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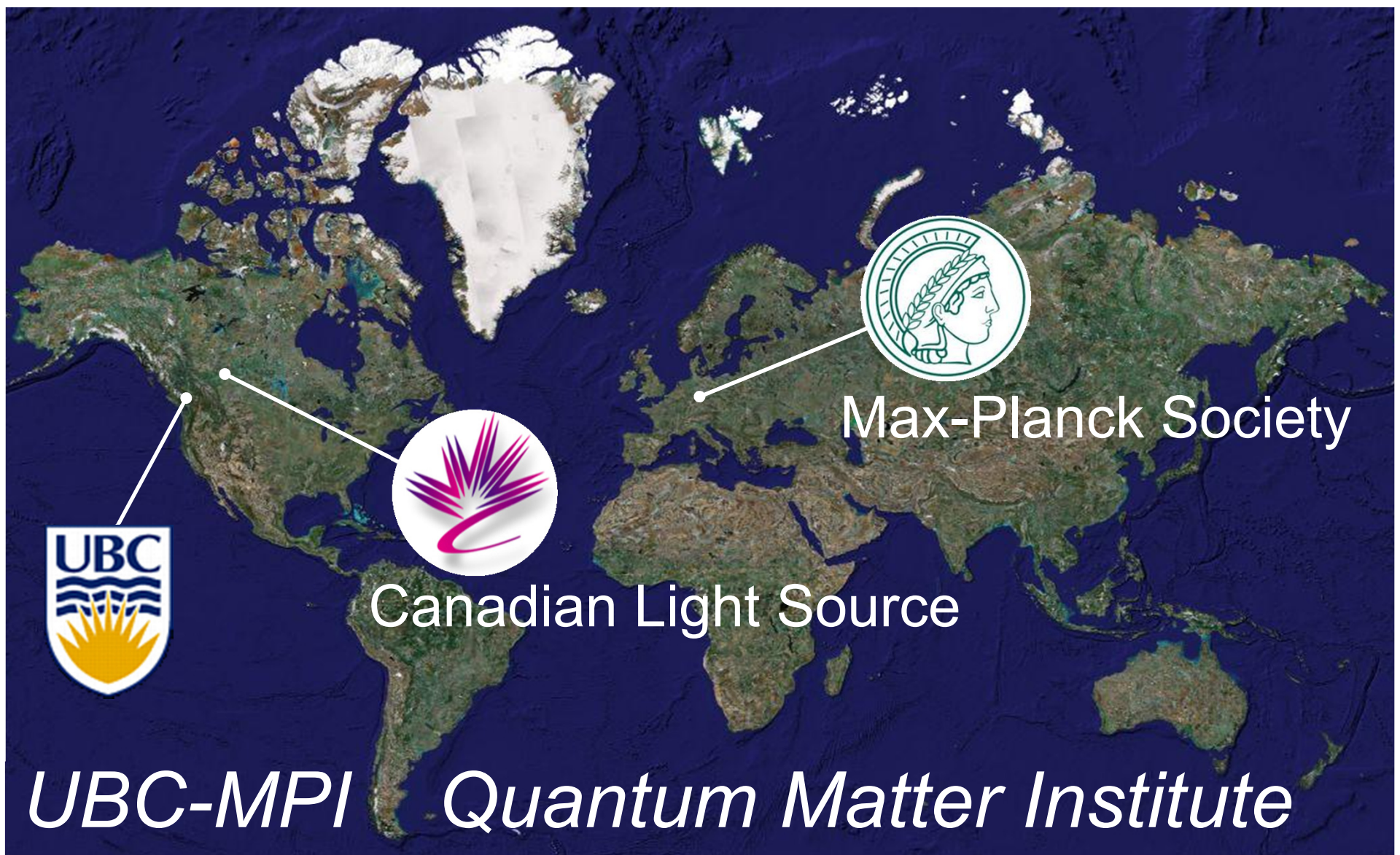
Andrea Damascelli

*UBC-MPI Quantum Matter Institute*

# ARPES on Correlated Electron Systems

CUSO Lecture – Lausanne 02/2011





  
Canadian Light Source

  
Max-Planck Society

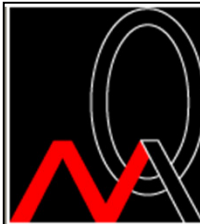
*UBC-MPI Quantum Matter Institute*



## Outline Part I

- Introduction: Transition metal oxides
- Birth and history of photoemission
- ARPES: Fundamentals and spectral function
- ARPES: Technique and developments
- Bulk, surface, and Fermi surfaces:  $\text{Sr}_2\text{RuO}_4$
- Superconducting gap: BCS and HTSC

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people

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projects

- ARPES intro
- open positions

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presentations

pictures

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# ARPES ON COMPLEX SYSTEMS

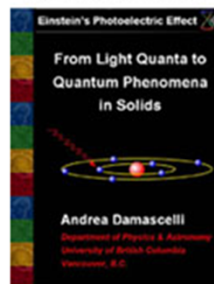
## Electronic and Magnetic Interactions in Novel Complex Systems

Angle-resolved photoemission spectroscopy (ARPES) is one of the most direct methods of studying the electronic structure of solids and is the only truly momentum-resolved probe, which is essential for the investigation of low dimensional and strongly anisotropic systems. By measuring momentum and kinetic energy of the electrons photoemitted from a sample illuminated with radiation of energy larger than the material work function, it is possible to gain information on both energy and the momentum of the electronic excitations inside the solid.

As the intensity measured in photoemission experiments is proportional to the single-particle spectral function  $A(\mathbf{k},\omega) = -\frac{1}{\pi} \text{Im}G(\mathbf{k},\omega)$ , ARPES provides direct insights on the Green's function  $G(\mathbf{k},\omega)$  which describes the propagation of an electron in a many-body system. This is of vital importance in elucidating the connection between electronic, magnetic, and chemical structure of solids, in particular for those complex systems which cannot be described within the independent-particle picture.

The last decade witnessed significant progress in this technique and its applications, thus ushering in a new era in photoelectron spectroscopy. Today, ARPES experiments with 2 meV energy resolution and 0.2 degree angular resolution are a reality even for photoemission on solids, providing detailed information on band dispersion and Fermi surface, as well as on the strength and nature of those many-body correlations which may profoundly affect the one-electron excitation spectrum and, in turn, determine the macroscopic physical properties.

The Photoelectric Effect



ARPES: Introduction



ARPES on HTSC's



ARPES: Viewgraphs



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## Probing the Electronic Structure of Complex Systems by ARPES

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PACS Ref: 79.60.i, 71.18.+y; 71.20.-b

### Abstract

Angle-resolved photoemission spectroscopy (ARPES) is one of the most direct methods of studying the electronic structure of solids. By measuring the kinetic energy and angular distribution of the electrons photoemitted from a sample illuminated with sufficiently high-energy radiation, one can gain information on both the energy and momentum of the electrons propagating inside a material. This is of vital importance in elucidating the connection between electronic, magnetic, and chemical structure of solids, in particular for those complex systems which cannot be appropriately described within the independent-particle picture. The last decade witnessed significant progress in this technique and its applications, thus ushering in a new era in photoelectron spectroscopy; today, ARPES experiments with 2 meV energy resolution and  $0.2^\circ$  angular resolution are a reality even for photoemission on solids. In this paper we will review the fundamentals of the technique and present some illustrative experimental results; we will show how ARPES can probe the momentum-dependent electronic structure of solids providing detailed information on band dispersion and Fermi surface as well as on the strength and nature of many-body correlations, which may profoundly affect the one-electron excitation spectrum and in turn the macroscopic physical properties.

photoemission event is decomposed in three independent steps: optical excitation between the initial and final *bulk* Bloch eigenstates, *travel* of the excited electron to the surface, and escape of the photoelectron into vacuum after transmission through the *surface* potential barrier. This is the most common approach, in particular when photoemission spectroscopy is used as a tool to map the electronic band structure of solids. However, from the quantum-mechanical point of view photoemission should not be described in terms of several independent events but rather as a *one-step* process (Fig. 1(b)): in terms of an optical transition (with probability given by Eq. (12)) between initial and final states consisting of many-body wave functions that obey appropriate boundary conditions at the surface of the solid. In particular (see Fig. 2), the initial state should be one of the possible  $N$ -electron eigenstates of the semi-infinite crystal, and the final state must be one of the



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# Outline Part I

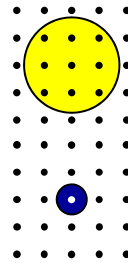
## Introduction:

## Transition metal oxides

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# Strongly Correlated Electron Systems

d - f  
open  
shells  
materials



$U \ll W$   
Charge fluctuations

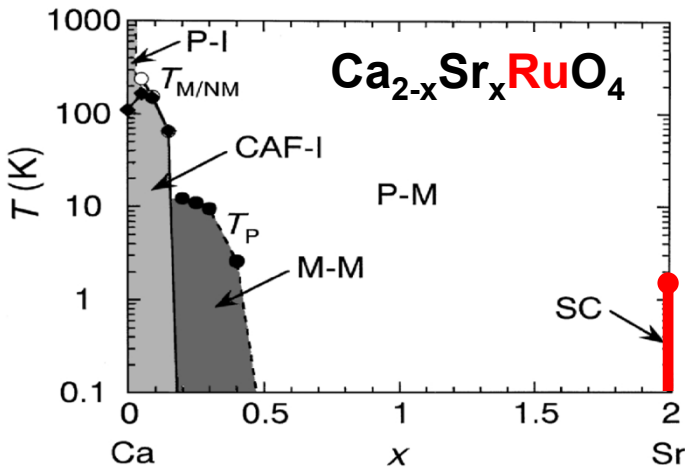
$U \gg W$   
Spin fluctuations

I	II	IIIb	IVb	Vb	VIb	VIIb	VIIIb	Ib	IIb	III	IV	V	VI	VII	0		
H															He		
Li	Be									B	C	N	O	F	Ne		
Na	Mg									Al	Si	P	S	Cl	Ar		
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba	La*	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
Fr	Ra	Ac**	Rf	Db	Sg	Bh	Hs	Mt									
Lanthanides *		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu		
Actinides **		Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr		

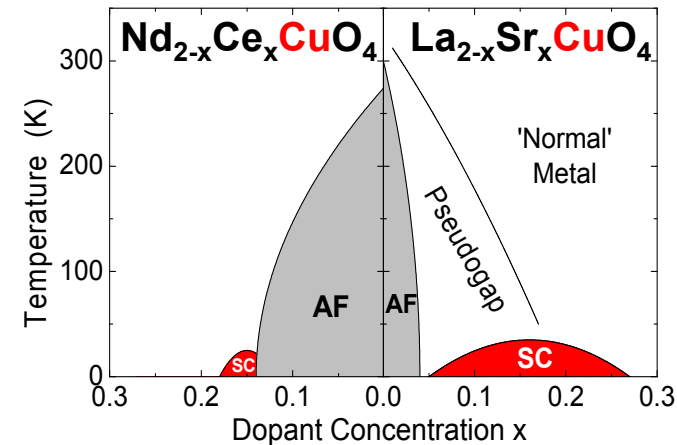
Control  
parameters

Bandwidth ( $U/W$ )  
Band filling  
Dimensionality

Degrees of  
freedom  
Charge / Spin  
Orbital  
Lattice



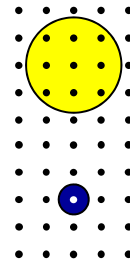
- Kondo
- Mott-Hubbard
- Heavy Fermions
- Unconventional SC
- Spin-charge order
- Colossal MR





# Strongly Correlated Electron Systems

**d - f  
open  
shells  
materials**



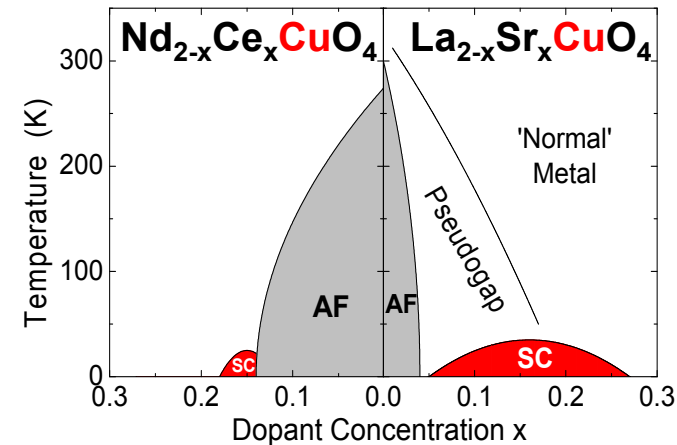
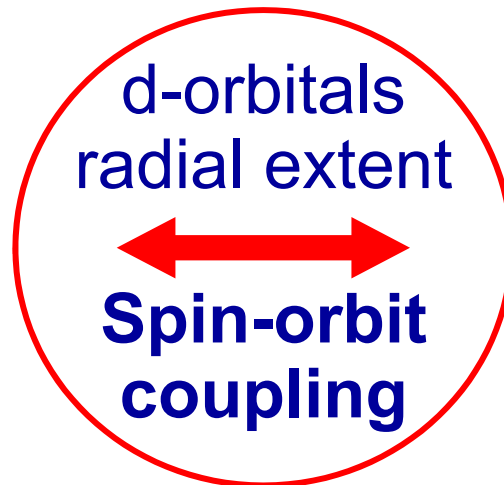
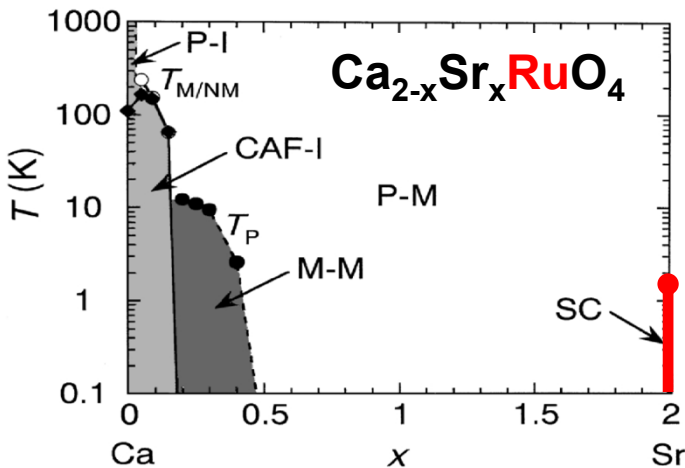
$U \ll W$   
Charge fluctuations

$U \gg W$   
Spin fluctuations

**Control  
parameters**  
Bandwidth ( $U/W$ )  
Band filling  
Dimensionality

I	II	IIIb	IVb	Vb	VIb	VIIb	VIIIb	Ib	IIb	III	IV	V	VI	VII	0		
H															He		
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Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe
Cs	Ba	La*	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn
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**Degrees of  
freedom**  
Charge / Spin  
Orbital  
Lattice

