are mobile at room temperature and slowly form ordered superstructures.

**Advantage:** At a fixed oxygen content  $x$ , hole doping  $p$  can vary over time.



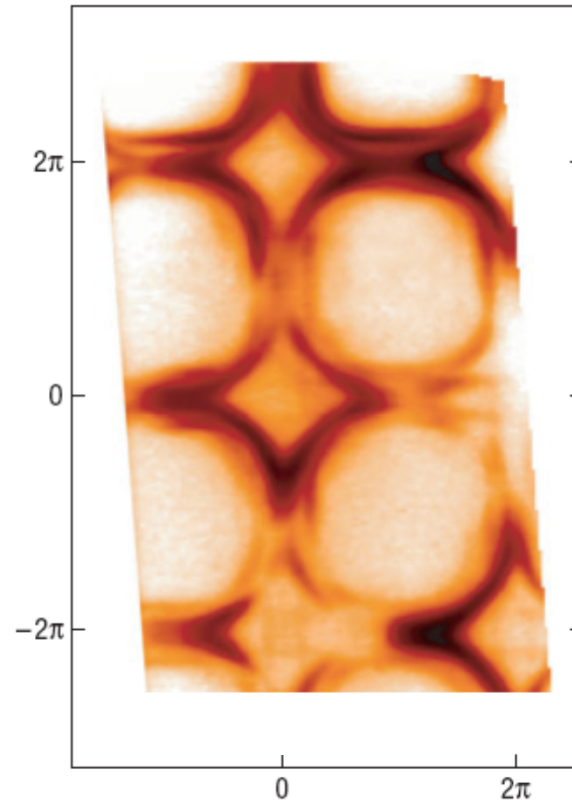
# Fermiology of YBCO by ARPES



Elfimov, Sawatzky, Damascelli  
PRB **77**, 060504 (2008)

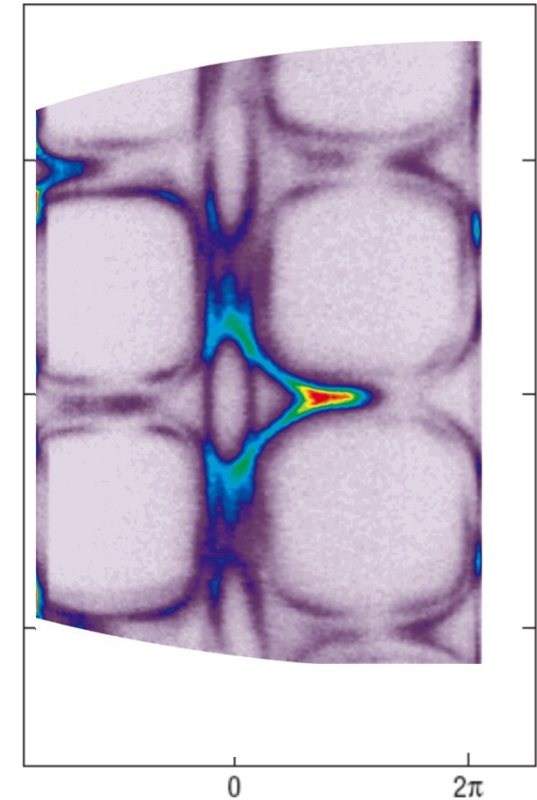
Large doping almost independent of oxygen content

Fermi surface of  
twinned  $\text{YBa}_2\text{Cu}_3\text{O}_{6.51}$



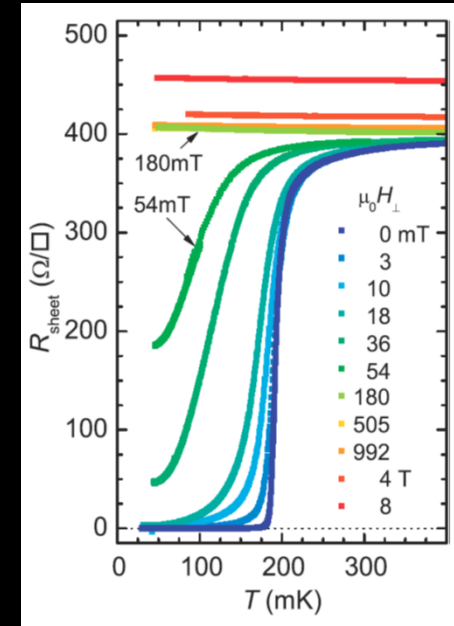
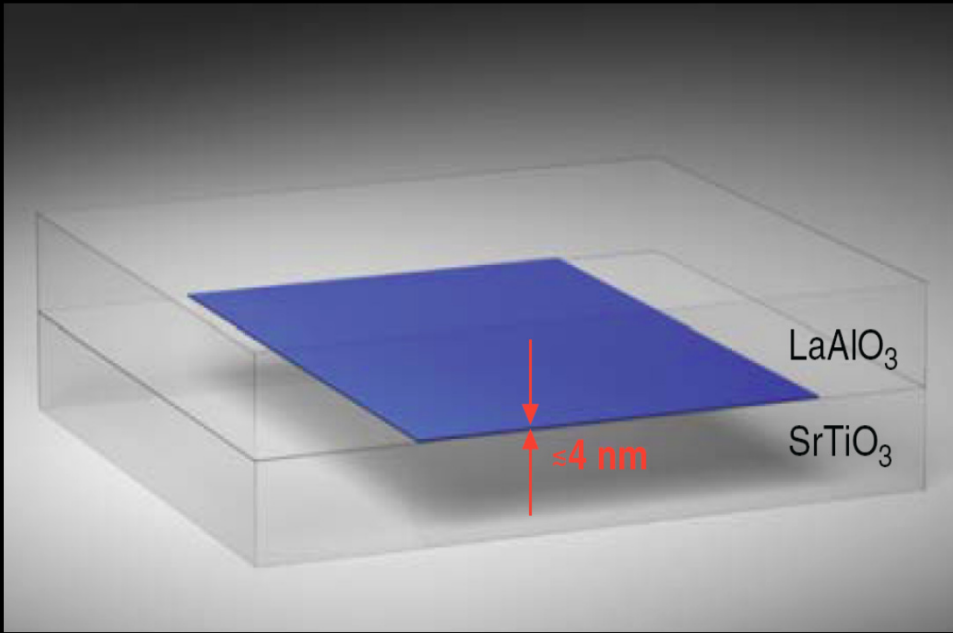
Hossain et al.  
Nature Physics **4**, 527 (2008)

Fermi surface of  
detwinned  $\text{YBa}_2\text{Cu}_3\text{O}_{6.99}$



Fournier et al.  
Nature Physics **6**, 905 (2010)

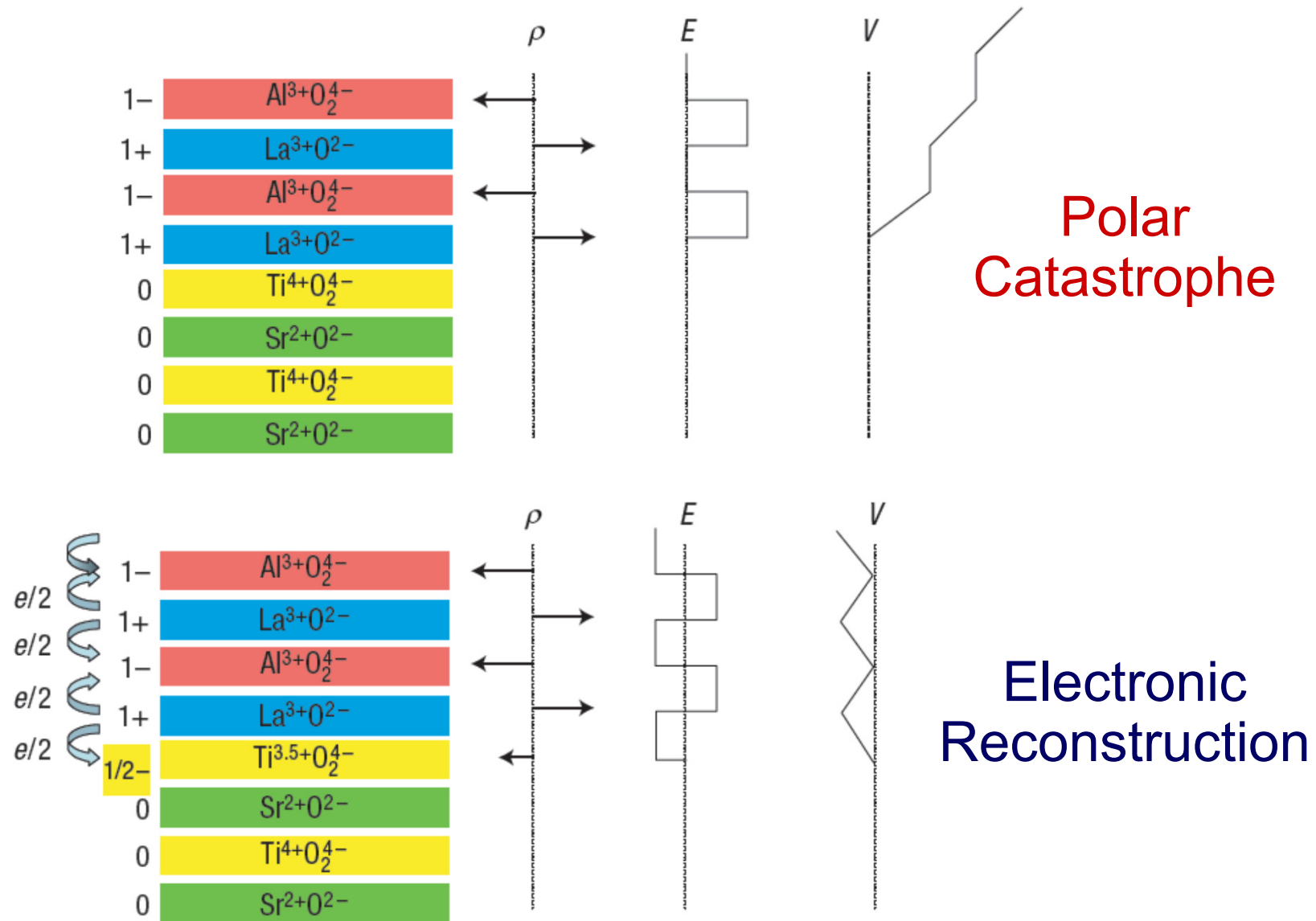
# Whither Oxide Electronics?



Carrier mobility  $10^4 \text{ cm}^2/(\text{Vs})$

2DEG, superconductivity, magnetism, orbital ordering, etc.

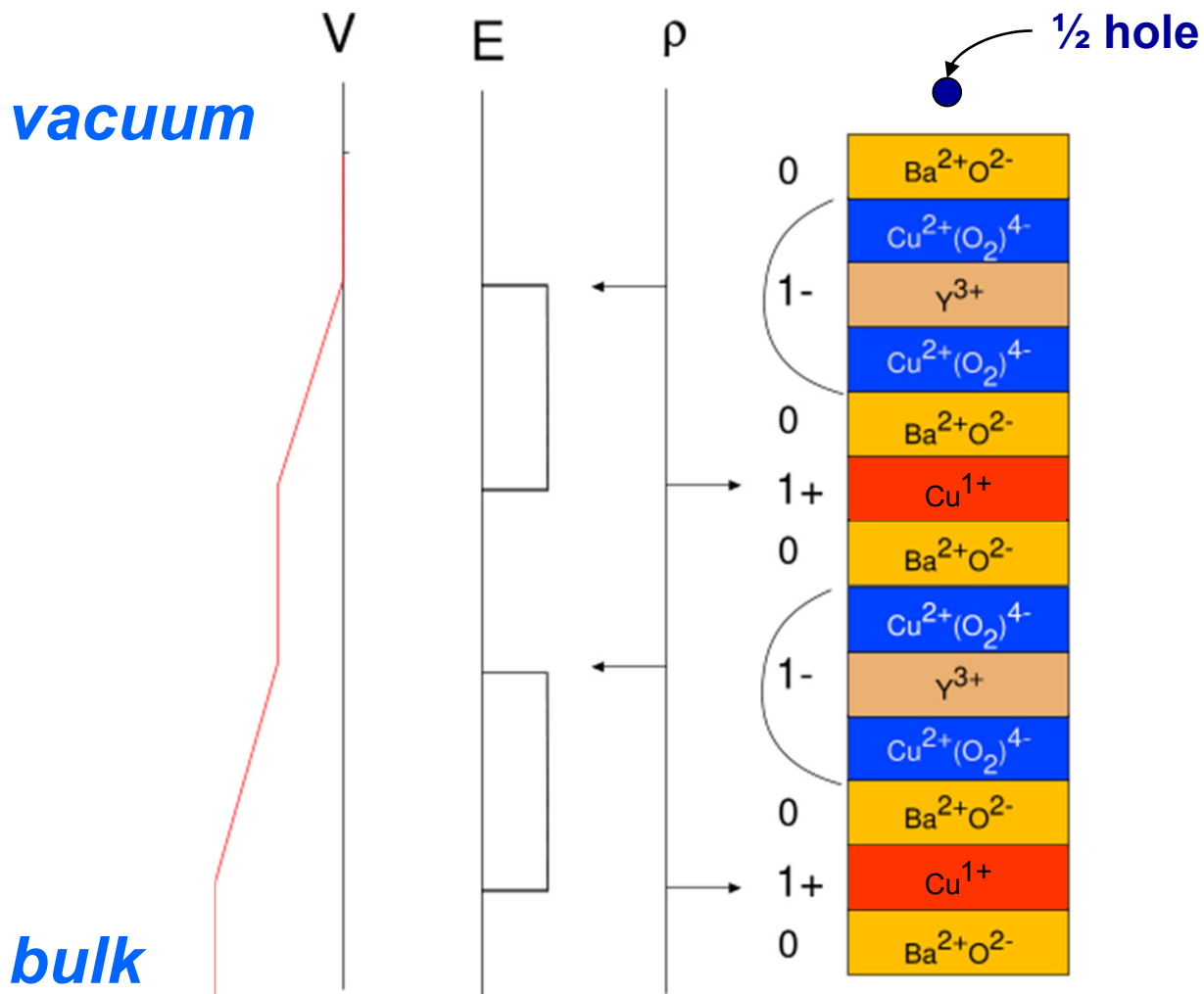
# Electronic Reconstruction at the Interface