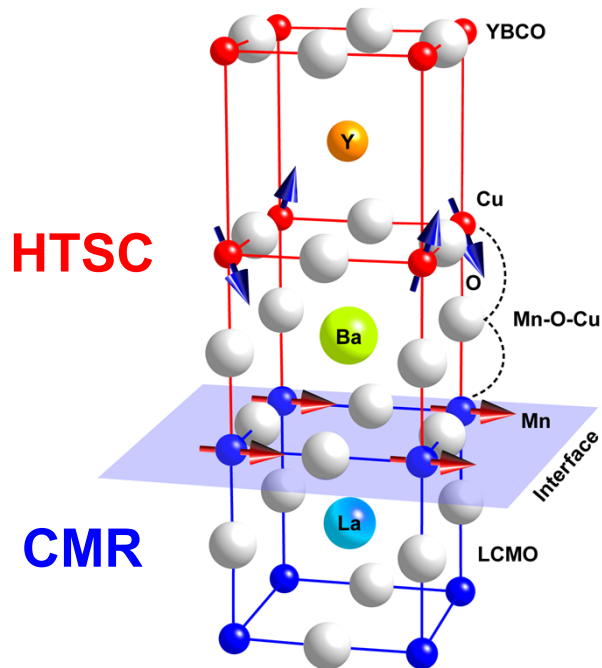


# Novel Complex Materials and Functionalities



**Tune the physical properties**

Chakhalian et al., Nature Physics 2006



- Modern synthesis methods  
Single crystals, multilayers, nanostructures
- Sophisticated structural tools  
Physical, chemical, and magnetic structures
- Novel probes of intrinsic susceptibilities  
Lattice, magnetic, and electronic excitations

$$\begin{array}{cc} \varepsilon(q, q', \omega) & \chi(q, q', \omega) \\ N(\vec{r}, E) & A(\vec{k}, E) \end{array}$$

Interface-tuned magnetism  
in oxide multilayers



Understand interplay of  
**lattice, spin, charge, orbital**  
degrees of freedom



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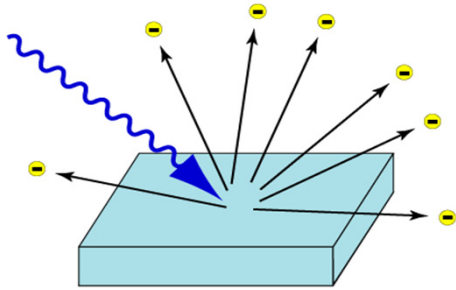


# Outline Part I

## Birth and history of photoemission

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# Probing Electrons in Reciprocal Space



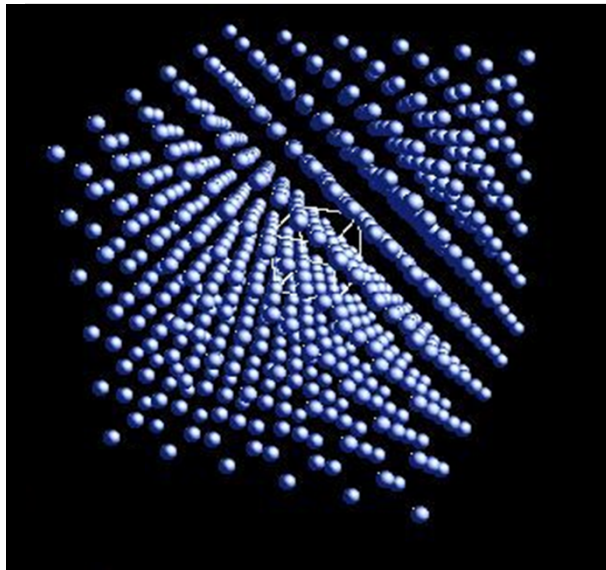
## Angle Resolved PhotoElectron Spectroscopy

FIRST EVIDENCE FOR THE QUANTIZATION OF LIGHT!

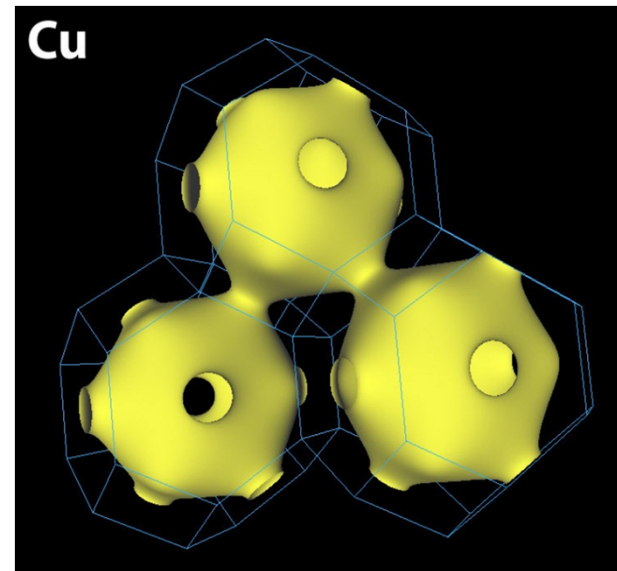
**Velocity and direction of the electrons in the solid**

Low-energy Electronic Structure → Macroscopic Physical Properties

*Superconductivity, Magnetism, Density Waves, ....*



**X-ray diffraction**



**Photoemission**

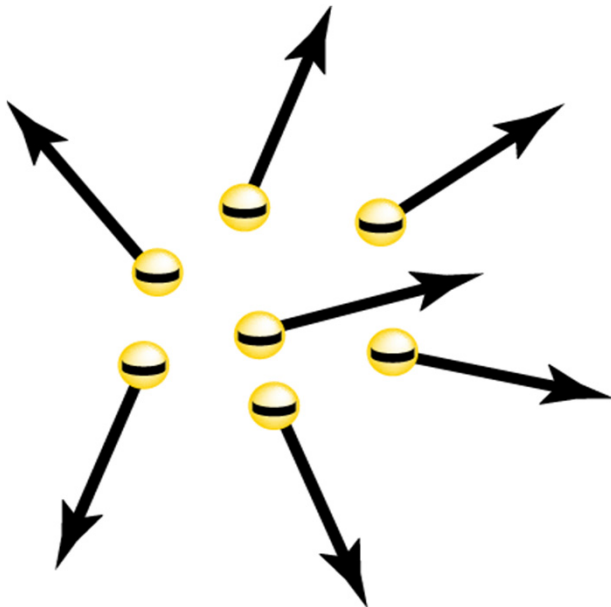
# Interaction Effects between Electrons : “Many-body Physics”

**Many-body effects** are due to the interactions between the **electrons** and **each other**, or with other **excitations inside the crystal** :

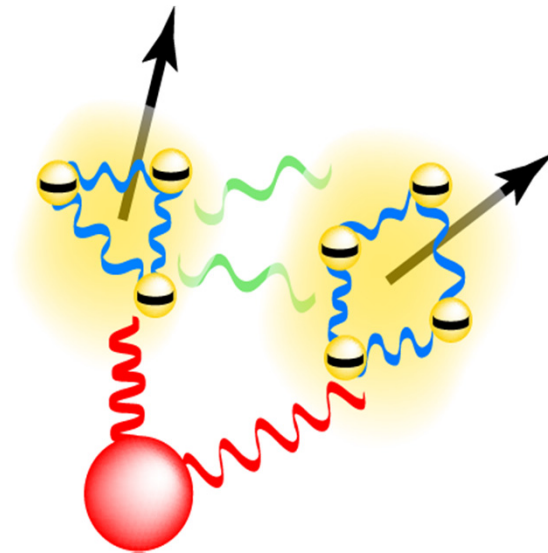
- 1) A “many-body” problem : intrinsically hard to calculate and understand
- 2) Responsible for many surprising phenomena :

***Superconductivity, Magnetism, Density Waves, ....***

**Non-Interacting**



**Interacting**



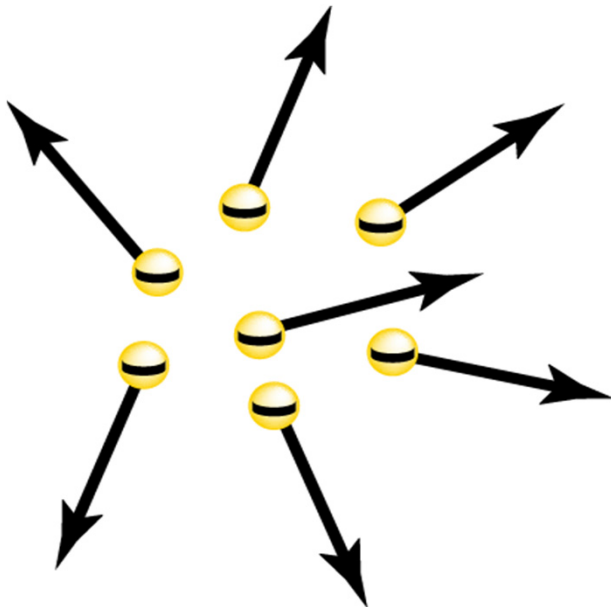
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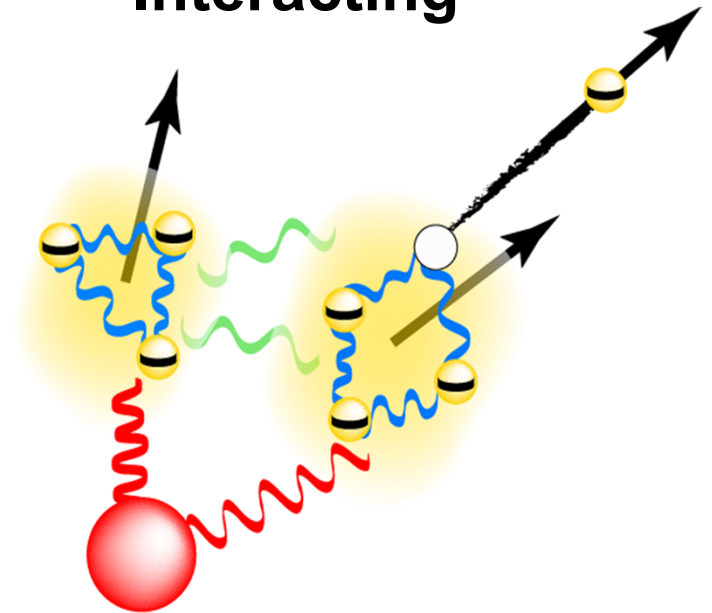
- 1) A “many-body” problem : intrinsically hard to calculate and understand
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***Superconductivity, Magnetism, Density Waves, ....***

**Non-Interacting**



**Interacting**



# Einstein's Annus Mirabilis: 1905



- **The Brownian motion**  
*"On the motion of small particles suspended in liquids at rest required by the molecular-kinetic theory of heat."*  
Annalen der Physik, **17** (1905), pp. 549-560.
- **The photoelectric effect**  
*"On a heuristic viewpoint concerning the production and transformation of light"*  
Annalen der Physik, **17** (1905), pp. 132-148.
- **The special theory of relativity**  
*"On the electrodynamics of moving bodies"*  
Annalen der Physik, **17** (1905), pp. 891-921
- **Mass-energy Equivalency  $E=mc^2$**   
*"Does the inertia of a body depend on its energy?"*  
Annalen der Physik, **18** (1905), pp. 639-41.

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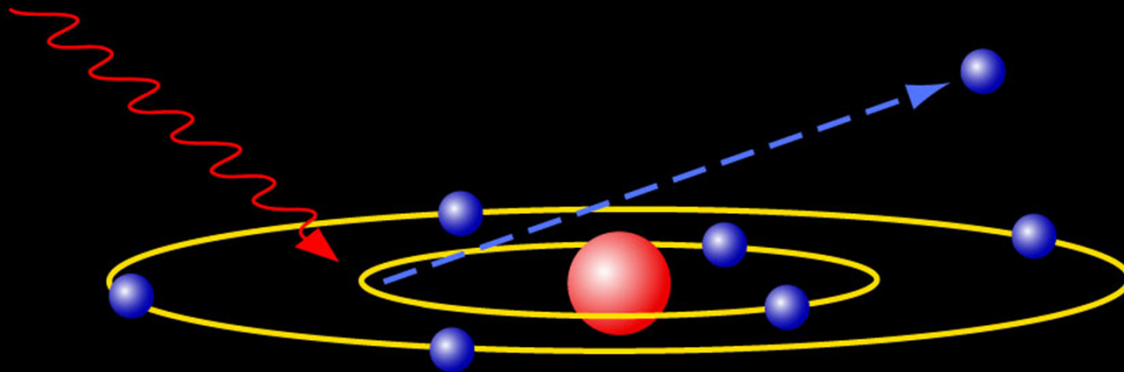
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# The Photoelectric Effect: Intro



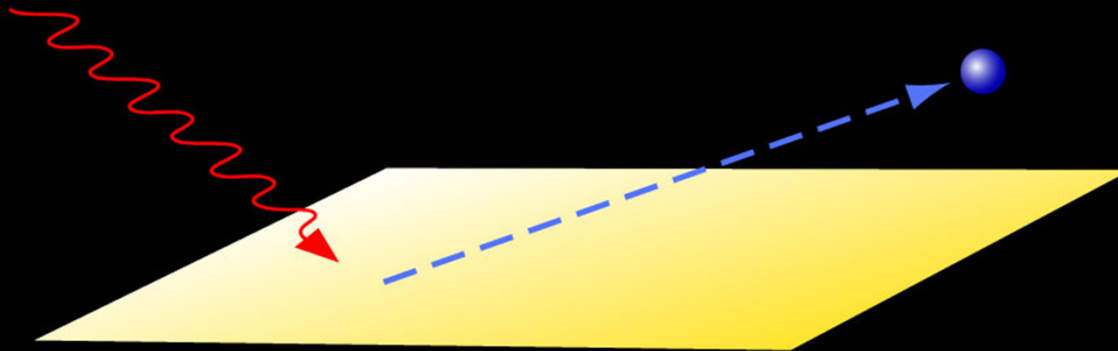
Emission of an **electron** due to the absorption of **light**



# The Photoelectric Effect: Intro



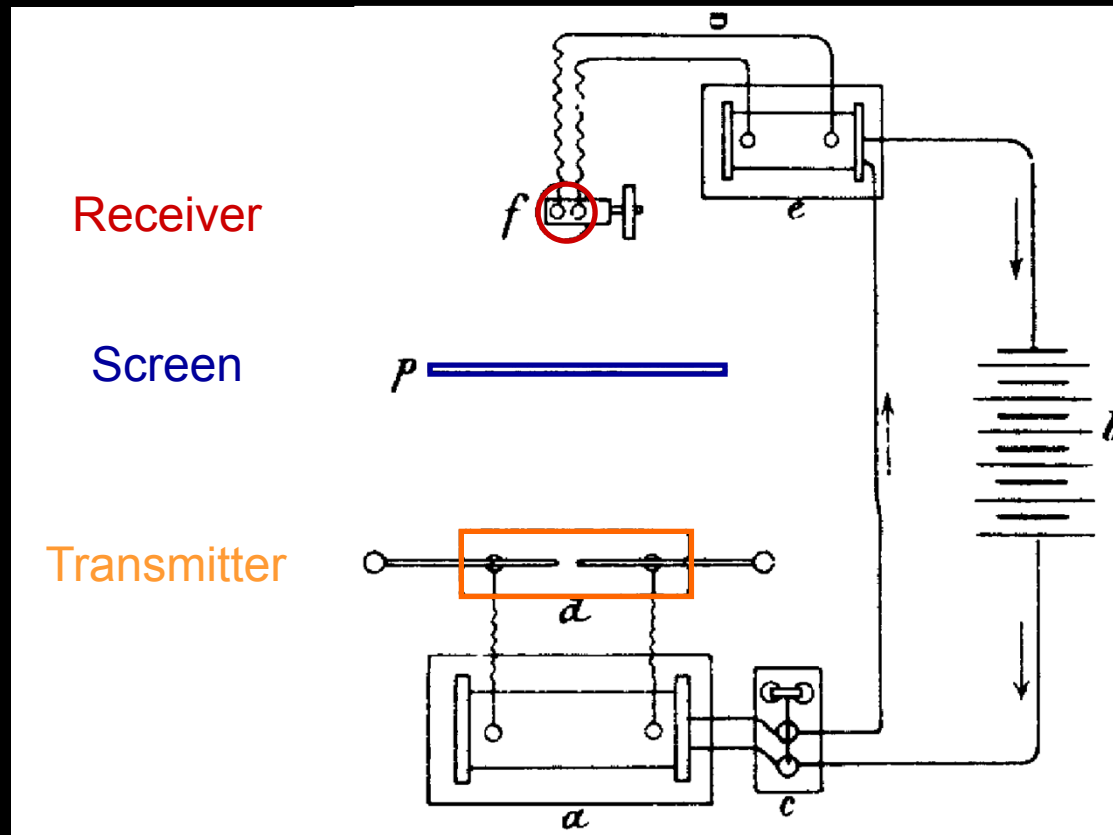
Emission of an **electron** due to the absorption of **light**



First experimental evidence  
for the quantization of light

# The Photoelectric Effect: History

**1887** Hertz finds **Maxwell's waves**; and something else

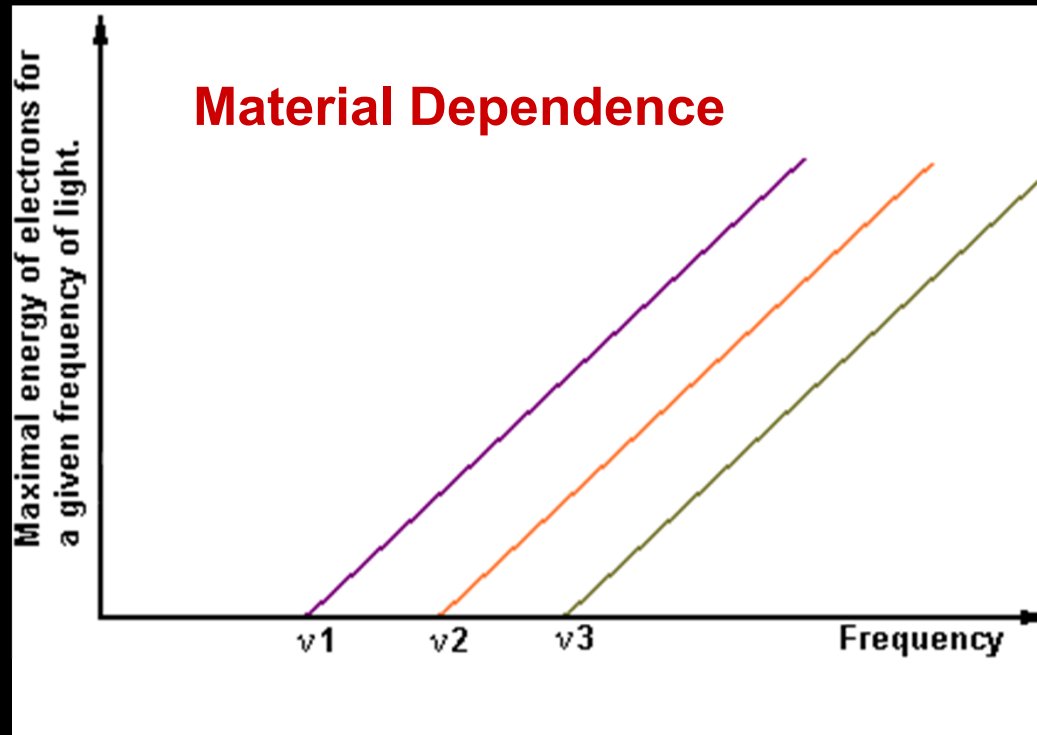


The small **RECEIVER SPARK** was more vigorous when the receiver was exposed to the ultraviolet light from the **TRANSMITTER SPARK**

# The Photoelectric Effect: History



**1902** von Lenard varies the **intensity** and **color** of the light



The **NUMBER** of electrons is proportional to the **INTENSITY**

The maximum  $E_{kin} = \frac{1}{2}mv^2$  is proportional to the **FREQUENCY**

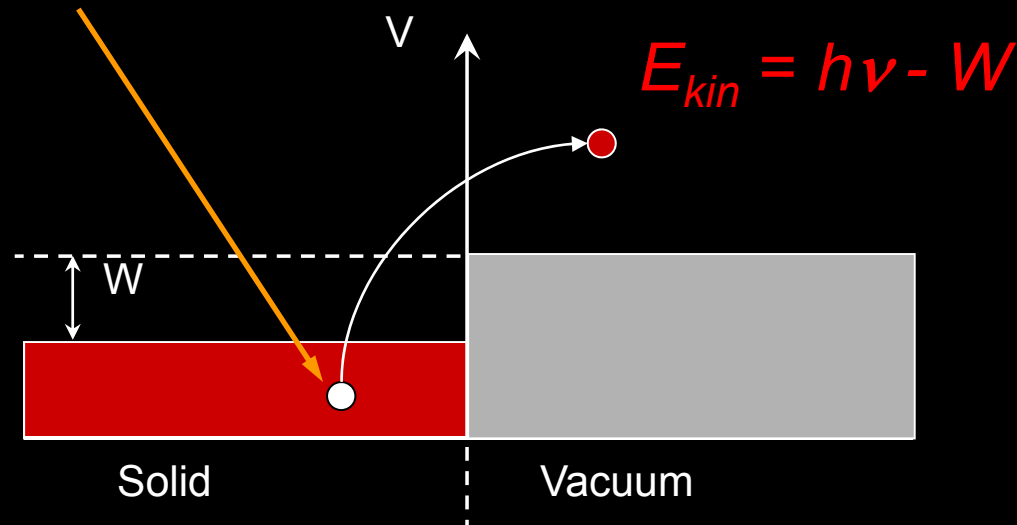
# The Photoelectric Effect: History



**1905** Einstein' hypothesis: **light quanta** with  $E = h\nu = hc / \lambda$

$$E = h\nu$$

$$h = 6.63 \times 10^{-34} \text{ Jsec} = 3.89 \times 10^{-15} \text{ eVsec}$$



The maximum  $E_{kin} = \frac{1}{2}mv^2$  is proportional to the FREQUENCY but depends also on the material work function  $W$

The NUMBER of electrons is proportional only to the INTENSITY

# The Photoelectric Effect: History



**1887** Heinrich Hertz

**1897** **Joseph Thomson:** “for the theoretical and experimental investigations on the conduction of electricity by gases”



1906

**1888** Wilhelm Hallwachs

**1902** **Philipp von Lenard:**  
“for his work on cathode rays”



1905

**1905** **Albert Einstein:** “for his services to Theoretical Physics, and .... for his discovery of the law of the photoelectric effect”



1921

**1916** **Robert Millikan:** “for his work on the elementary charge of electricity and on the photoelectric effect”



1923

# Einstein's hypothesis is too revolutionary

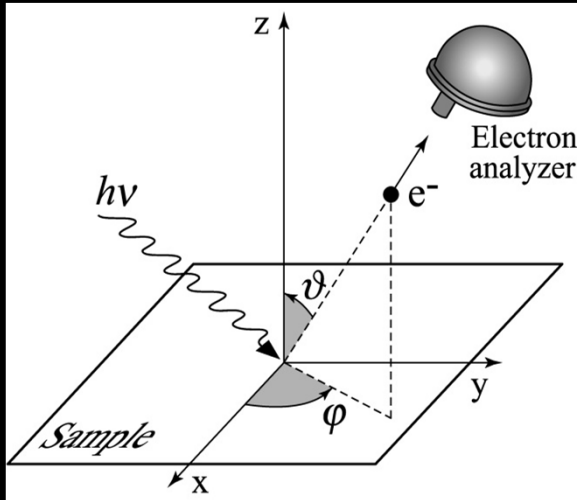


In 1913 Einstein was elected to the **Prussian Academy of Sciences** and appointed to a research position in Berlin. In his nomination speech to the Prussian Academy, **Planck** says:


"Summing up, we may say that there is hardly one among the great problems in which modern physics is so rich, to which Einstein has not made an important contribution."

"That he may sometimes have **missed the target** in his speculations, as for example, in his **hypothesis** of light quanta, **cannot really be held too much against** him, for it is not possible to introduce fundamentally new ideas, even in the most exact sciences, without occasionally taking a risk".

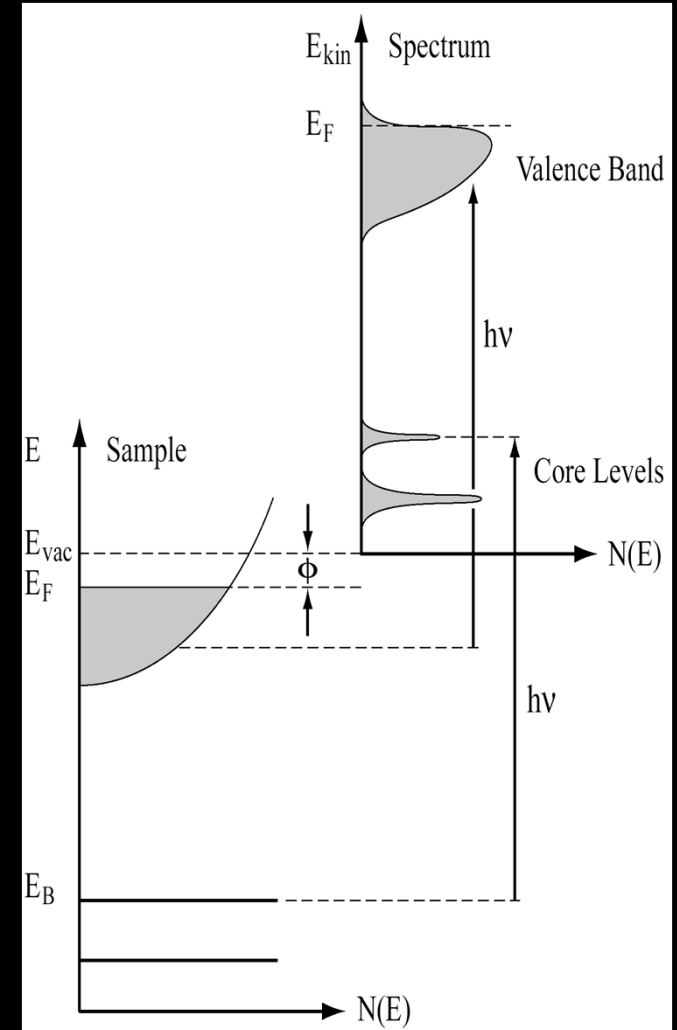
# Scientific application: Spectroscopy



## Electron Spectroscopy for Chemical Analysis (ESCA)

Kai Siegbahn:  1981

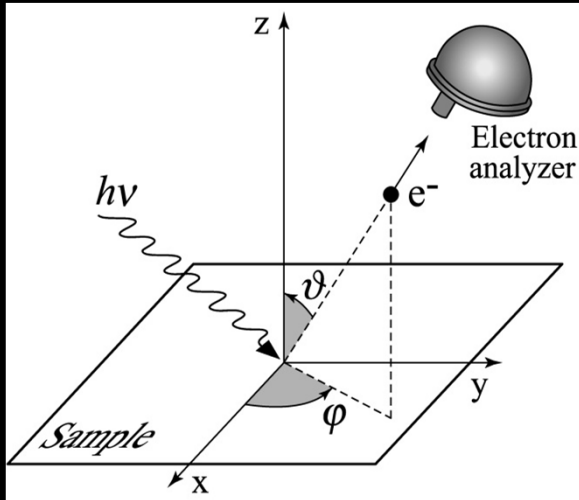
“for his contribution to the development of high-resolution electron spectroscopy”




$$E_{kin} = h\nu - \phi - |E_B|$$



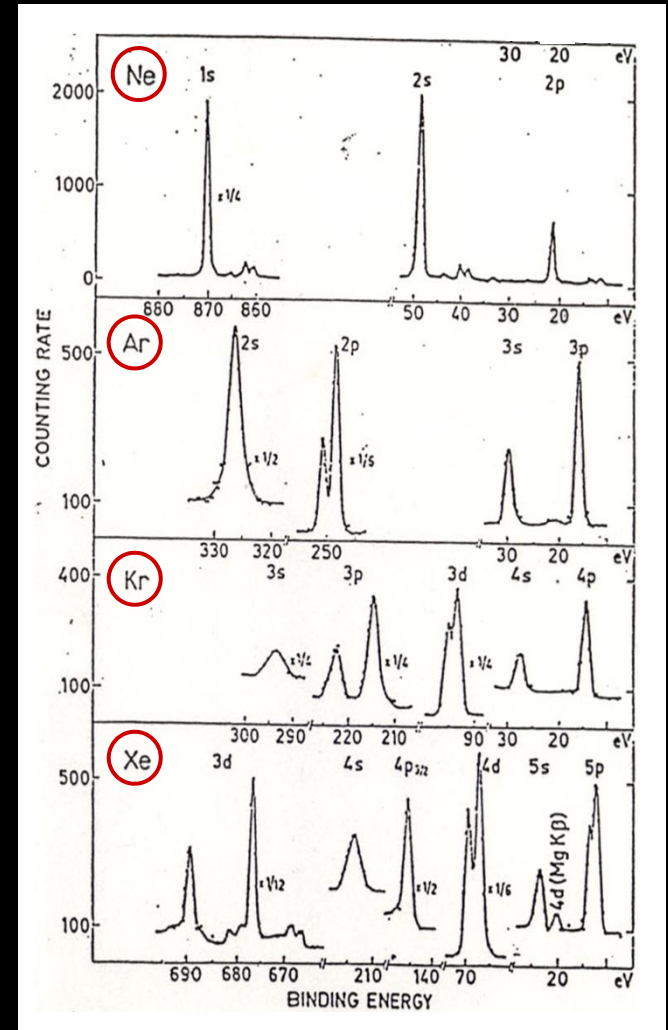
# Scientific application: Spectroscopy



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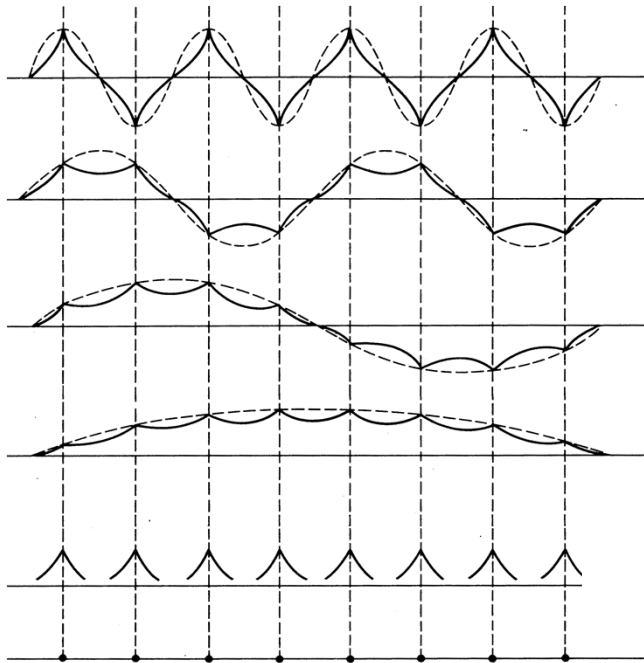
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$$E_{kin} = h\nu - \phi - |E_B|$$