# Electronic Surface Reconstruction in $\text{YBa}_2\text{Cu}_3\text{O}_{6.0}$

Polar catastrophe

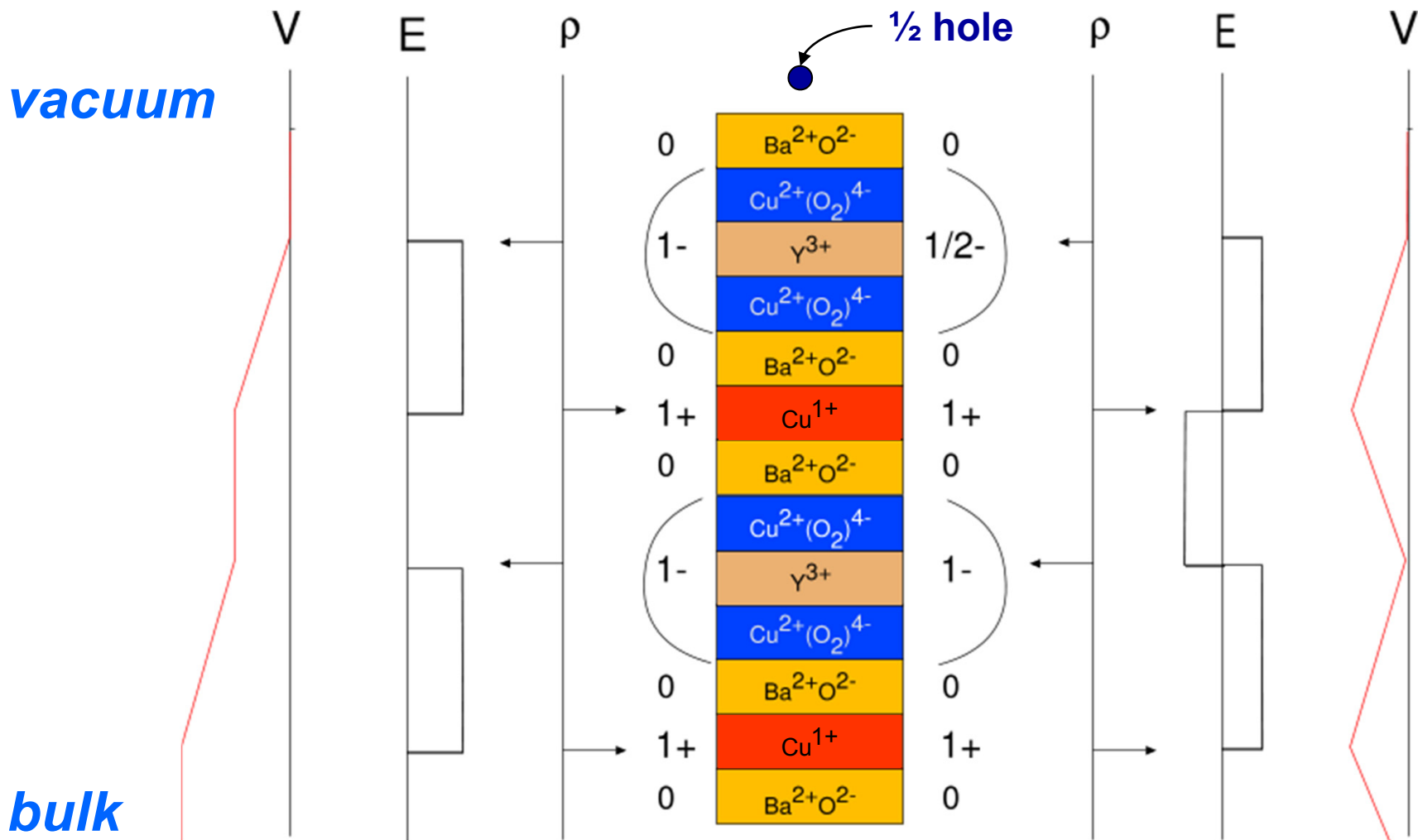
Self-doping of YBCO surface



# Electronic Surface Reconstruction in $\text{YBa}_2\text{Cu}_3\text{O}_{6.0}$

Polar catastrophe

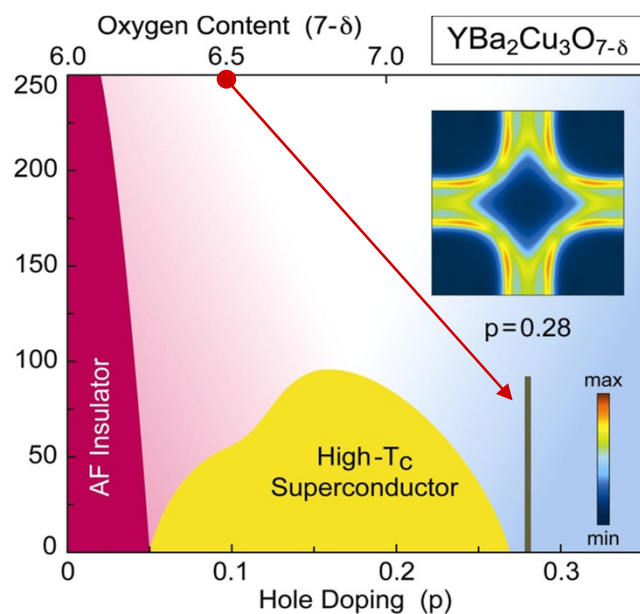
Self-doping of YBCO surface



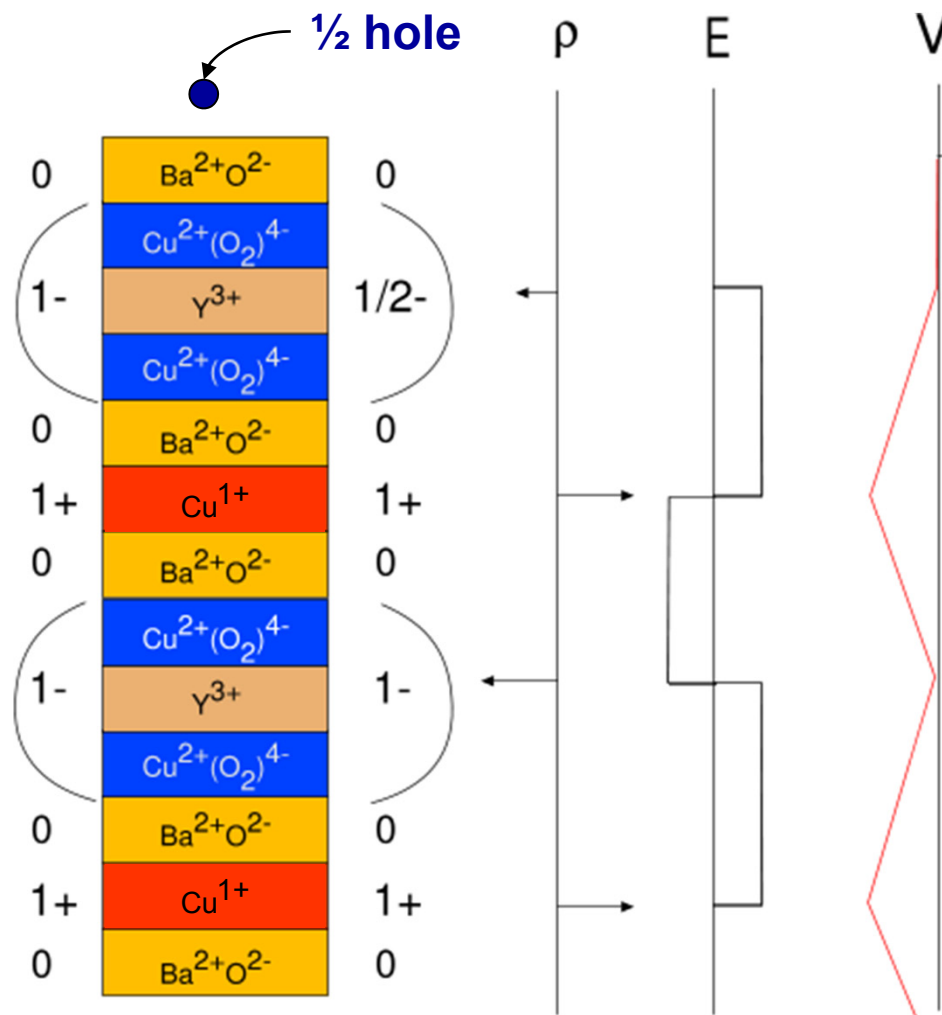
# Electronic Surface Reconstruction in $\text{YBa}_2\text{Cu}_3\text{O}_{6.0}$