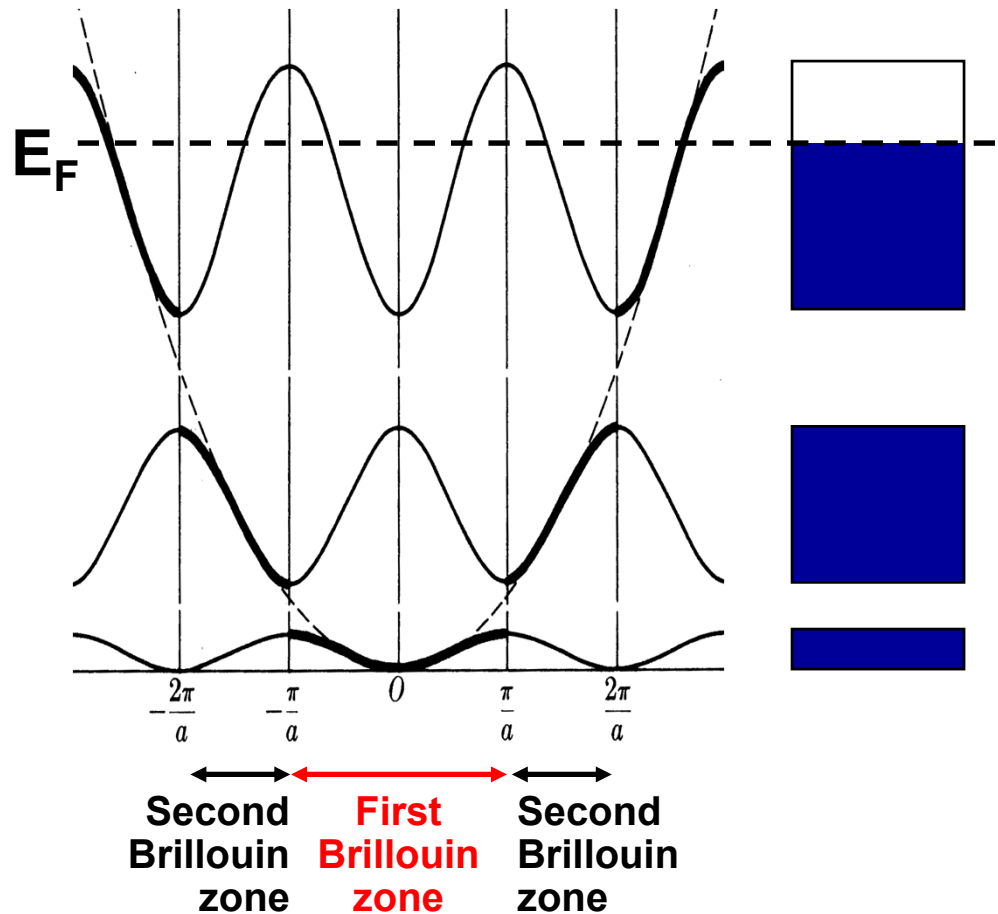
# Solid State: Electrons in Reciprocal Space

Wave functions  
in a 1D lattice



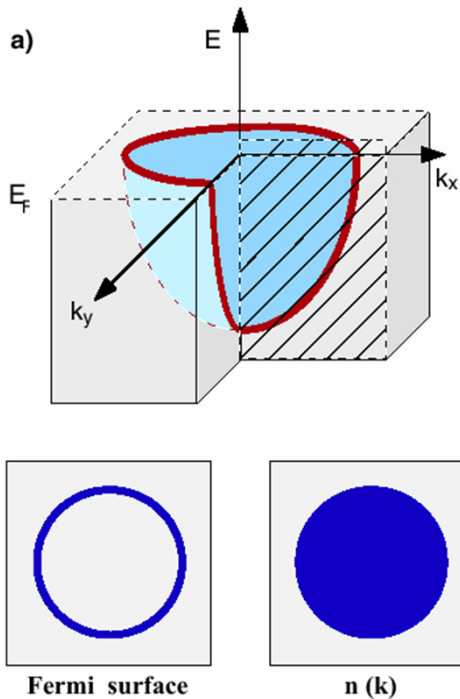
1D chain of atoms

Allowed electronic states  
Repeated-zone scheme



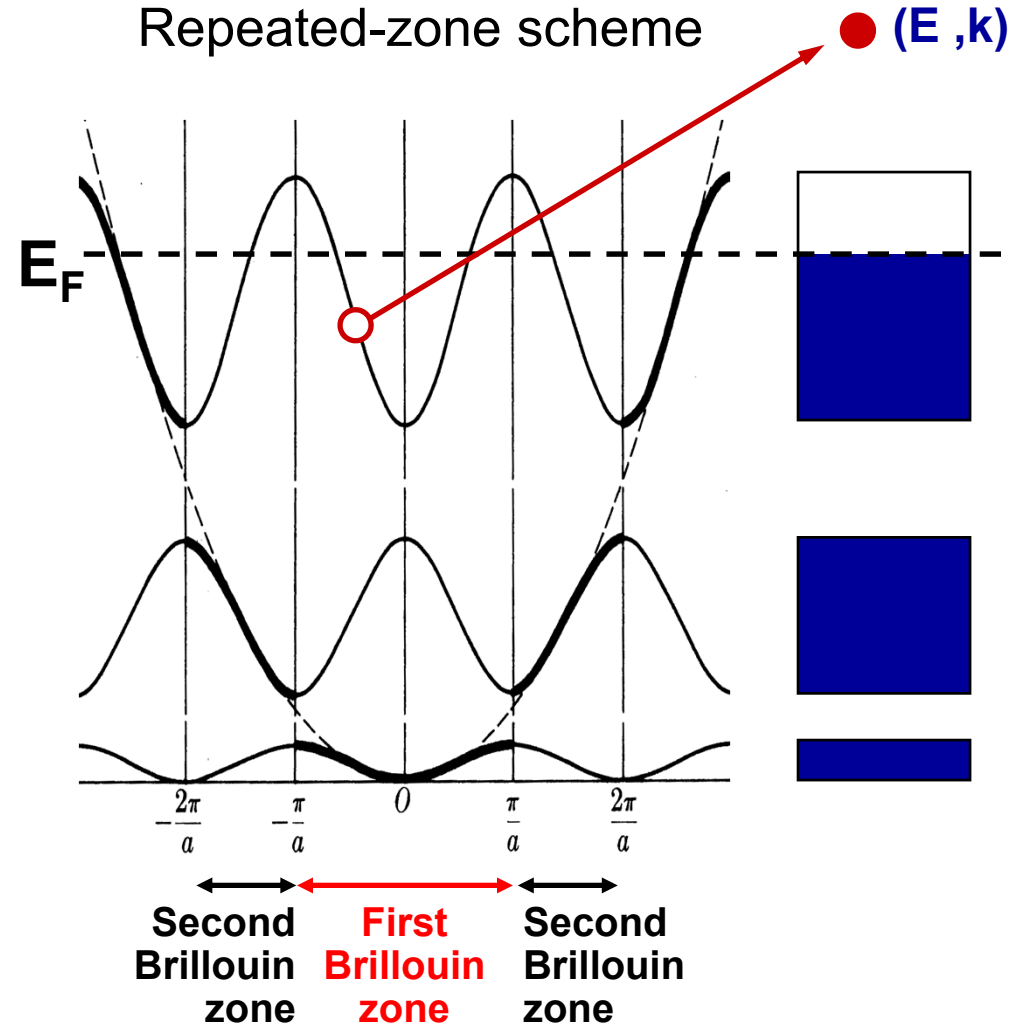
# Solid State: Electrons in Reciprocal Space

Many **properties** of a solids are determined by **electrons near  $E_F$**  (**conductivity, magnetoresistance, superconductivity, magnetism**)



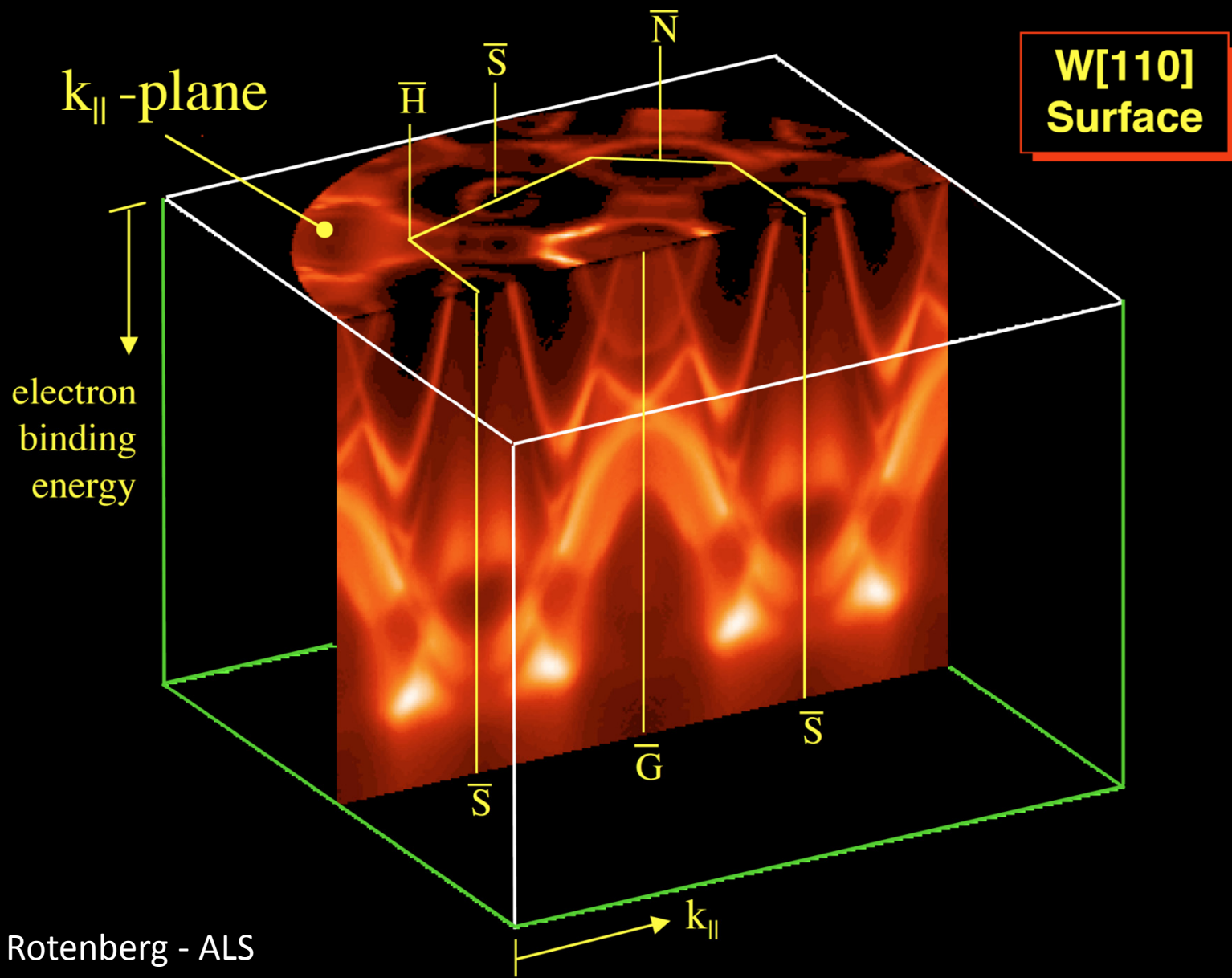
## Allowed electronic states

Repeated-zone scheme



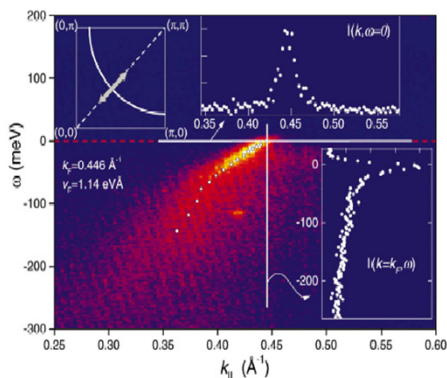
Only a **narrow energy slice** around  $E_F$  is relevant for these properties ( **$kT=25$  meV** at room temperature)

# Band Mapping and Fermi Contours



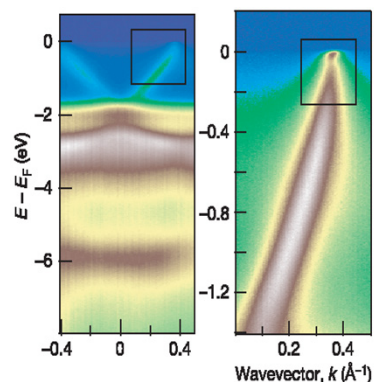
# ARPES: Widespread Impact in Complex Materials

## HTSC's



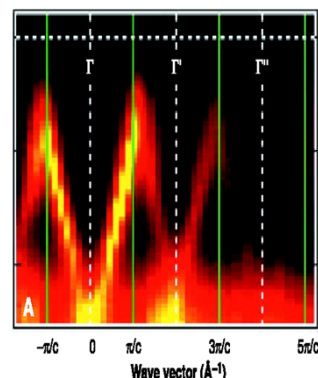
Science 1999

## CMR's



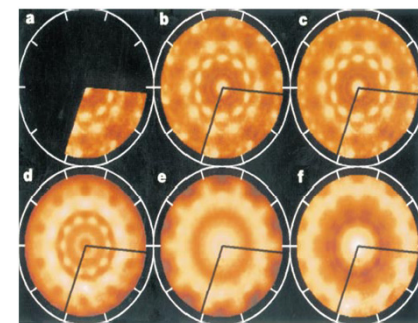
Nature 2005

## CDW's



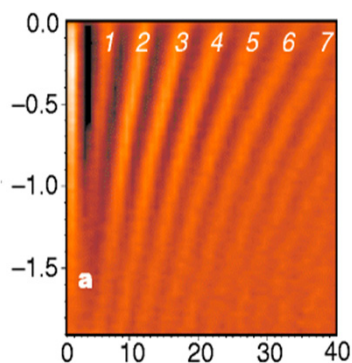
Science 2000

## Quasicrystals



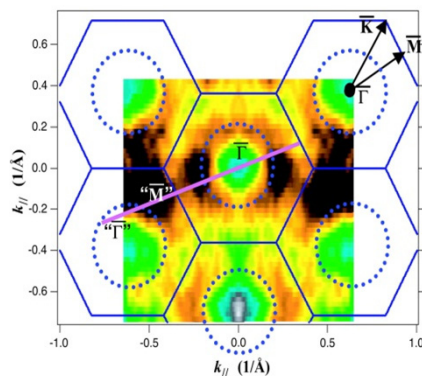
Nature 2000

## Quantum Wells



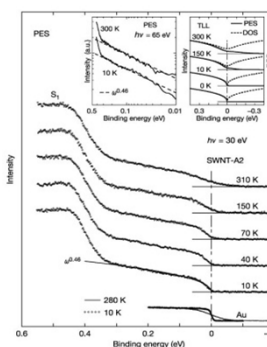
Nature 1999

## C<sub>60</sub>



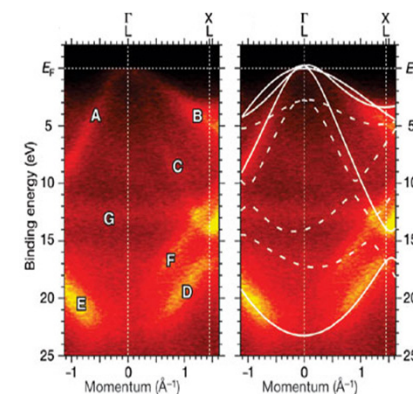
Science 2003

## Nanotubes



Nature 2003

## Diamond



Nature 2005



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# Outline Part I

## ARPES: Fundamentals and spectral function

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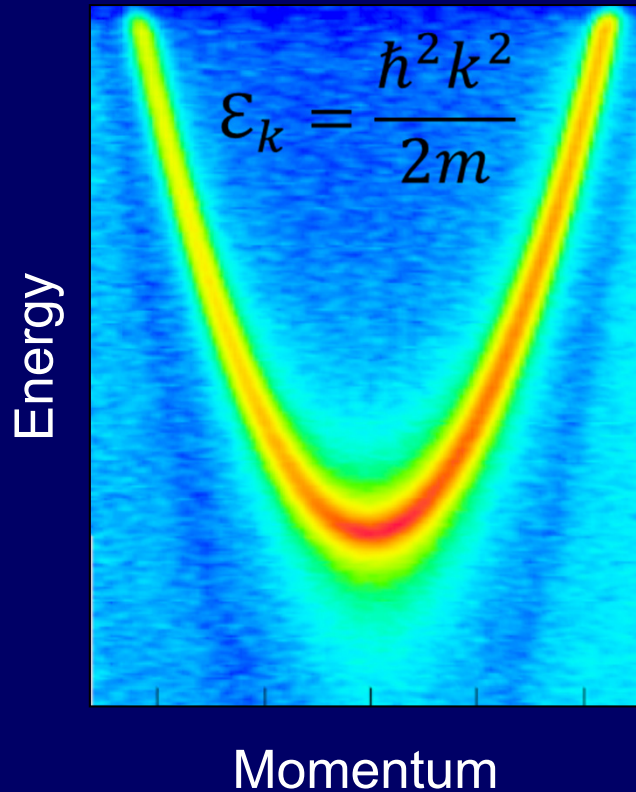
# Band Velocity