## Self-doping of YBCO surface

Self-doping

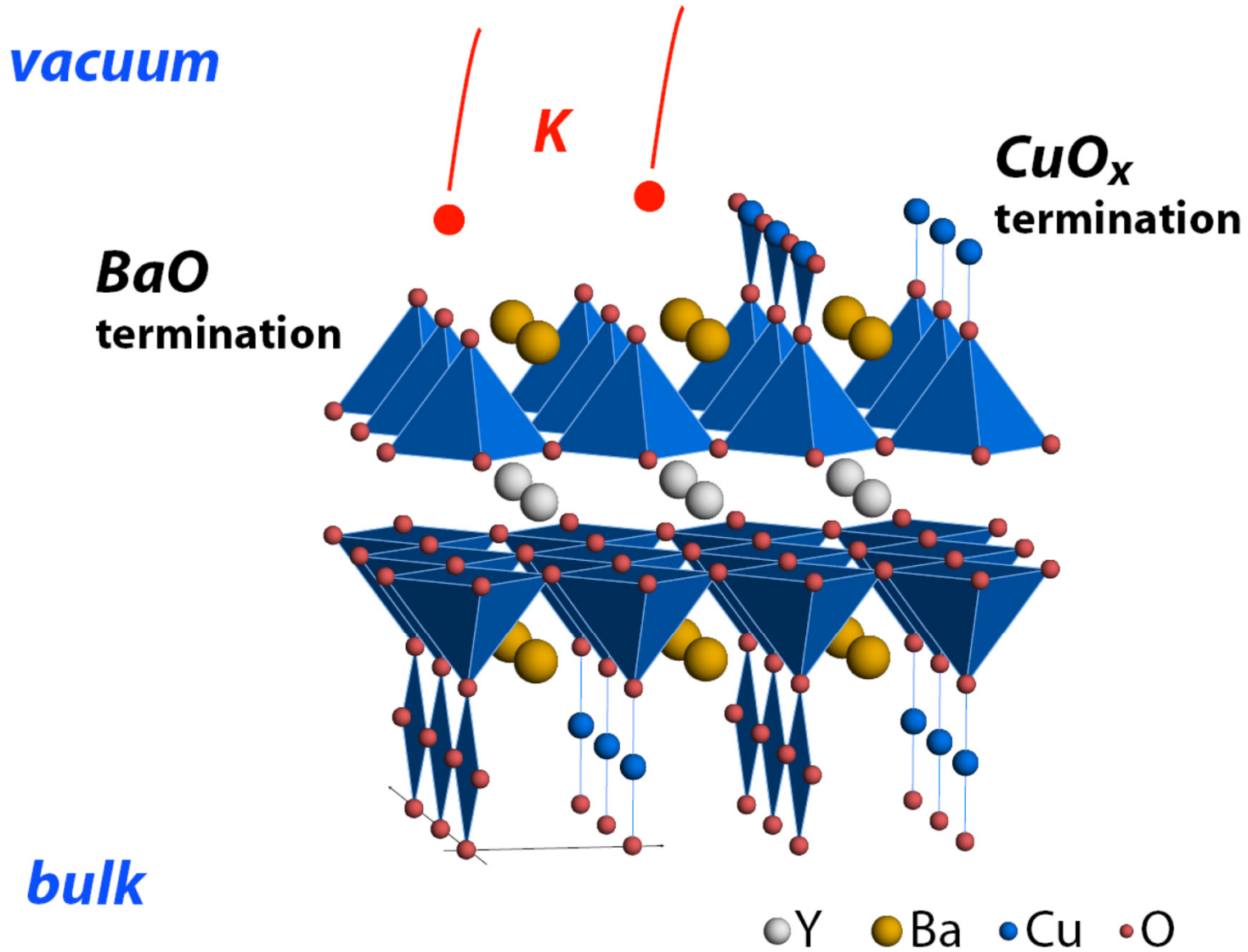


Overdoping

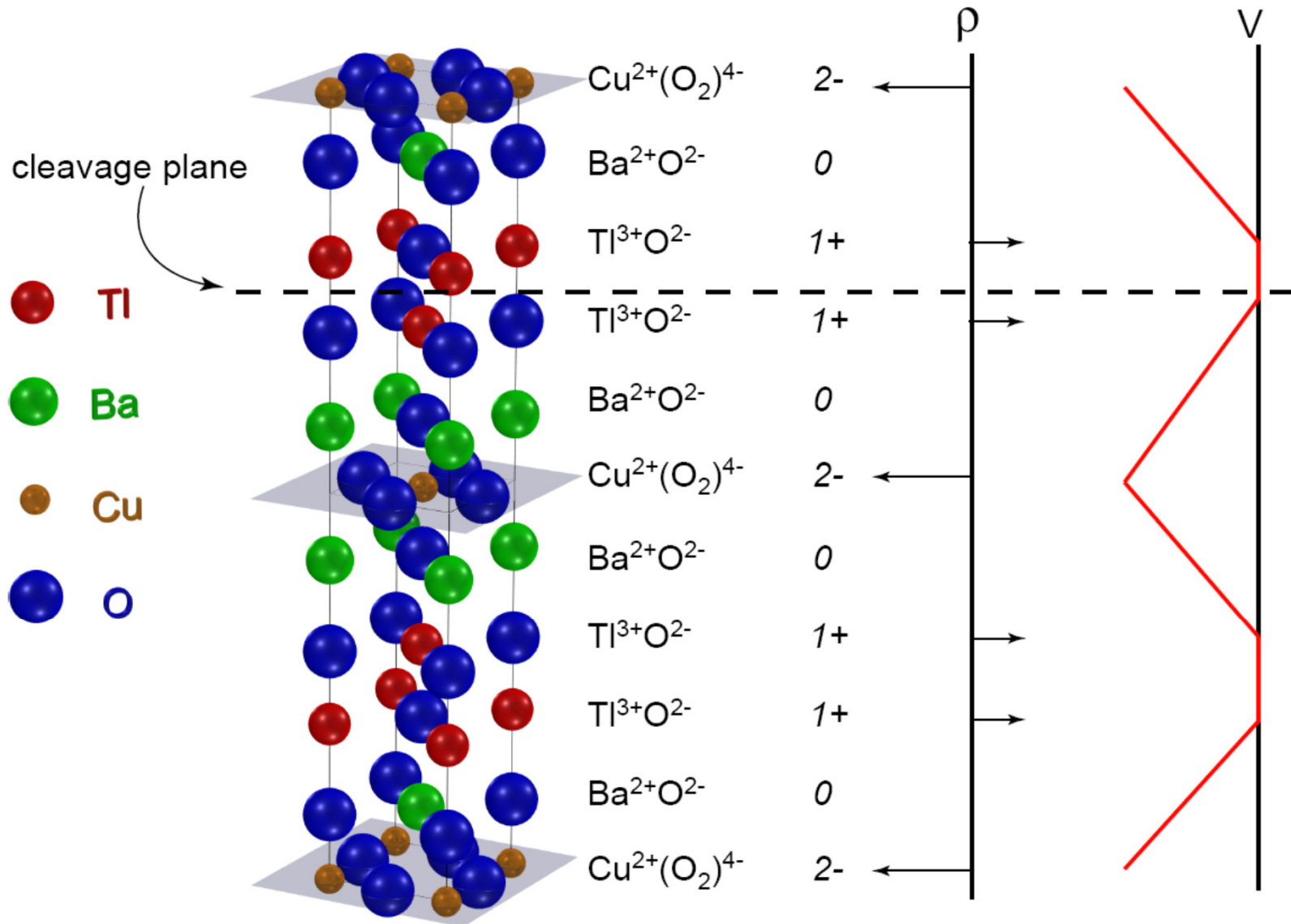




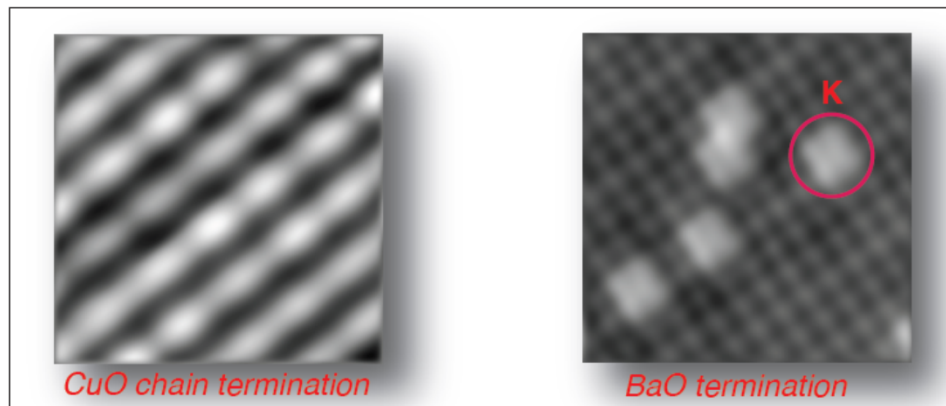
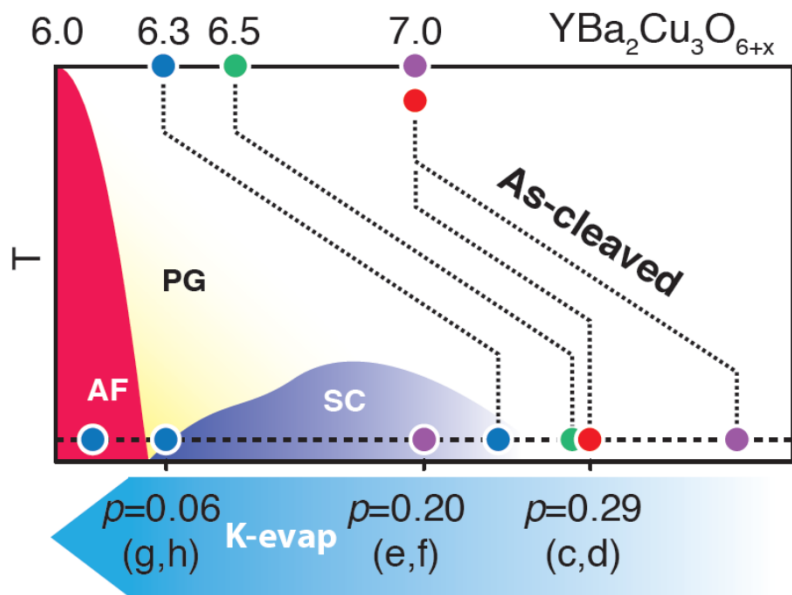
# Fixing the YBCO surface self-doping by K deposition



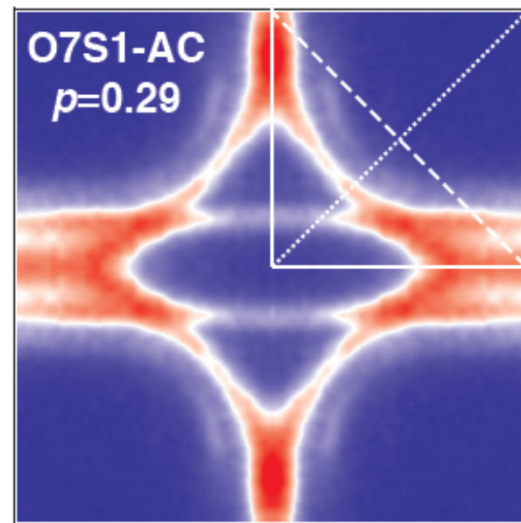
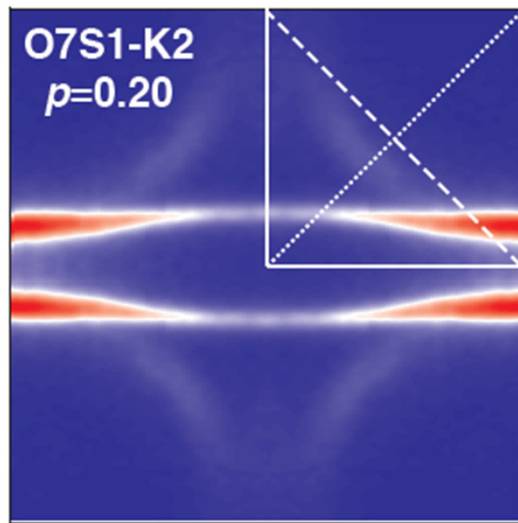
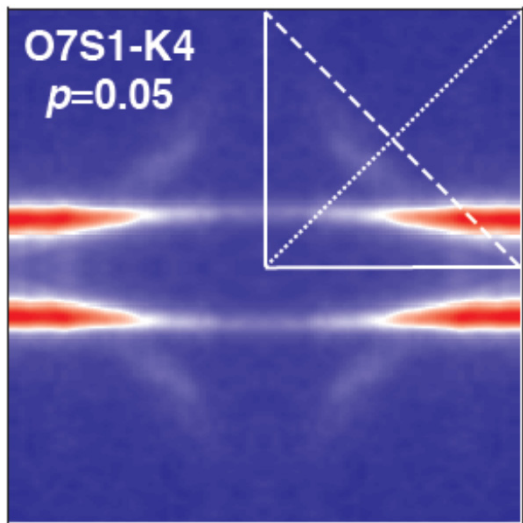
# Is the Surface of $Tl_{2-y}Ba_2Cu_{1+y}O_{6+x}$ polar? NO!!



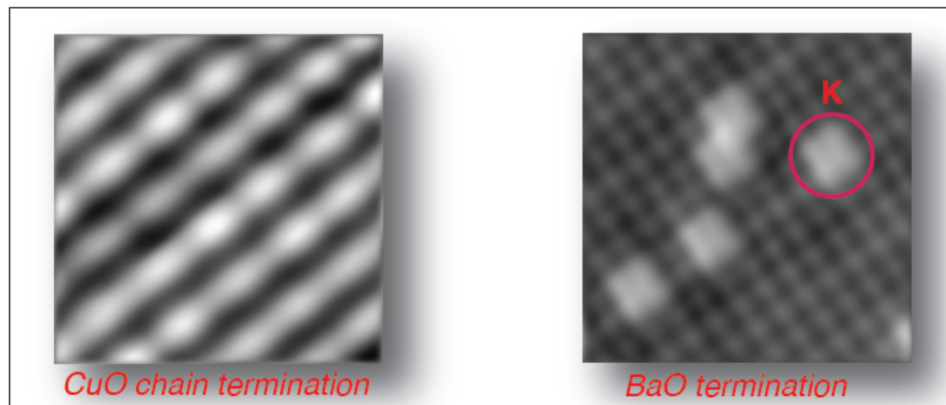
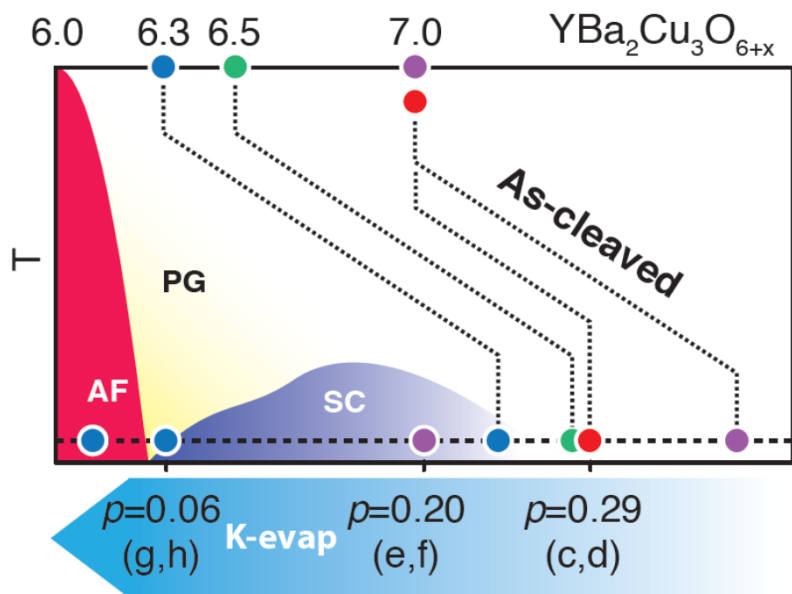
# ARPES on K-deposited YBCO: counting carriers