$$v_k = \frac{1}{\hbar} \frac{\partial \epsilon_k}{\partial k}$$

# Band Mass

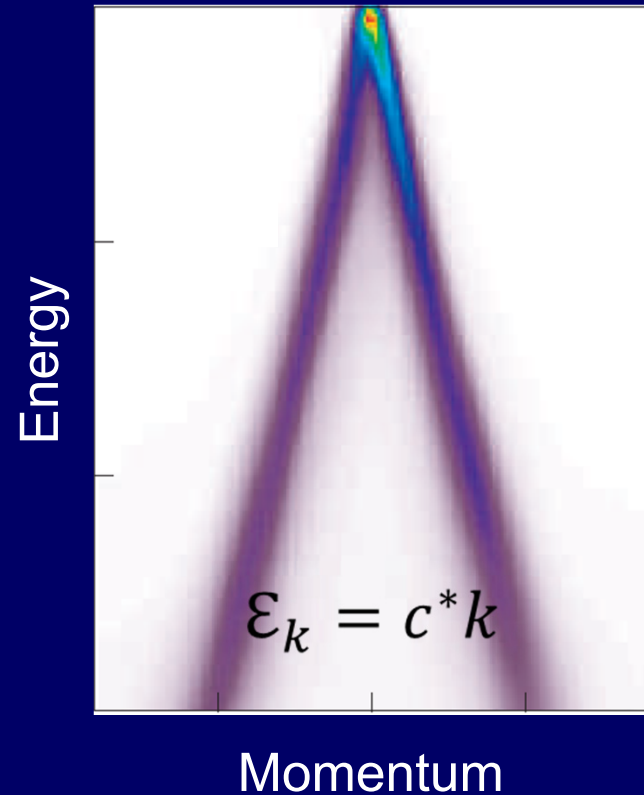
$$\frac{1}{m_k} = \frac{1}{\hbar^2} \frac{\partial^2 \epsilon_k}{\partial k^2}$$

## Cu surface state



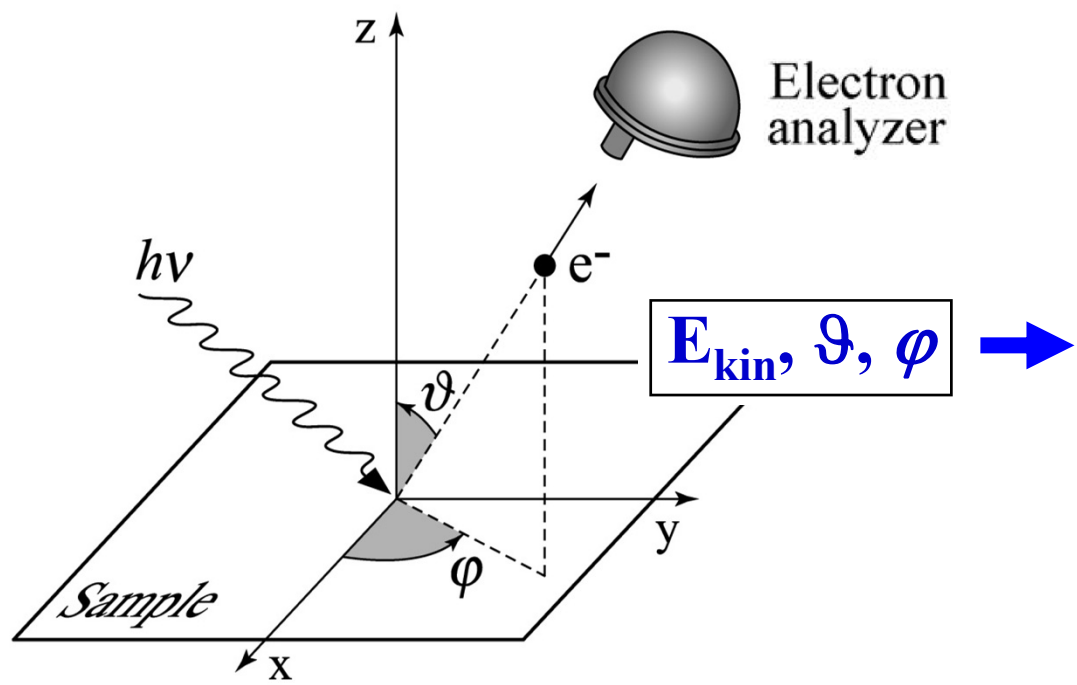
Reinert & Hufner, NJP 2005

## Graphene



Zhou et al., Nat. Phys. 2006

# Angle-Resolved Photoemission Spectroscopy



$$\mathbf{K} = \mathbf{p} / \hbar = \sqrt{2mE_{kin}} / \hbar$$

$$K_x = \frac{1}{\hbar} \sqrt{2mE_{kin}} \sin \vartheta \cos \varphi$$

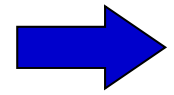
$$K_y = \frac{1}{\hbar} \sqrt{2mE_{kin}} \sin \vartheta \sin \varphi$$

$$K_z = \frac{1}{\hbar} \sqrt{2mE_{kin}} \cos \vartheta$$

Vacuum

$$E_{kin}$$

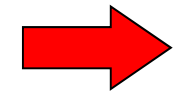
$$\mathbf{K}$$



Conservation laws

$$E_f - E_i = h\nu$$

$$\mathbf{k}_f - \mathbf{k}_i = \cancel{\mathbf{k}_{h\nu}}$$



Solid

$$E_B$$

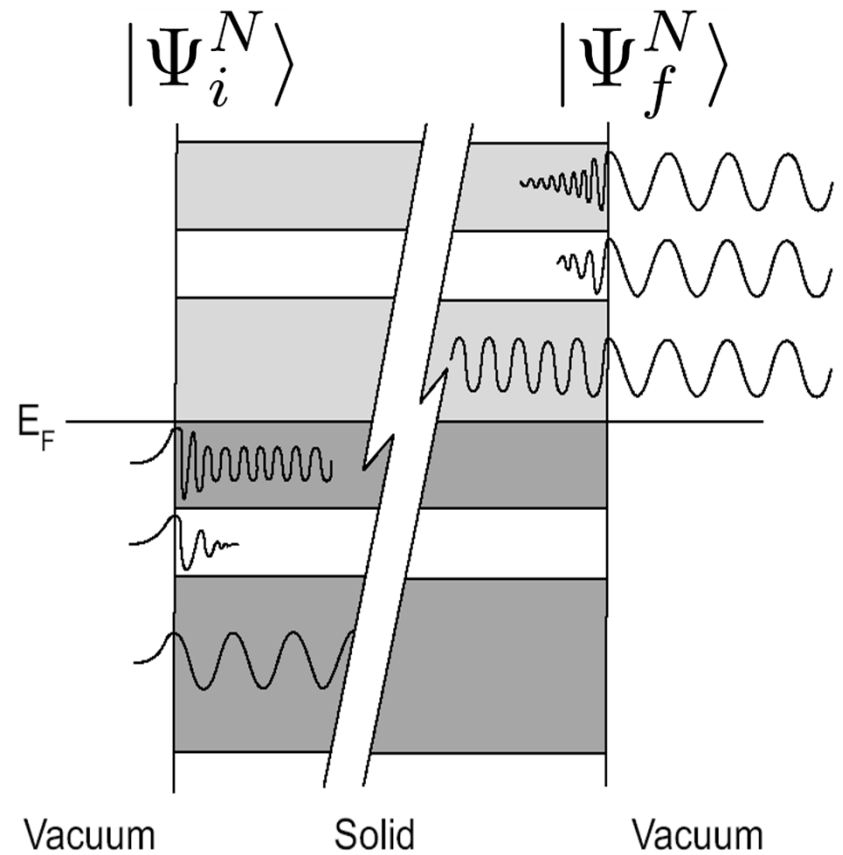
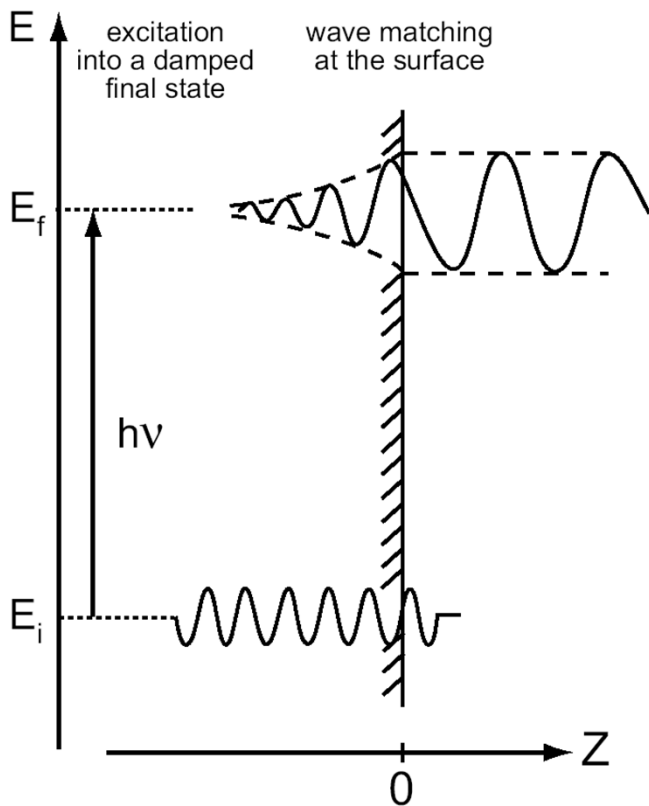
$$\mathbf{k}$$



# ARPES: One-Step vs Three-Step Model

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(k, \omega) \end{array} \right\} w_{fi} \propto |\langle \Psi_f^N | \mathbf{A} \cdot \mathbf{p} | \Psi_i^N \rangle|^2 \delta(E_f^N - E_i^N - h\nu)$$

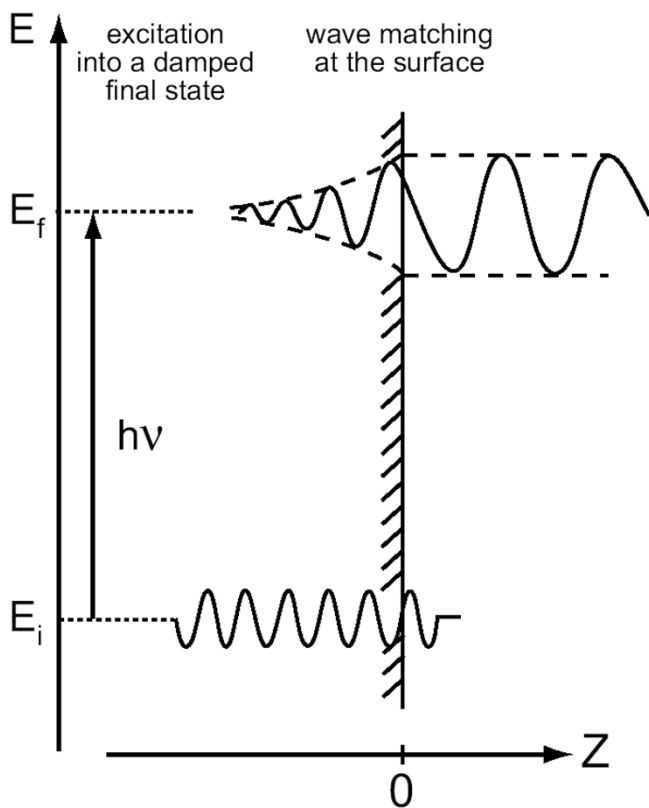
## One-step model



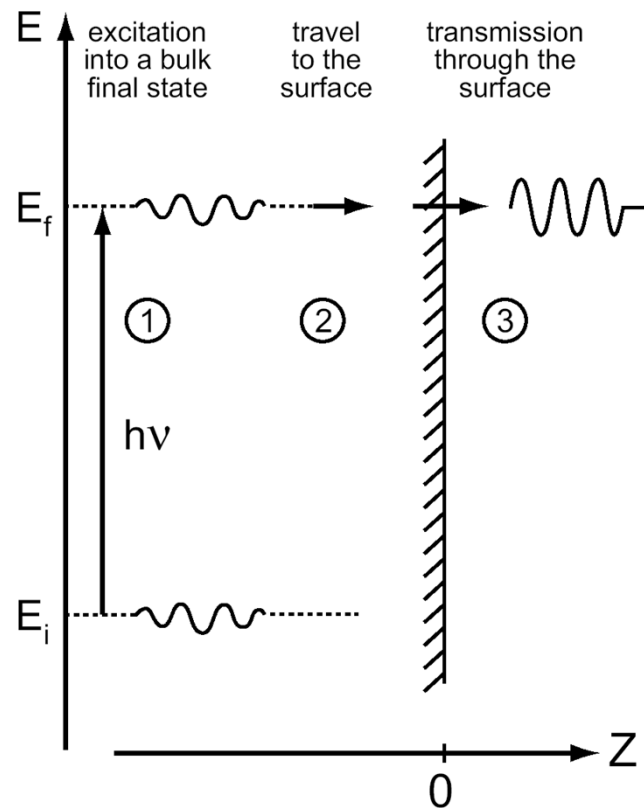
# ARPES: One-Step vs Three-Step Model

Photoemission Intensity  $I(k, \omega)$  }  $w_{fi} \propto |\langle \Psi_f^N | \mathbf{A} \cdot \mathbf{p} | \Psi_i^N \rangle|^2 \delta(E_f^N - E_i^N - h\nu)$

## One-step model



## Three-step model



# ARPES: The Sudden Approximation

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(\mathbf{k}, \omega) \end{array} \right\} w_{fi} \propto |\langle \Psi_f^N | \mathbf{A} \cdot \mathbf{p} | \Psi_i^N \rangle|^2 \delta(E_f^N - E_i^N - h\nu)$$

---

$$\left. \begin{array}{l} \text{Sudden approximation} \\ \text{One Slater determinant} \end{array} \right\} \begin{array}{l} \Psi_f^N = \mathcal{A} \phi_f^{\mathbf{k}} \Psi_f^{N-1} \\ \Psi_i^N = \mathcal{A} \phi_i^{\mathbf{k}} \Psi_i^{N-1} \end{array}$$

# ARPES: The Sudden Approximation

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(\mathbf{k}, \omega) \end{array} \right\} w_{fi} \propto |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2 \delta(\omega - h\nu)$$

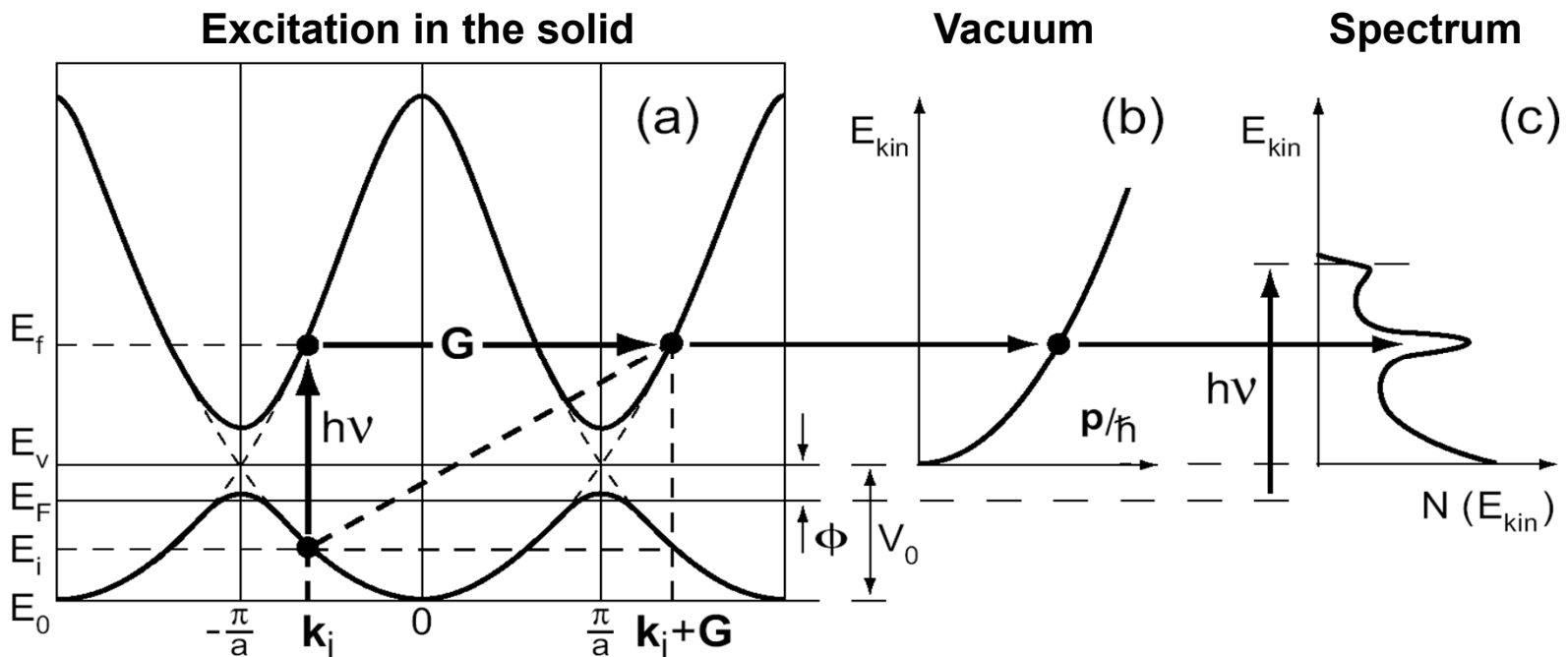
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$$\left. \begin{array}{l} \text{Sudden approximation} \\ \text{One Slater determinant} \end{array} \right\} \begin{array}{l} \Psi_f^N = \mathcal{A} \phi_f^{\mathbf{k}} \Psi_f^{N-1} \\ \Psi_i^N = \mathcal{A} \phi_i^{\mathbf{k}} \Psi_i^{N-1} \end{array}$$

# ARPES: The Sudden Approximation

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(\mathbf{k}, \omega) \end{array} \right\} w_{fi} \propto |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2 \delta(\omega - h\nu)$$

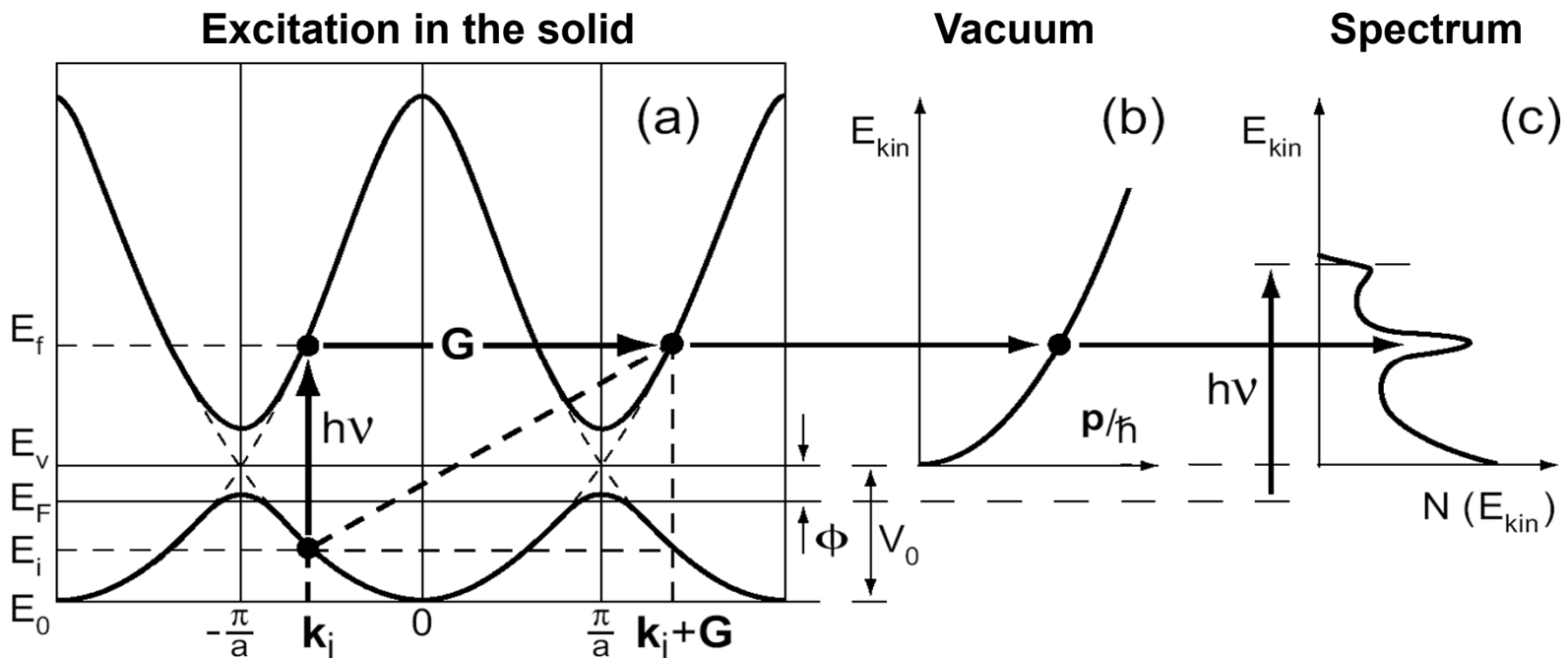
$$\left. \begin{array}{l} \text{Sudden approximation} \\ \text{One Slater determinant} \end{array} \right\} \begin{array}{l} \Psi_f^N = \mathcal{A} \phi_f^{\mathbf{k}} \Psi_f^{N-1} \\ \Psi_i^N = \mathcal{A} \phi_i^{\mathbf{k}} \Psi_i^{N-1} \end{array}$$



# ARPES: Role of the Crystal Potential

Photoemission Intensity  $I(\mathbf{k}, \omega)$  }  $w_{fi} \propto |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \nabla V | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2 \delta(\omega - h\nu)$

**Sudden approximation** }  $\Psi_f^N = \mathcal{A} \phi_f^{\mathbf{k}} \Psi_f^{N-1}$   
**One Slater determinant** }  $\Psi_i^N = \mathcal{A} \phi_i^{\mathbf{k}} \Psi_i^{N-1}$



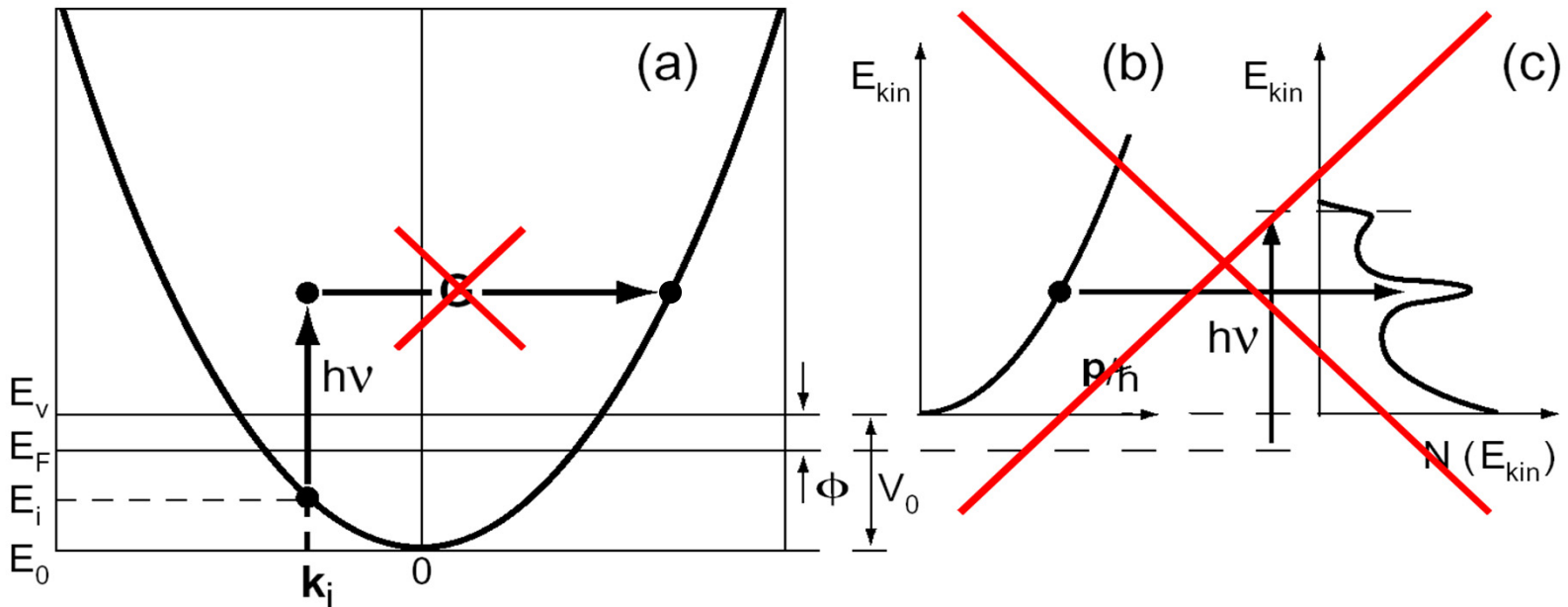
# ARPES: Role of the Crystal Potential

Photoemission Intensity  $I(k, \omega)$  }  $w_{fi} \propto |\langle \phi_f^{\mathbf{k}} | \underline{\mathbf{A}} \cdot \nabla V | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2 \delta(\omega - h\nu)$

**Sudden approximation**  
**One Slater determinant**

$$\Psi_f^N = \mathcal{A} \phi_f^{\mathbf{k}} \Psi_f^{N-1}$$

$$\Psi_i^N = \mathcal{A} \phi_i^{\mathbf{k}} \Psi_i^{N-1}$$



# ARPES: Role of the Crystal Potential

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(\mathbf{k}, \omega) \end{array} \right\} w_{fi} \propto \left| \langle \phi_f^{\mathbf{k}} | \underline{\mathbf{A}} \cdot \nabla V | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle \right|^2 \delta(\omega - h\nu)$$

---

*“In a nearly-free electron gas, optical absorption may be viewed as a two-step process. The absorption of the photon provides the electron with the additional energy it needs to get to the excited state. The crystal potential imparts to the electron the additional momentum it needs to reach the excited state. This momentum comes in multiples of the reciprocal-lattice vectors  $\mathbf{G}$ : So in a reduced zone picture, the transitions are vertical in wave-vector space. But in photoemission, it is more useful to think in an extended-zone scheme.”*

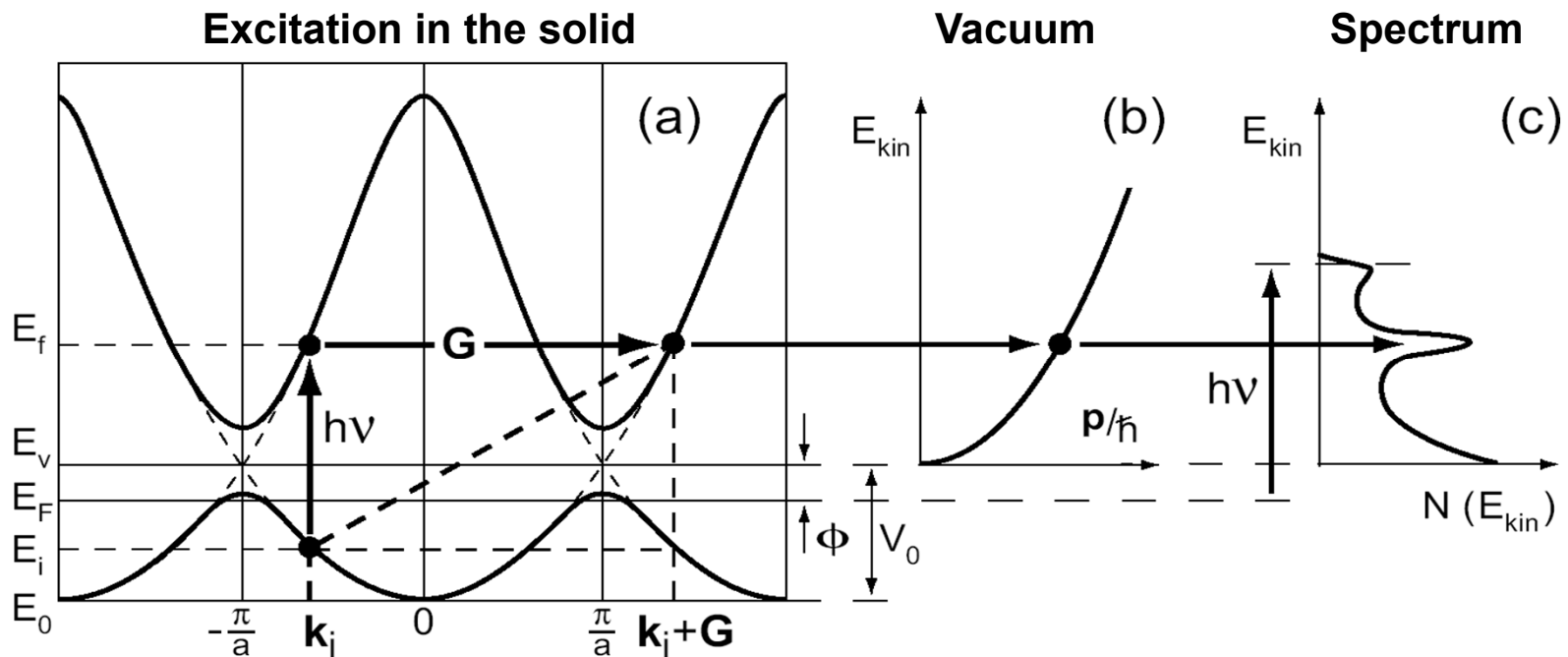
G.D. Mahan, Phys. Rev. B **2**, 4334 (1970)