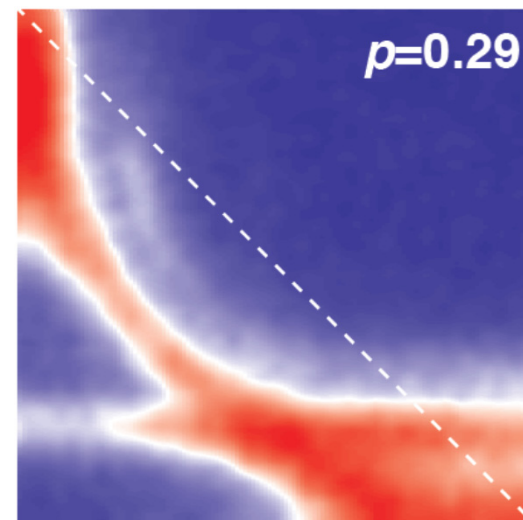
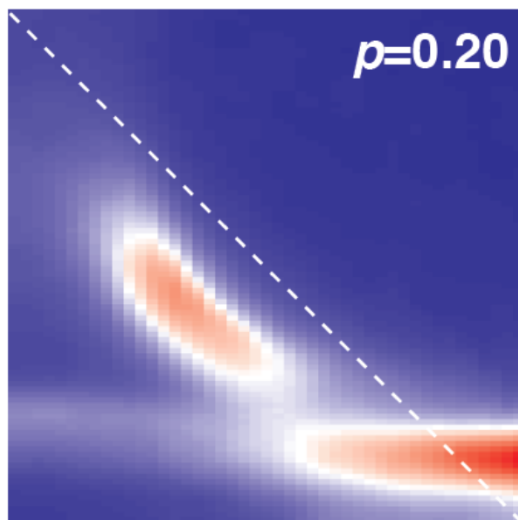
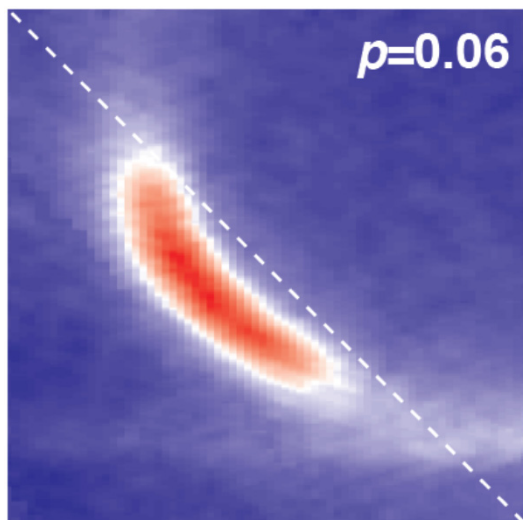
D. Fournier, Nature Physics **6**, 905 (2010)



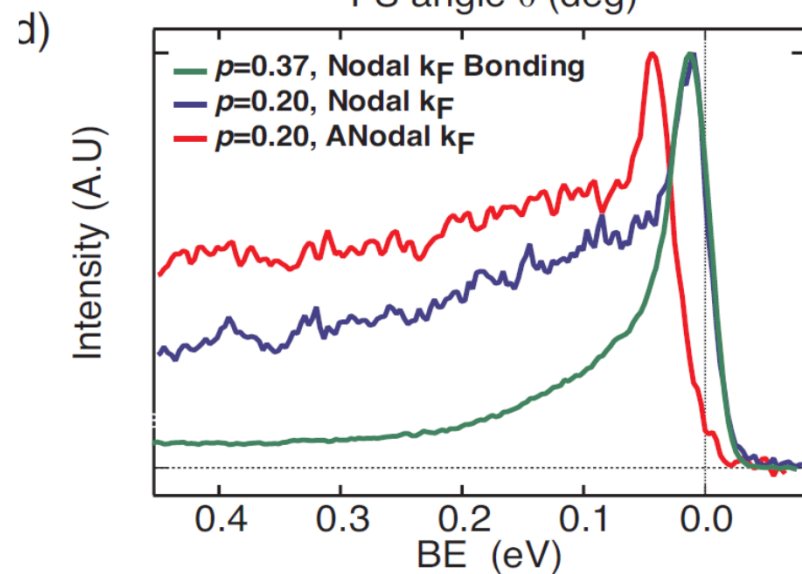
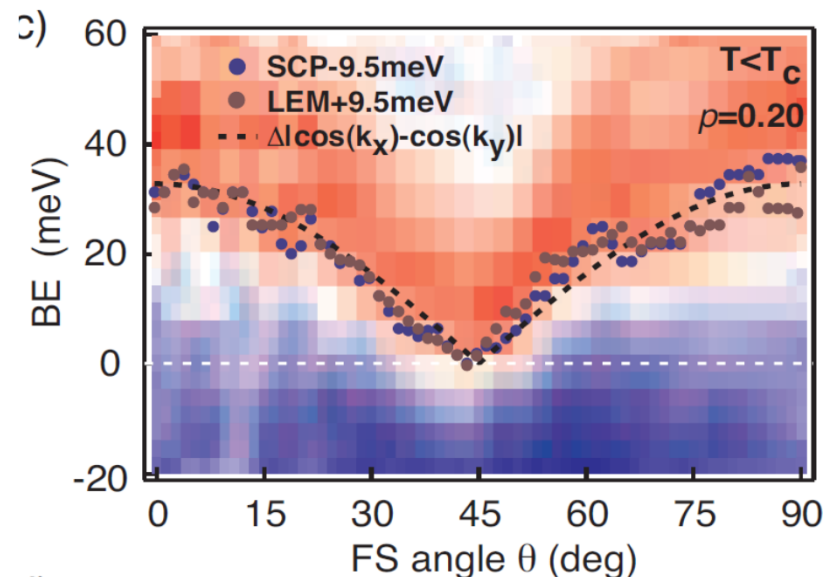
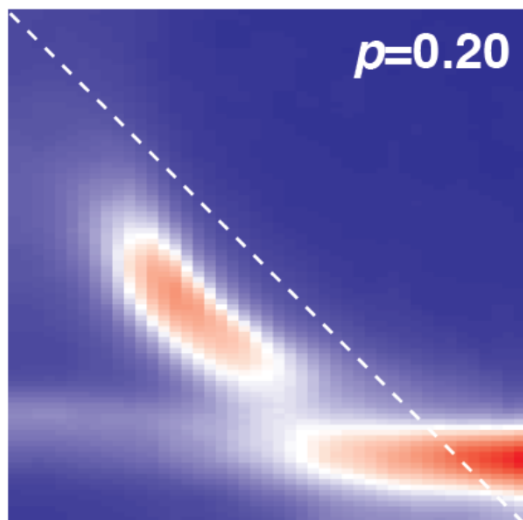
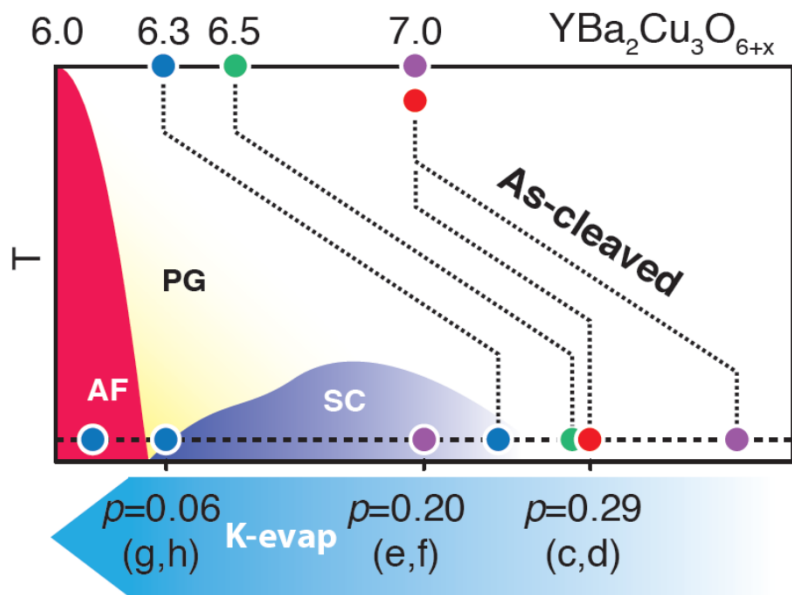
# ARPES on K-deposited YBCO: arcs vs. pockets



Fournier et al., Nature Physics **6**, 905 (2010)

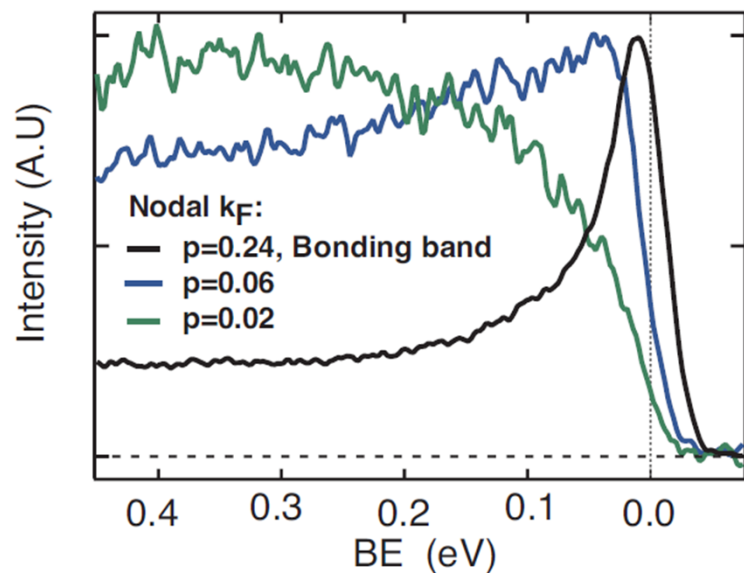
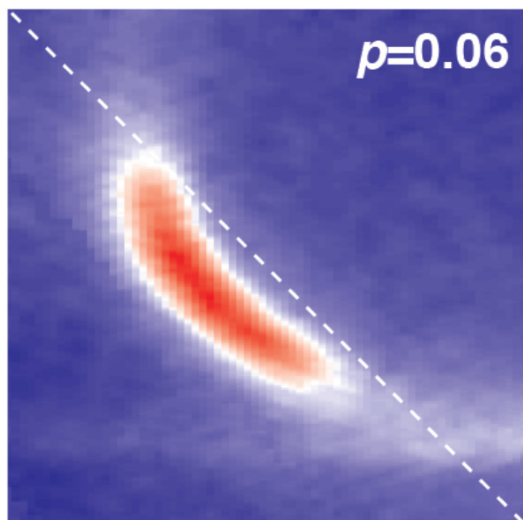
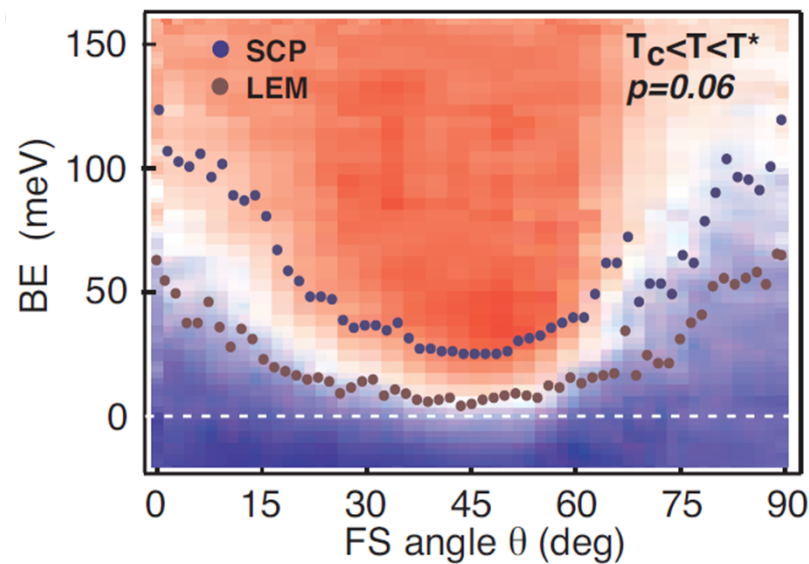
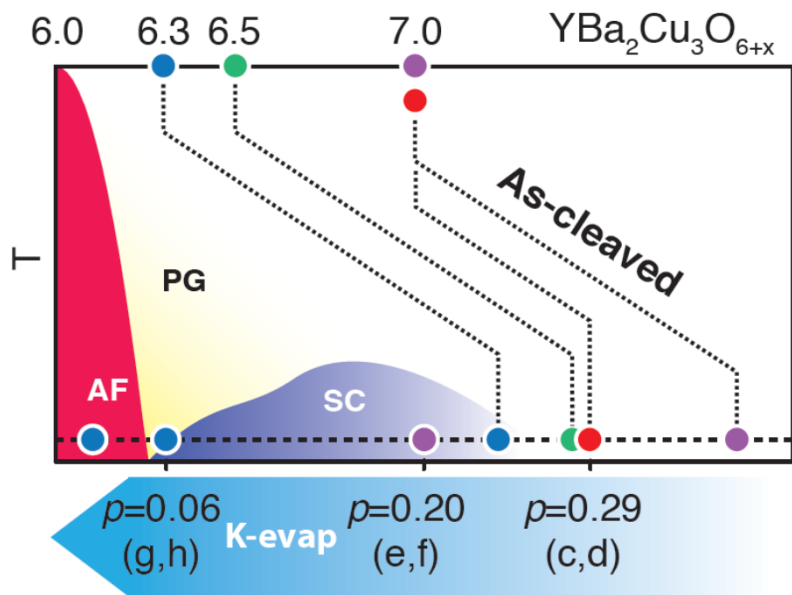


# ARPES on K-deposited YBCO: SP and pseudogap



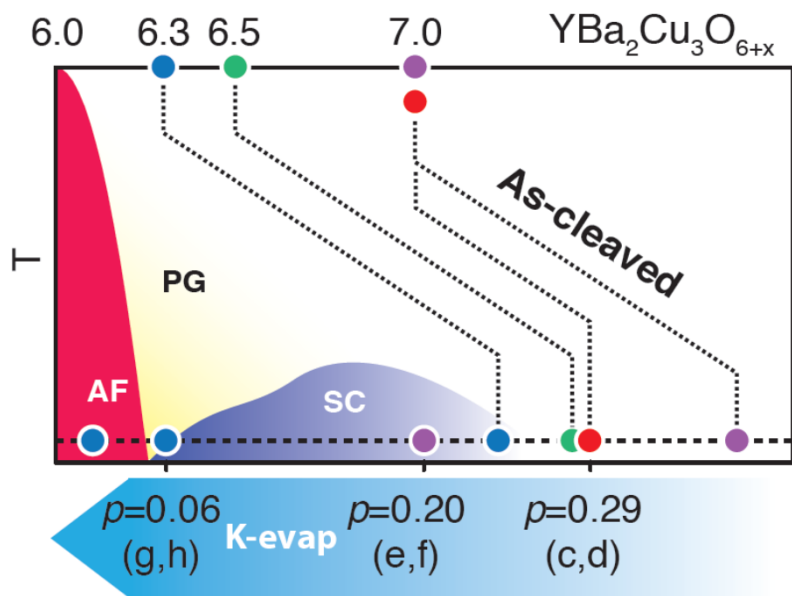


# ARPES on K-deposited YBCO: SP and pseudogap



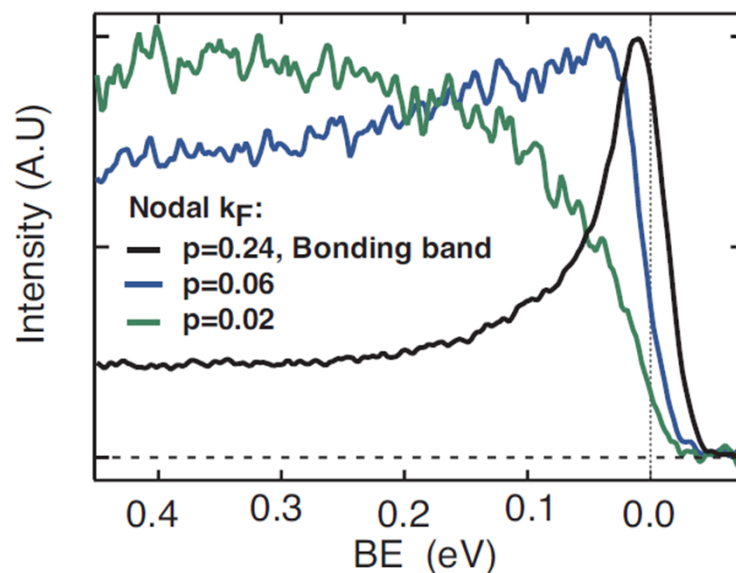
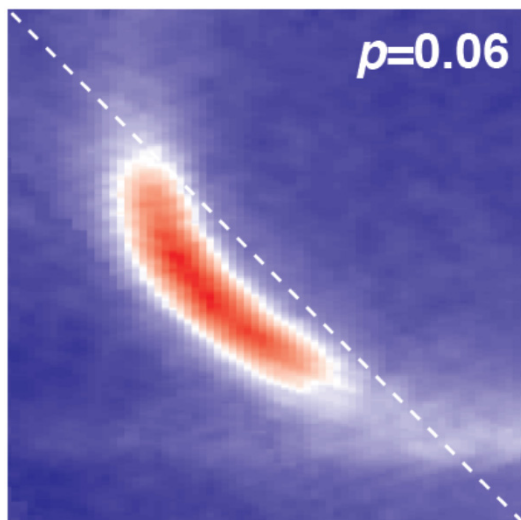


# ARPES on K-deposited YBCO: SP and pseudogap



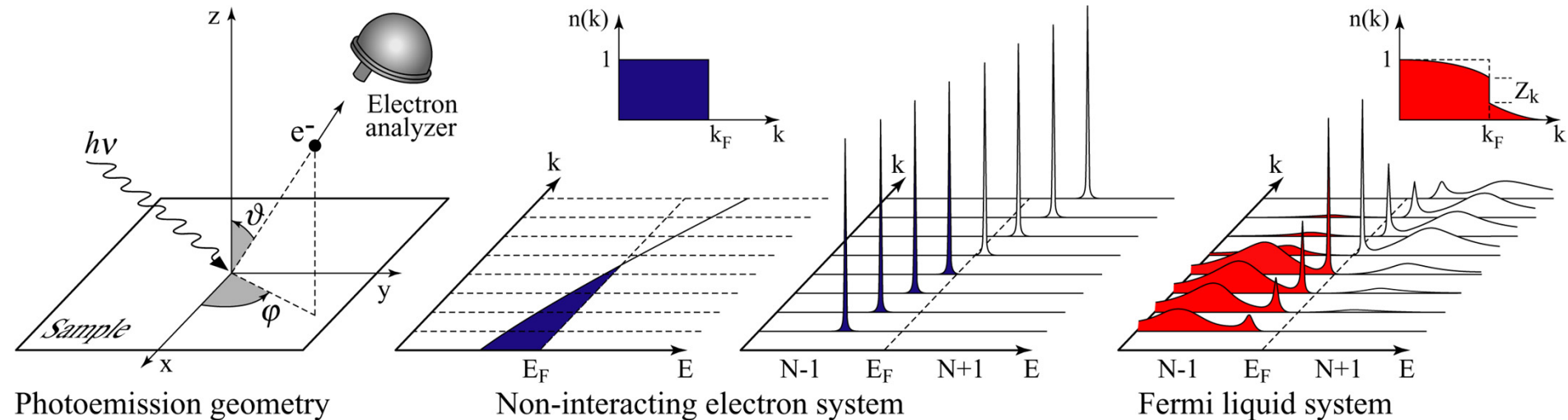
K doping provides access to the whole phase diagram (FS, dispersion, SC gap)

The FS collapses in 4 disconnected arcs  
NO evidence for pockets in ARPES !!



# ARPES: The One-Particle Spectral Function

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



Photoemission intensity:  $I(k, \omega) = I_0 |M(k, \omega)|^2 f(\omega) A(k, \omega)$

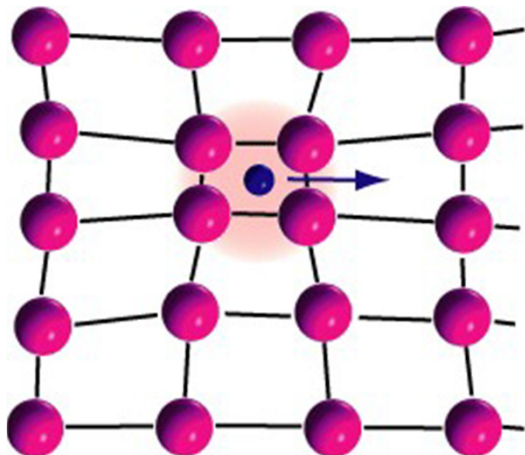
**Single-particle spectral function**

$$A(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\mathbf{k}, \omega)}{[\omega - \epsilon_{\mathbf{k}} - \Sigma'(\mathbf{k}, \omega)]^2 + [\Sigma''(\mathbf{k}, \omega)]^2}$$

$\Sigma(\mathbf{k}, \omega)$ : the “self-energy” captures the effects of interactions

# Renormalization of Polaronic Quasiparticles

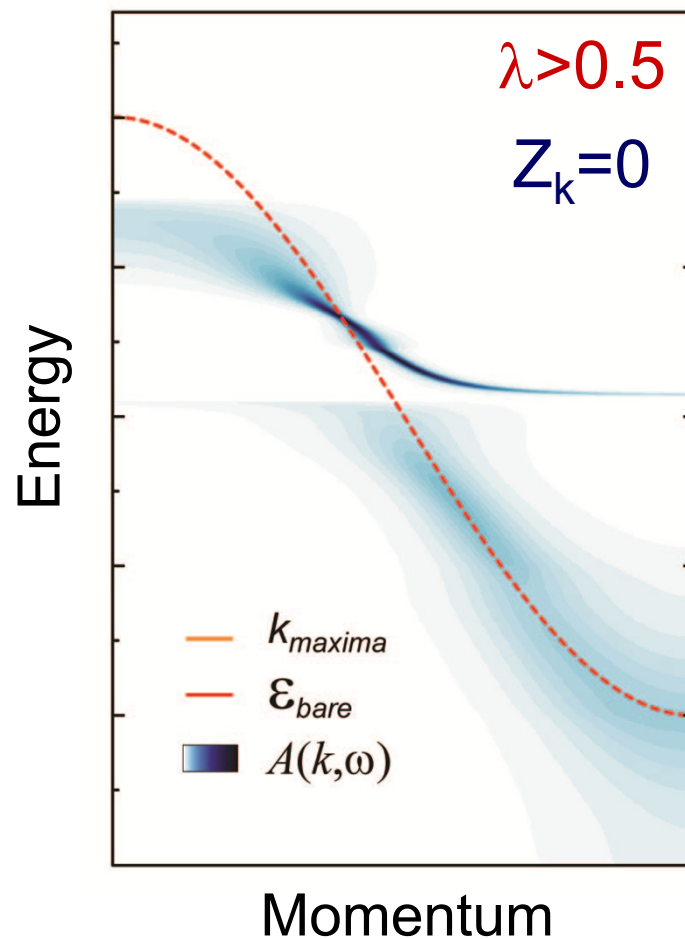
$$\mathcal{H} = \sum_k \varepsilon_k^b c_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$



$$A(\mathbf{k}, \omega) = Z_{\mathbf{k}} \frac{\Gamma_{\mathbf{k}}/\pi}{(\omega - \varepsilon_{\mathbf{k}})^2 + \Gamma_{\mathbf{k}}^2} + A_{inc}$$

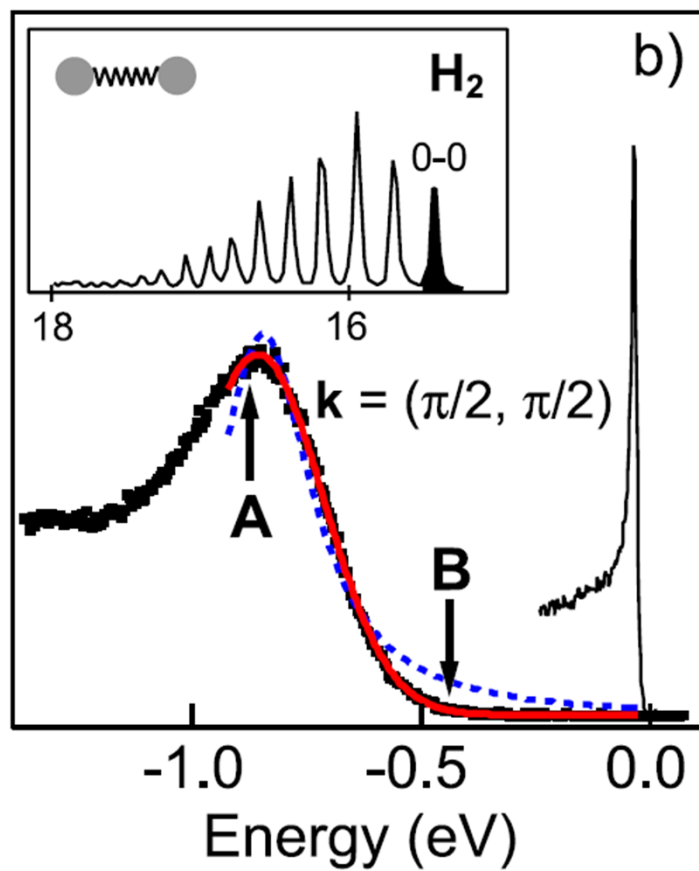
$$m^* > m \quad |\varepsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$