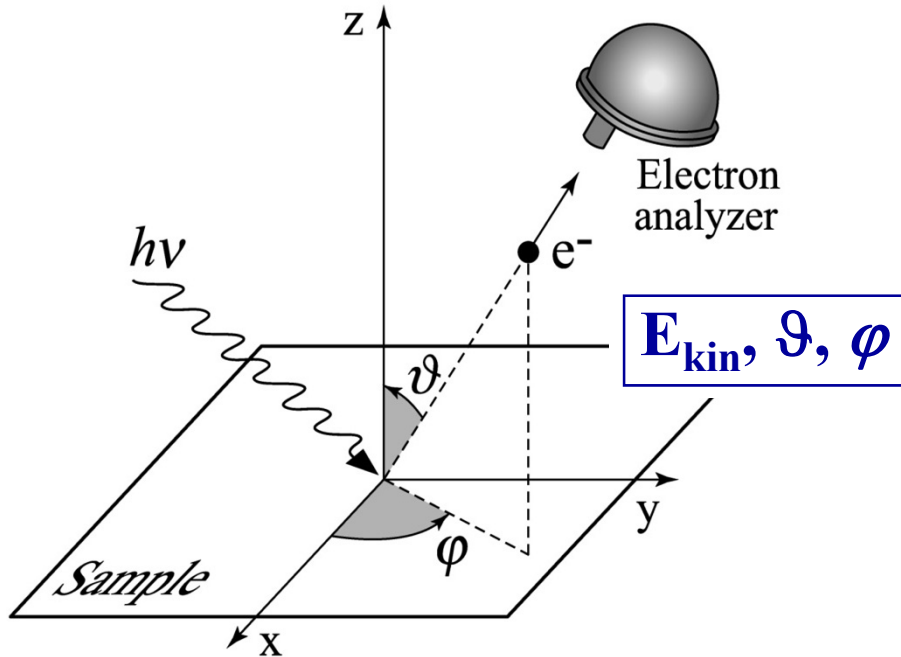
# ARPES: Three-step Model & Sudden Approximation

$$\left. \begin{array}{l} \text{Photoemission} \\ \text{Intensity } I(\mathbf{k}, \omega) \end{array} \right\} w_{fi} \propto \left| \langle \phi_f^{\mathbf{k}} | \underline{\mathbf{A}} \cdot \nabla V | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle \right|^2 \delta(\omega - h\nu)$$

The photoemission intensity for the SAME band is very DIFFERENT in various Brillouin zones



# ARPES: Energetics and Kinematics

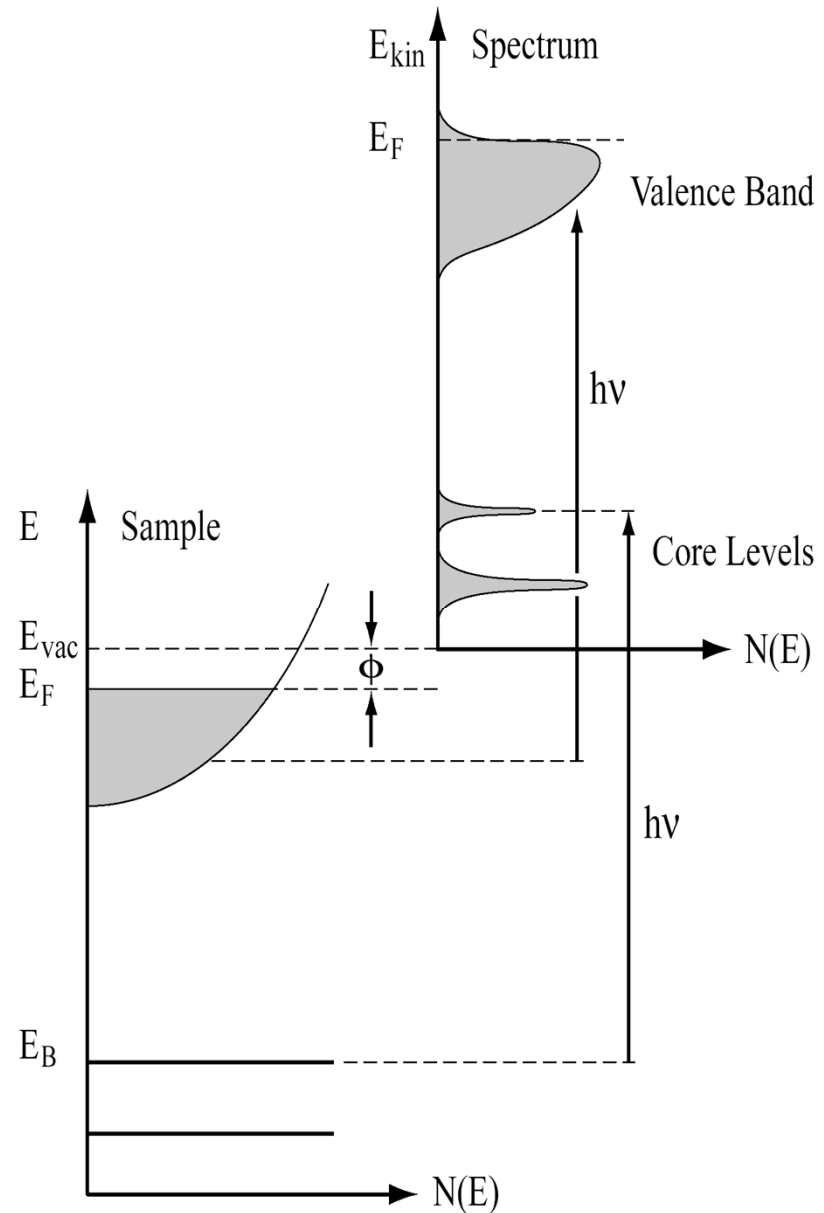


Energy Conservation

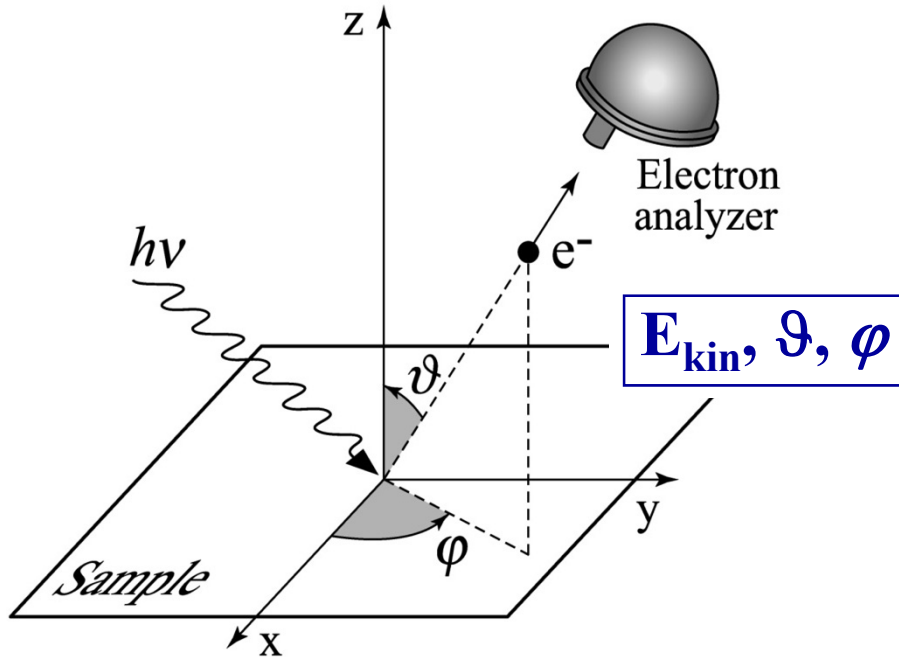
$$E_{kin} = h\nu - \phi - |E_B|$$

Momentum Conservation

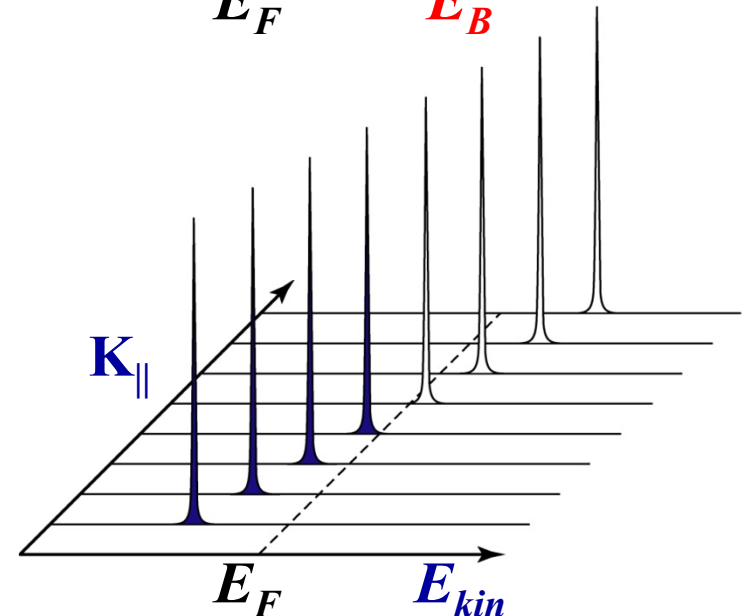
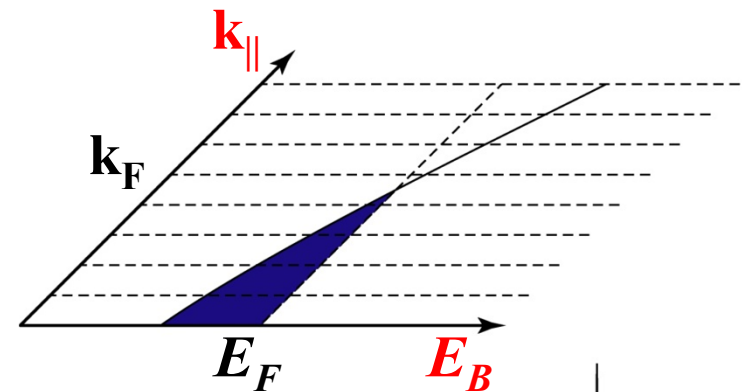
$$\hbar \mathbf{k}_{||} = \hbar \mathbf{K}_{||} = \sqrt{2m E_{kin}} \cdot \sin \theta$$



# ARPES: Energetics and Kinematics



## Electrons in Reciprocal Space



Energy Conservation

$$E_{kin} = h\nu - \phi - |E_B|$$

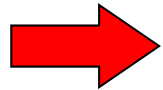
Momentum Conservation

$$\hbar \mathbf{k}_{\parallel} = \hbar \mathbf{K}_{\parallel} = \sqrt{2m E_{kin}} \cdot \sin \theta$$

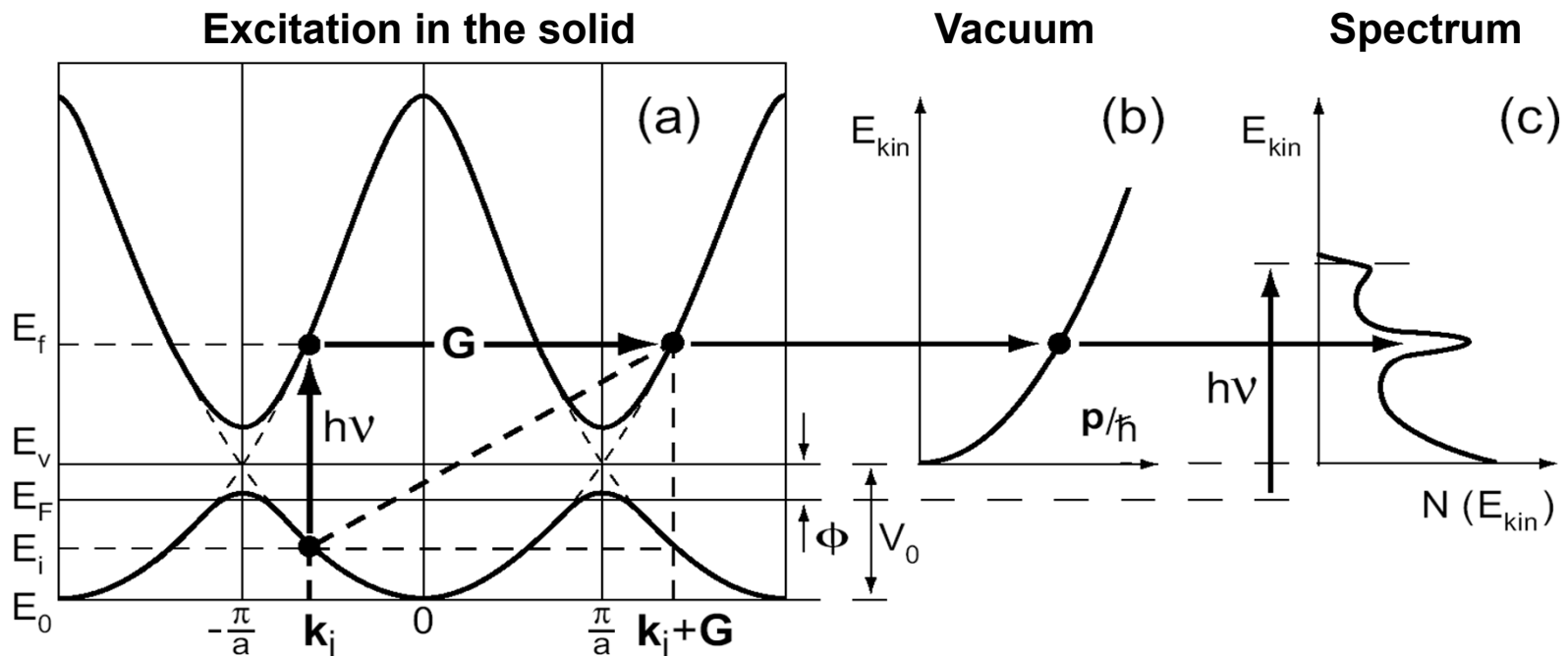
# ARPES in 3D: Inner Potential and Determination of $k_z$

**Free-electron final state**  $E_f(\mathbf{k}) = \frac{\hbar^2 \mathbf{k}^2}{2m} - |E_0| = \frac{\hbar^2 (\mathbf{k}_{\parallel}^2 + \mathbf{k}_{\perp}^2)}{2m} - |E_0|$

**because**  $\frac{\hbar^2 \mathbf{k}_{\parallel}^2}{2m} = E_{kin} \sin^2 \vartheta$   $E_f = E_{kin} + \phi$   $V_0 = |E_0| + \phi$