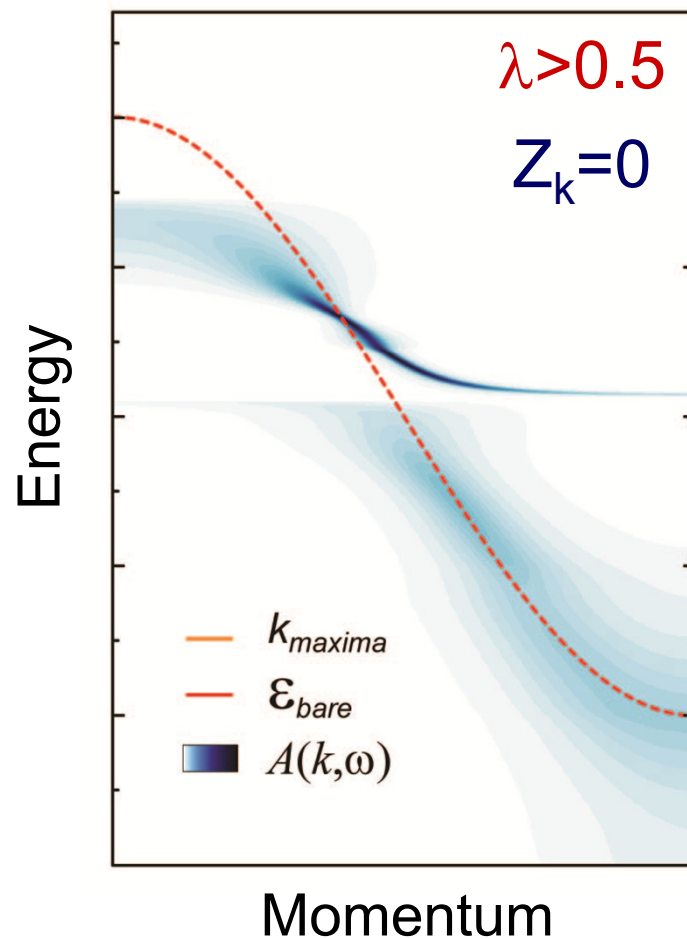


# Renormalization of Polaronic Quasiparticles

$$\mathcal{H} = \sum_k \varepsilon_k b_k^\dagger c_k + \Omega \sum_Q b_Q^\dagger b_Q + \frac{g}{\sqrt{N}} \sum_{k,Q} c_{k-Q}^\dagger c_k (b_Q^\dagger + b_{-Q})$$

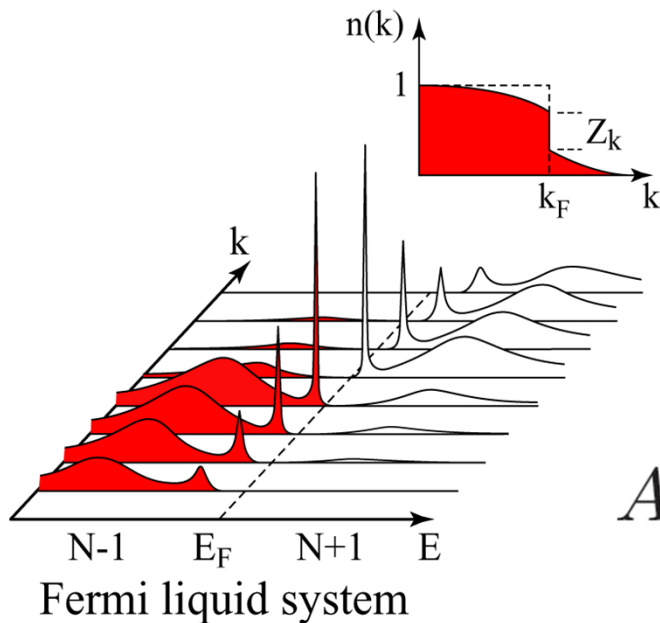


K.M. Shen et al., PRL **93**, 267002 (2004)



Veenstra, Goodvin, Berci, Damascelli, PRB **82**, 012504 (2010)

# Quasiparticle Coherence across the Phase Diagram



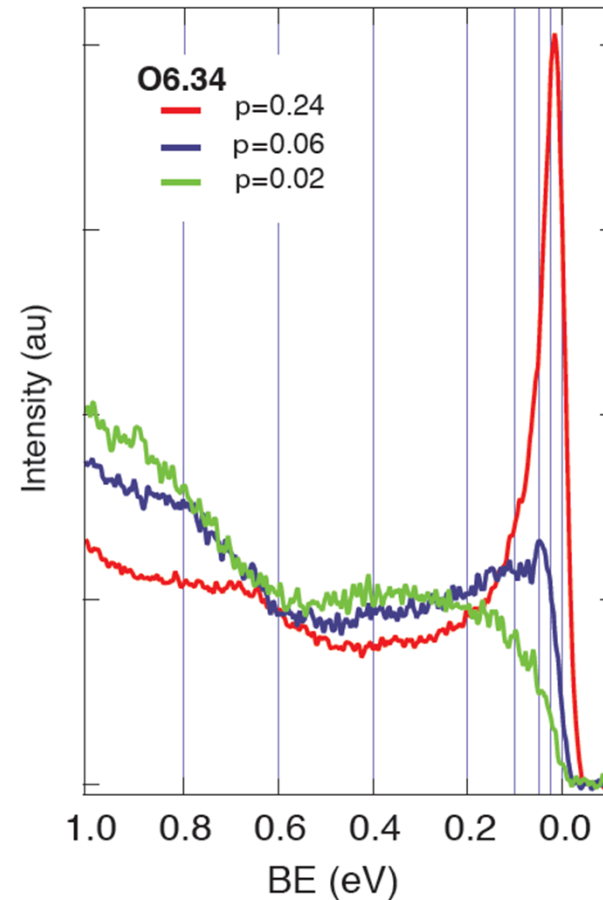
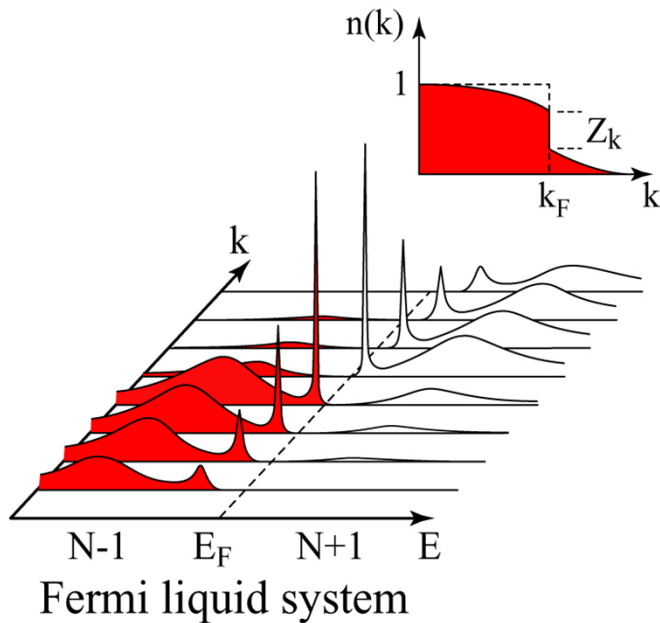
$$Z_k = \int A_{coh}(k, \omega) d\omega$$

$$I(k, \omega) = I_0(k) f(\omega) A(k, \omega)$$

$$A(k, \omega) \equiv A_{coh}(k, \omega) + A_{incoh}(k, \omega)$$

$$Z_k = \int I_{coh}(k, \omega) d\omega / \int I(k, \omega) d\omega$$

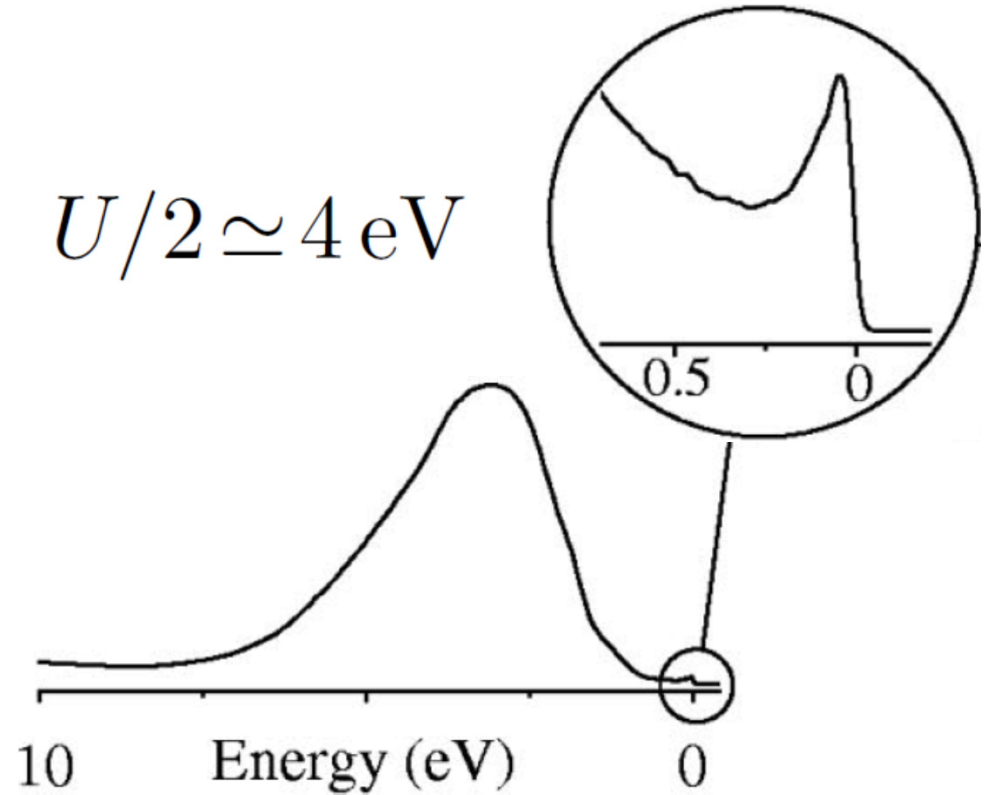
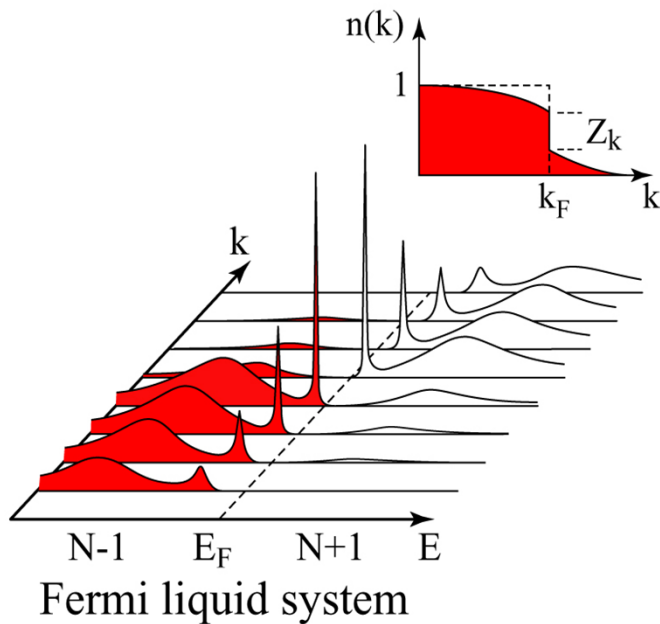
# Quasiparticle Coherence across the Phase Diagram



$$Z_k = \int I_{coh}(k, \omega) d\omega / \int I(k, \omega) d\omega$$

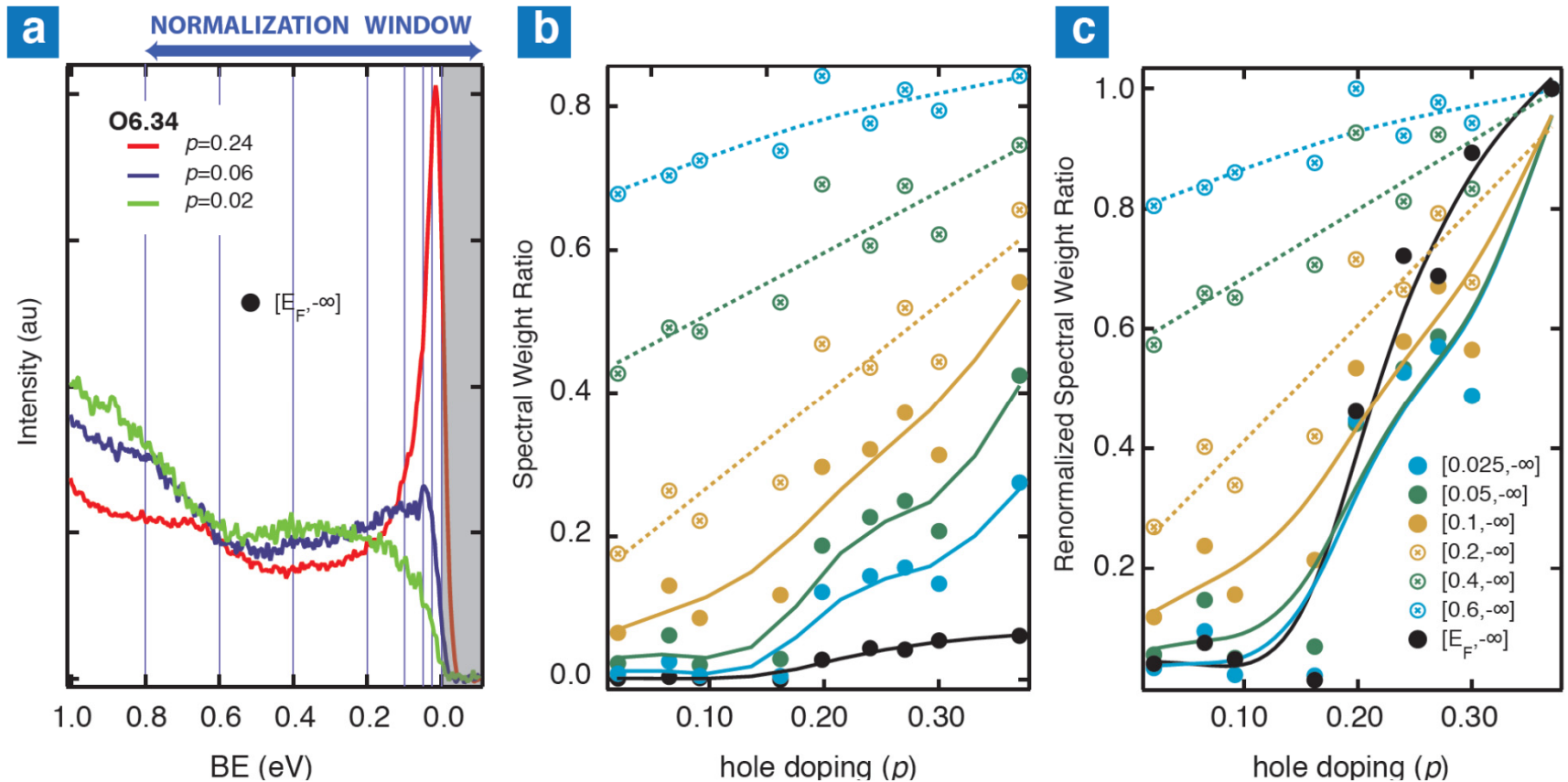


# Quasiparticle Coherence across the Phase Diagram



$$Z_k = \int I_{coh}(k, \omega) d\omega / \int I(k, \omega) d\omega$$

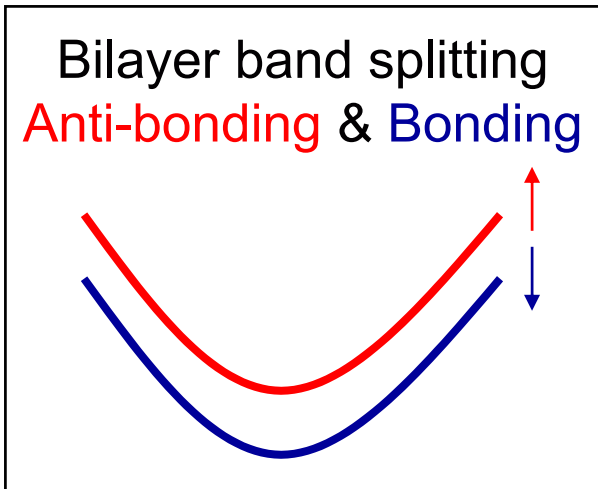
# Quasiparticle Coherence across the Phase Diagram



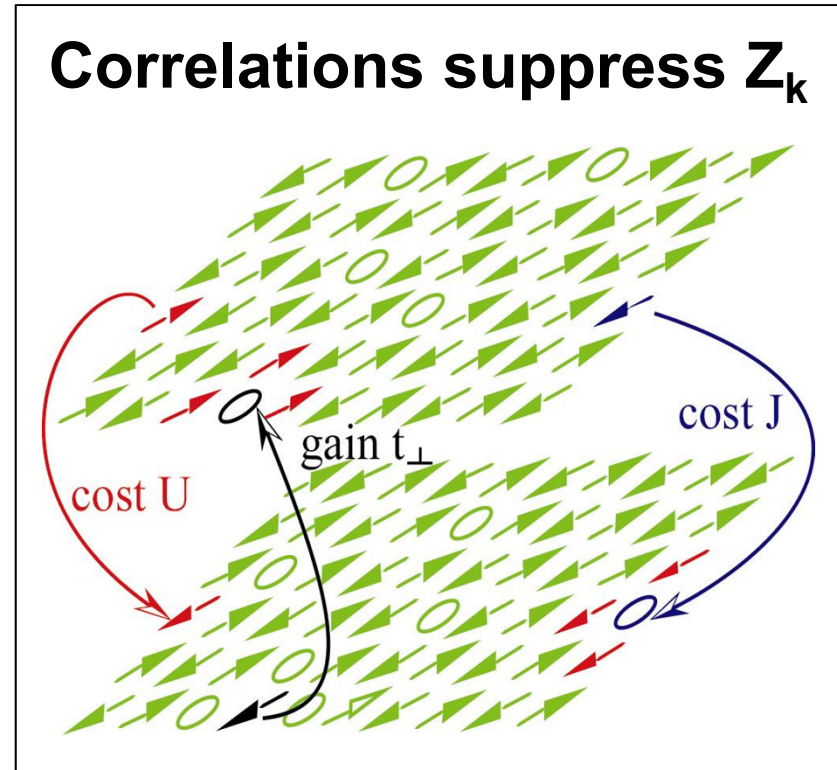
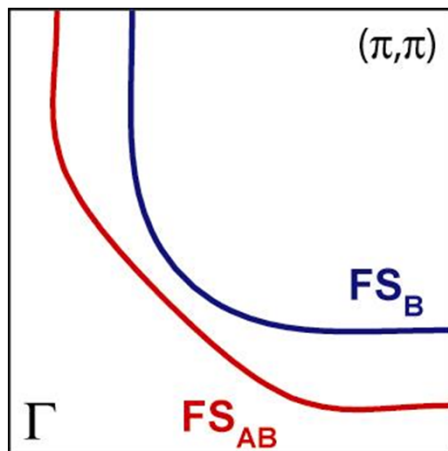
$$Z_N = \int_{BE_{min}}^{-\infty} I(k_{F,N}, \omega) d\omega / \int_{0.8 eV}^{-\infty} I(k_{F,N}, \omega) d\omega$$

# Bilayer Band Splitting and Quasiparticle Integrity

$$\epsilon^{B,AB}(k) = \epsilon(k) \mp t_{\perp}^{eff}(k) = \epsilon(k) \mp Z_k t_{\perp}^{LDA}(k)$$



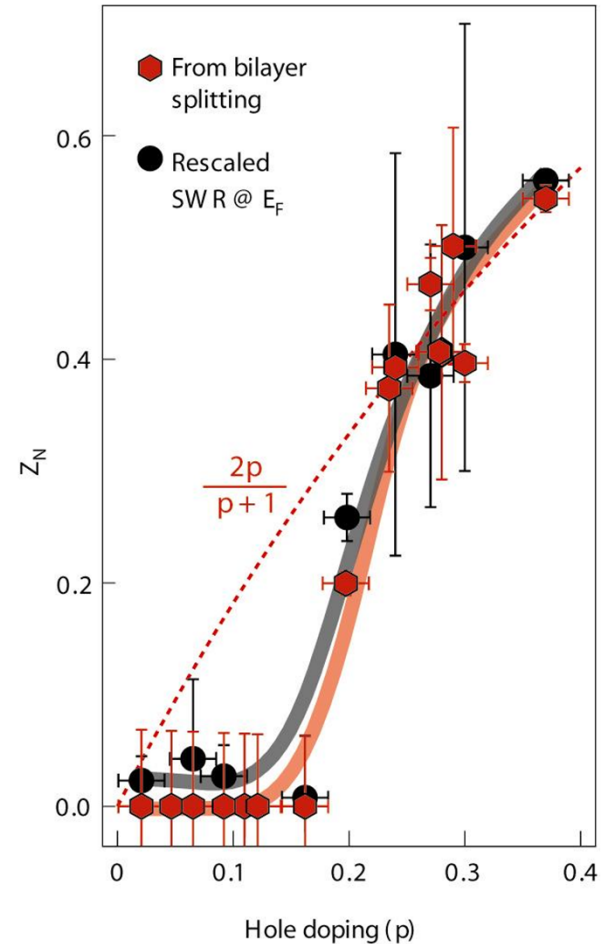
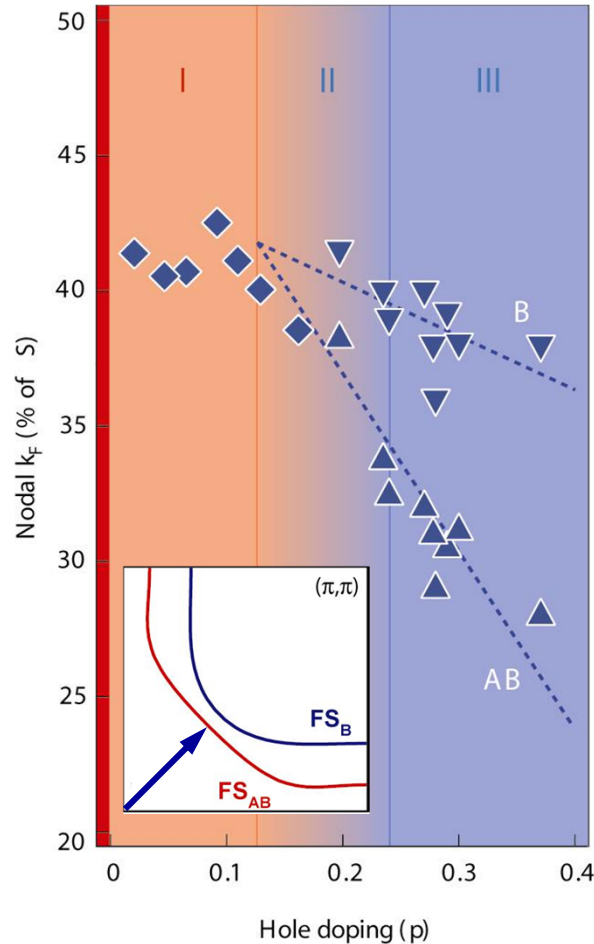
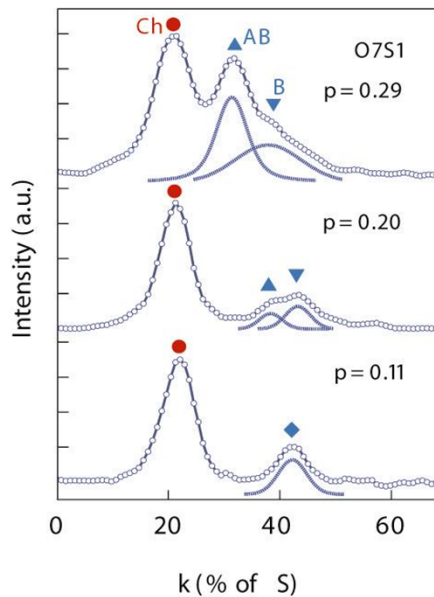
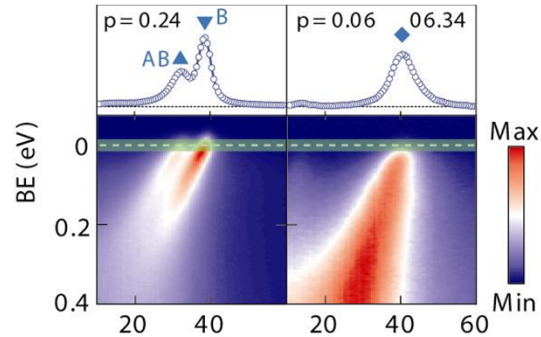
FS with bilayer splitting



$$Z \simeq 2p / (p + 1)$$

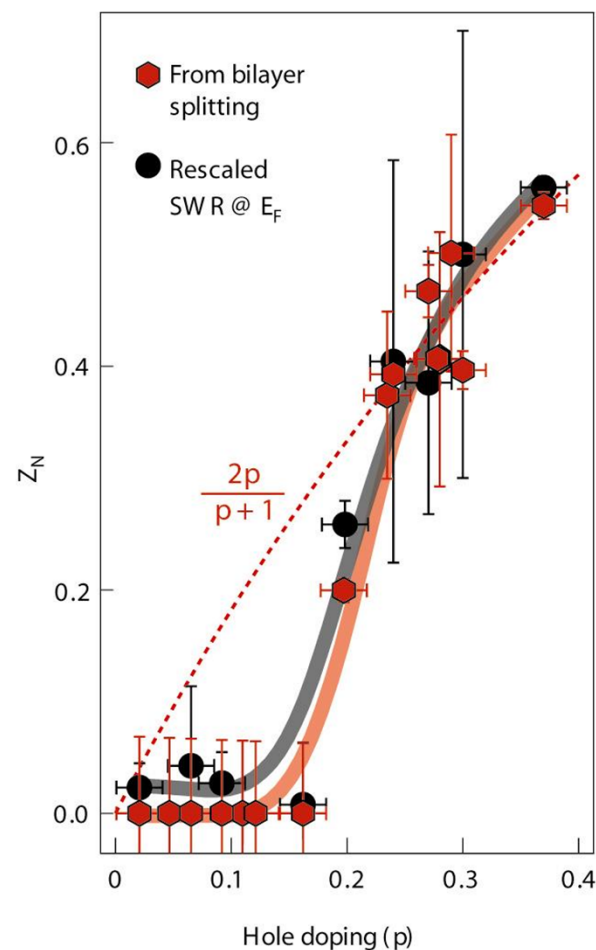
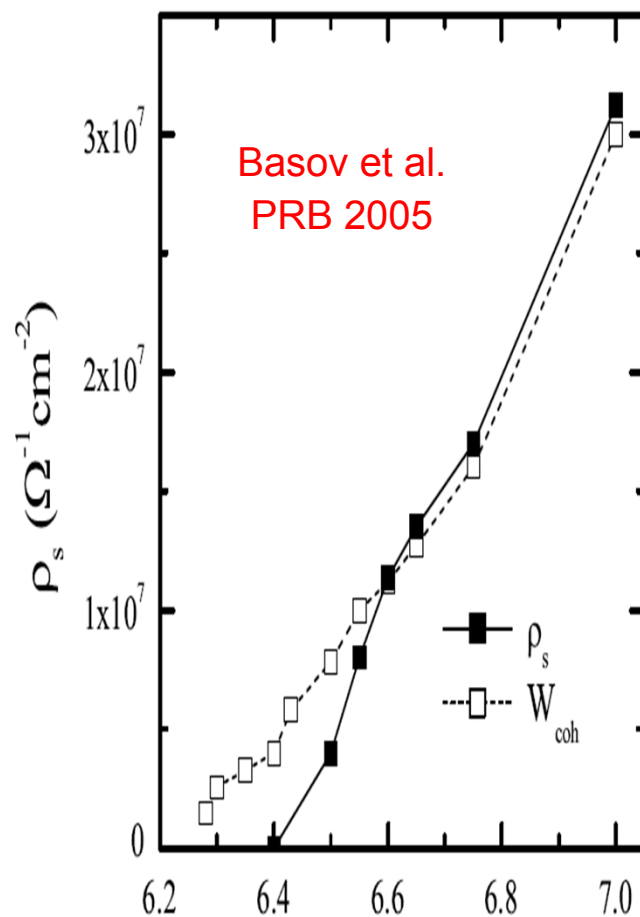
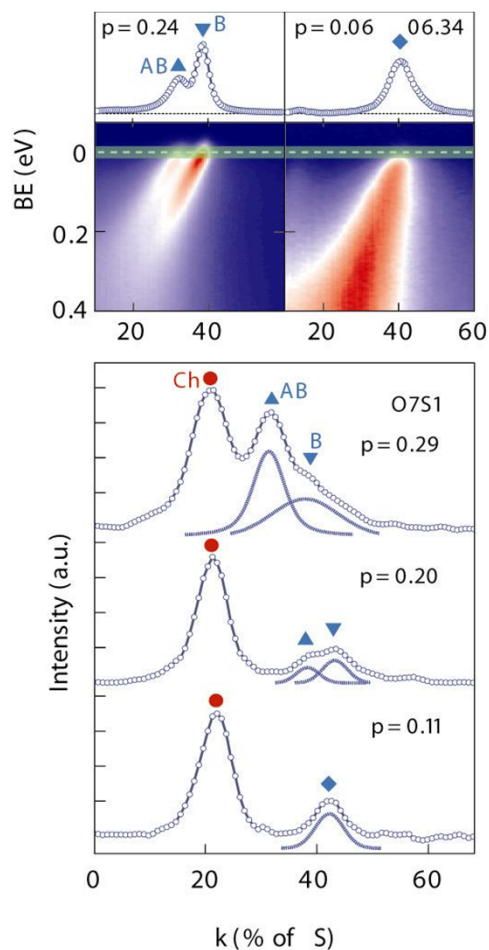
# Bilayer band splitting and quasiparticle coherence

$$Z_N = \Delta \epsilon_N^{B,AB} / 2t_{\perp}^{LDA}(N)$$



# Bilayer band splitting and quasiparticle coherence

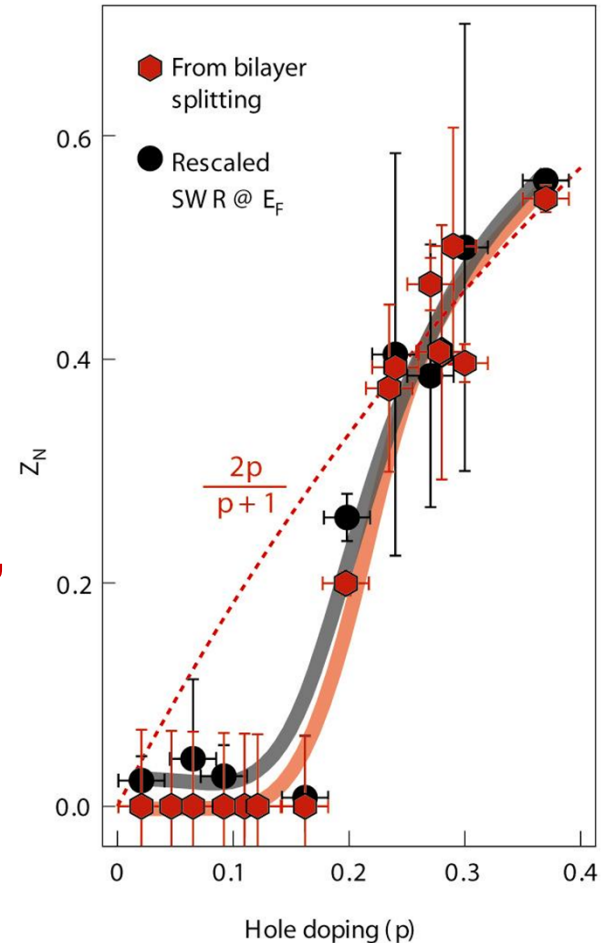
$$Z_N = \Delta \epsilon_N^{B,AB} / 2t_{\perp}^{LDA}(N)$$



# Bilayer band splitting and quasiparticle coherence

$$Z_N = \Delta \epsilon_N^{B,AB} / 2t_{\perp}^{LDA}(N)$$

- Quantitative estimate of  $Z$
- Agreement with  $2p/(p+1)$  for  $x > 0.23$
- Isotropic  $Z_N \sim 0.54$  and  $Z_{AN} \sim 0.50$
- Vanishing  $Z_N$  below 15-10%
- $t_{\perp} \sim 10\text{meV}$  consistent with QO
- $Z$  even smaller for pockets' "other side"
- Pseudogap? Loss of coherent SW
- Fermi surface? Luttinger's counting?







# Outline Part II

References, slides,  
and lecture notes

CUSO Lecture – Lausanne 02/2011

Physica Scripta. Vol. T109, 61–74, 2004

## Probing the Electronic Structure of Complex Systems by ARPES

Andrea Damascelli

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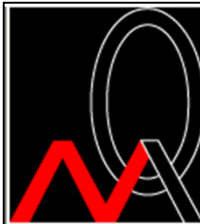
Received June 18, 2003; accepted June 30, 2003

PACS Ref: 79.60.i, 71.18.+y; 71.20.-b

### Abstract

Angle-resolved photoemission spectroscopy (ARPES) is one of the most direct methods of studying the electronic structure of solids. By measuring the kinetic energy and angular distribution of the electrons photoemitted from a sample illuminated with sufficiently high-energy radiation, one can gain information on both the energy and momentum of the electrons propagating inside a material. This is of vital importance in elucidating the connection between electronic, magnetic, and chemical structure of solids, in particular for those complex systems which cannot be appropriately described within the independent-particle picture. The last decade witnessed significant progress in this technique and its applications, thus ushering in a new era in photoelectron spectroscopy; today, ARPES experiments with 2 meV energy resolution and  $0.2^\circ$  angular resolution are a reality even for photoemission on solids. In this paper we will review the fundamentals of the technique and present some illustrative experimental results; we will show how ARPES can probe the momentum-dependent electronic structure of solids providing detailed information on band dispersion and Fermi surface as well as on the strength and nature of many-body correlations, which may profoundly affect the one-electron excitation spectrum and in turn the macroscopic physical properties.

photoemission event is decomposed in three independent steps: optical excitation between the initial and final *bulk* Bloch eigenstates, *travel* of the excited electron to the surface, and escape of the photoelectron into vacuum after transmission through the *surface* potential barrier. This is the most common approach, in particular when photoemission spectroscopy is used as a tool to map the electronic band structure of solids. However, from the quantum-mechanical point of view photoemission should not be described in terms of several independent events but rather as a *one-step* process (Fig. 1(b)): in terms of an optical transition (with probability given by Eq. (12)) between initial and final states consisting of many-body wave functions that obey appropriate boundary conditions at the surface of the solid. In particular (see Fig. 2), the initial state should be one of the possible  $N$ -electron eigenstates of the semi-infinite crystal, and the final state must be one of the



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# ARPES ON COMPLEX SYSTEMS

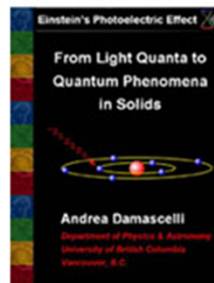
## Electronic and Magnetic Interactions in Novel Complex Systems

Angle-resolved photoemission spectroscopy (ARPES) is one of the most direct methods of studying the electronic structure of solids and is the only truly momentum-resolved probe, which is essential for the investigation of low dimensional and strongly anisotropic systems. By measuring momentum and kinetic energy of the electrons photoemitted from a sample illuminated with radiation of energy larger than the material work function, it is possible to gain information on both energy and the momentum of the electronic excitations inside the solid.

As the intensity measured in photoemission experiments is proportional to the single-particle spectral function  $A(\mathbf{k},\omega) = -\frac{1}{\pi} \text{Im}G(\mathbf{k},\omega)$ , ARPES provides direct insights on the Green's function  $G(\mathbf{k},\omega)$  which describes the propagation of an electron in a many-body system. This is of vital importance in elucidating the connection between electronic, magnetic, and chemical structure of solids, in particular for those complex systems which cannot be described within the independent-particle picture.

The last decade witnessed significant progress in this technique and its applications, thus ushering in a new era in photoelectron spectroscopy. Today, ARPES experiments with 2 meV energy resolution and 0.2 degree angular resolution are a reality even for photoemission on solids, providing detailed information on band dispersion and Fermi surface, as well as on the strength and nature of those many-body correlations which may profoundly affect the one-electron excitation spectrum and, in turn, determine the macroscopic physical properties.

The Photoelectric Effect



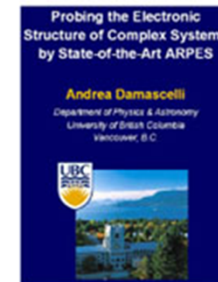
ARPES: Introduction



ARPES on HTSC's



ARPES: Viewgraphs





UNIVERSITY OF BRITISH COLUMBIA

Andrea Damascelli

*UBC-MPI Quantum Matter Institute*

Thank you!

CUSO Lecture – Lausanne 02/2011