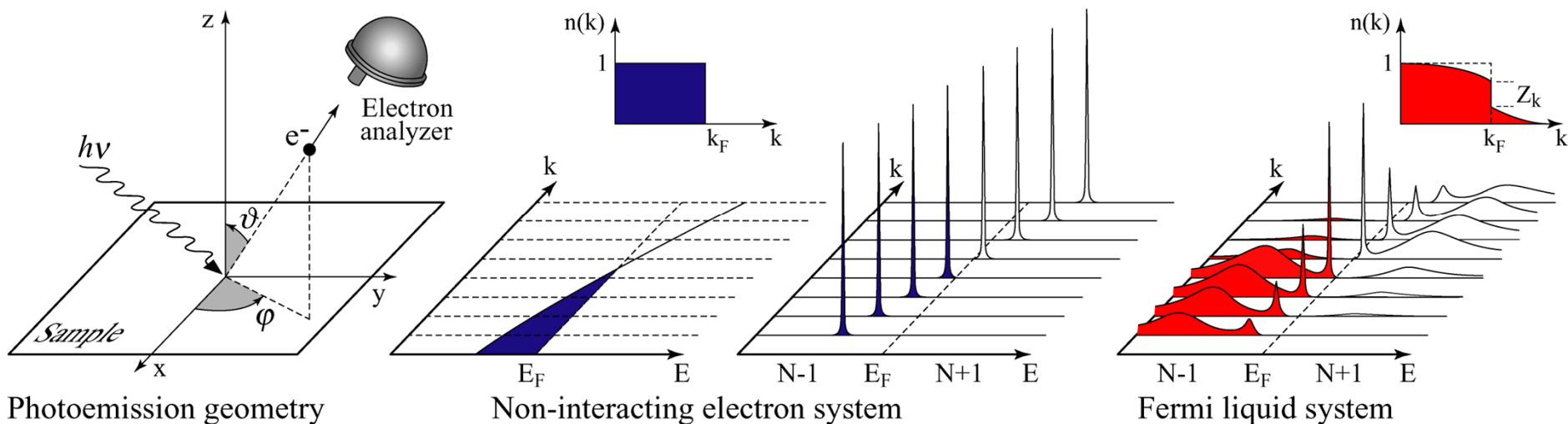


$$\mathbf{k}_{\perp} = \frac{1}{\hbar} \sqrt{2m(E_{kin} \cos^2 \vartheta + V_0)}$$



# ARPES: Interacting Systems

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



**Photoemission intensity:**  $I(\mathbf{k}, E_{kin}) = \sum_{f,i} w_{f,i}$

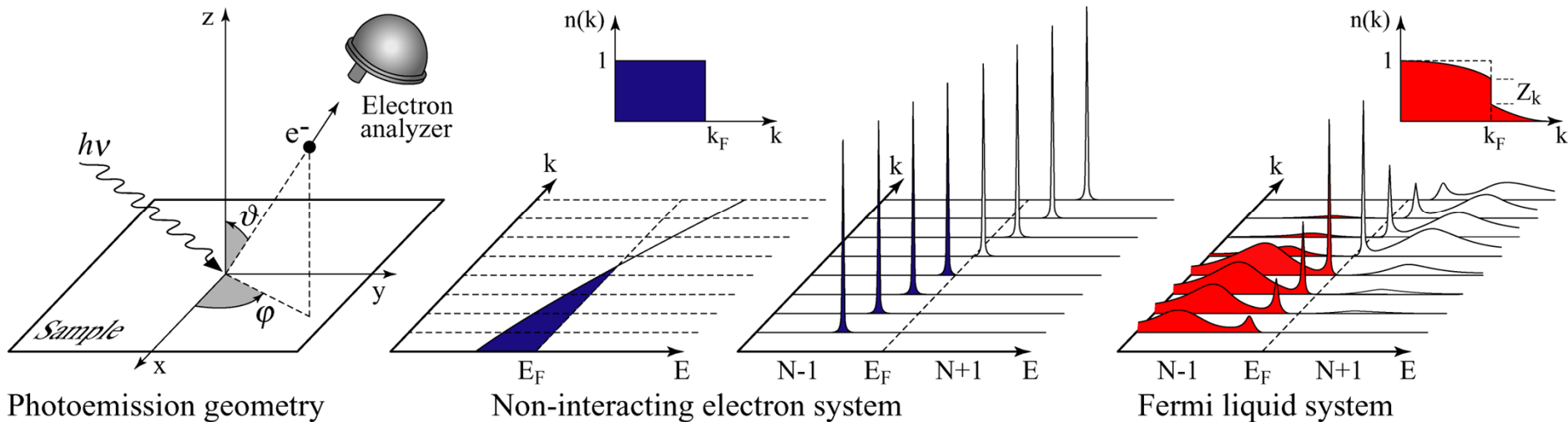
$$I(\mathbf{k}, E_{kin}) \propto \sum_{f,i} |M_{f,i}^{\mathbf{k}}|^2 \sum_m |c_{m,i}|^2 \delta(E_{kin} + E_m^{N-1} - E_i^N - h\nu)$$

$$|M_{f,i}^{\mathbf{k}}|^2 \equiv |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle|^2 \quad |c_{m,i}|^2 = |\langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2$$

**In general**  $\Psi_i^{N-1} = c_{\mathbf{k}} \Psi_i^N$  **NOT orthogonal**  $\Psi_m^{N-1}$

# ARPES: Interacting Systems

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



**Photoemission intensity:**  $I(\mathbf{k}, E_{kin}) = \sum_{f,i} w_{f,i}$

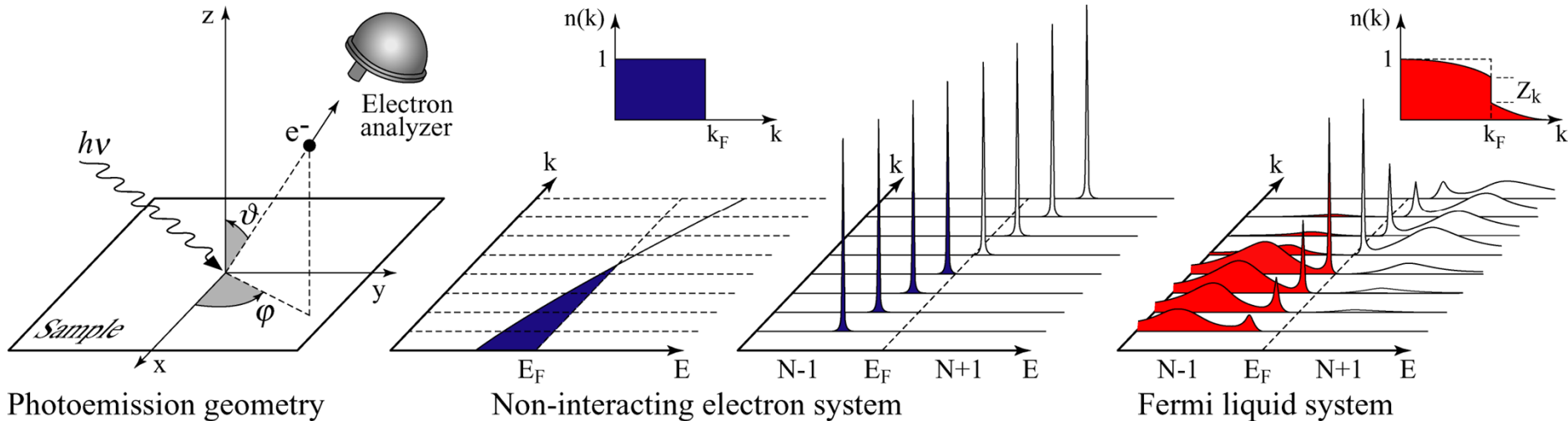
$$I(\mathbf{k}, E_{kin}) \propto \sum_{f,i} |M_{f,i}^{\mathbf{k}}|^2 \sum_m |c_{m,i}|^2 \delta(E_{kin} + E_m^{N-1} - E_i^N - h\nu)$$

$$|M_{f,i}^{\mathbf{k}}|^2 \equiv |\langle \phi_f^{\mathbf{k}} | \mathbf{A} \cdot \mathbf{p} | \phi_i^{\mathbf{k}} \rangle|^2 \quad |c_{m,i}|^2 = |\langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle|^2$$

**“Like removing a stone from a water bucket”**

# ARPES: Fermi Liquid Description

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



**Photoemission intensity:**  $I(\mathbf{k}, \omega) = I_0 |M(\mathbf{k}, \omega)|^2 f(\omega) A(\mathbf{k}, \omega)$

**Non-interacting**

$$A(\mathbf{k}, \omega) = \delta(\omega - \epsilon_{\mathbf{k}})$$

No Renormalization  
Infinite lifetime

**Fermi Liquid**

$$A(\mathbf{k}, \omega) = Z_{\mathbf{k}} \frac{\Gamma_{\mathbf{k}}/\pi}{(\omega - \epsilon_{\mathbf{k}})^2 + \Gamma_{\mathbf{k}}^2} + A_{inc}$$

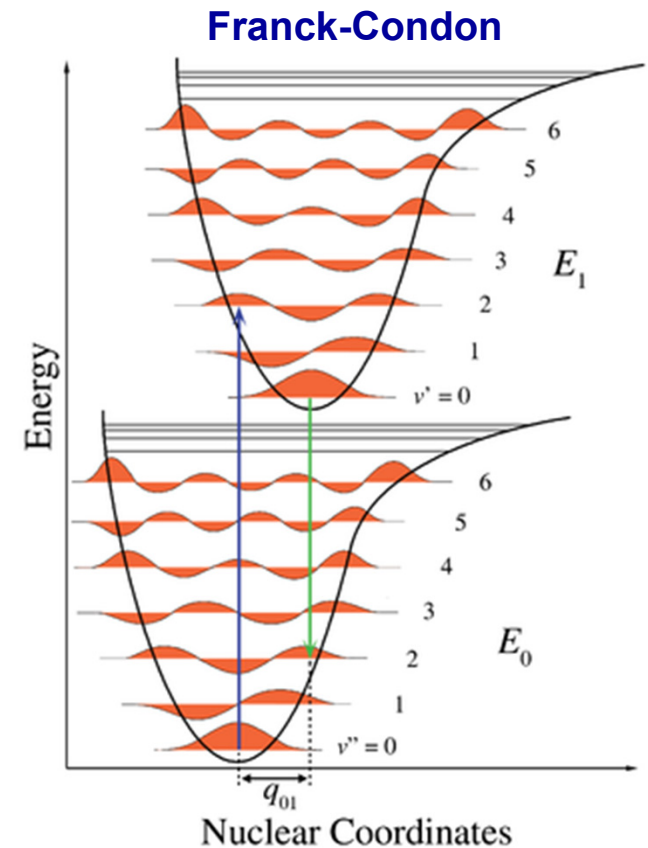
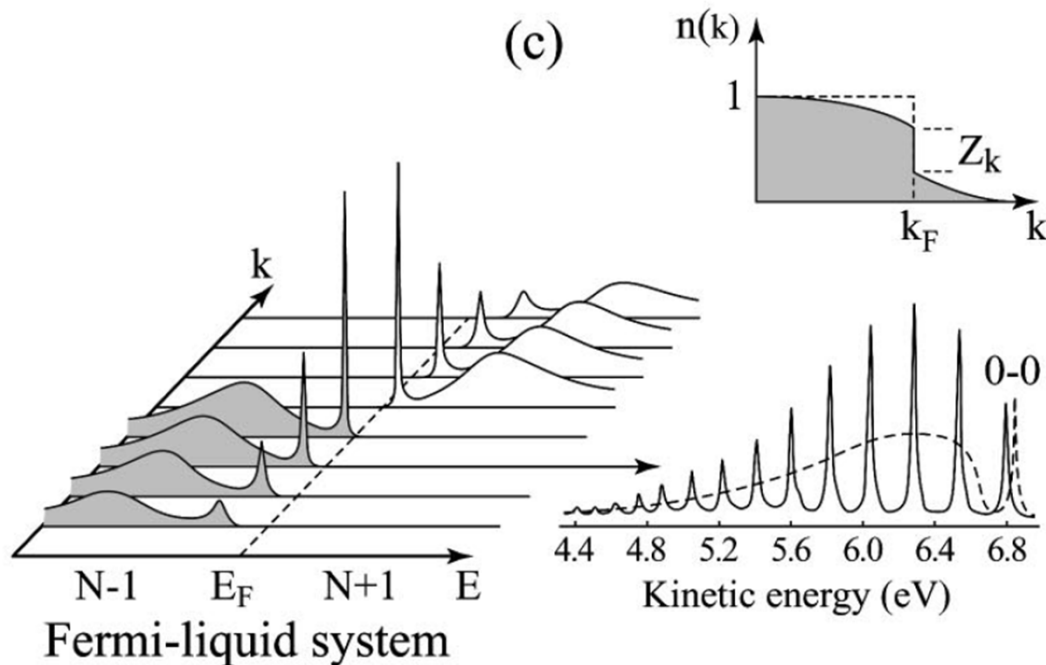
$$m^* > m \quad |\epsilon_{\mathbf{k}}| < |\epsilon_{\mathbf{k}}|$$

$$\tau_{\mathbf{k}} = 1/\Gamma_{\mathbf{k}}$$

$\Sigma(\mathbf{k}, \omega)$  : the “self-energy” captures the effects of interactions

# Testing Fermi-liquid models

G.A. Sawatzky

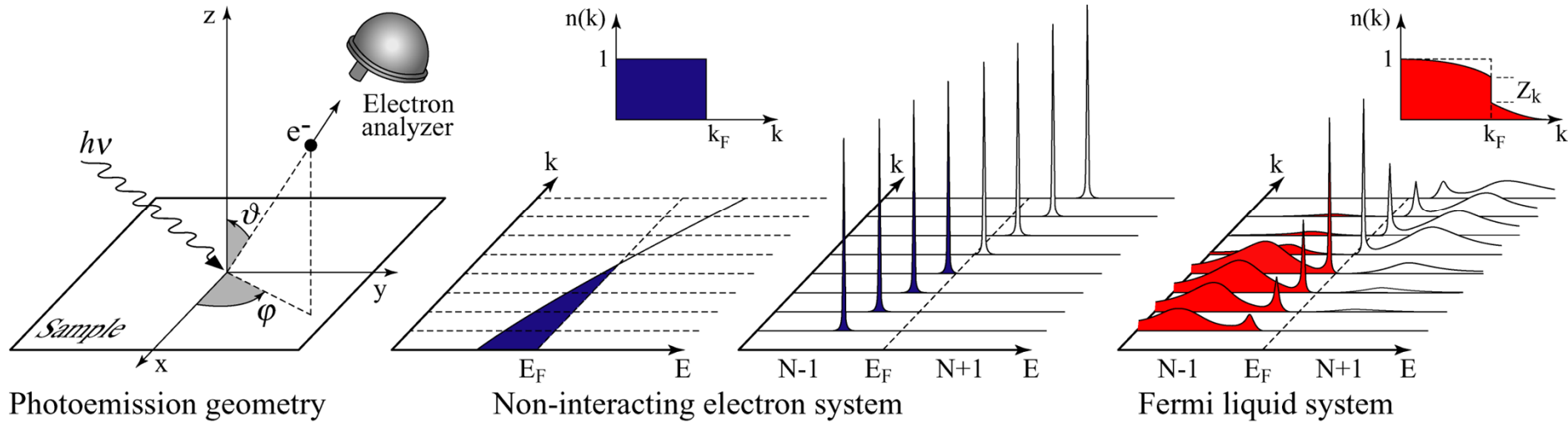


“In gaseous hydrogen, the equilibrium bond length is dependent on the degree of occupation of that level. The electrons are dressed by interatomic displacements. The intensities are given by the Franck-Condon factors, the molecular equivalent of the sudden approximation. The ARPES spectrum of solid hydrogen, developed from the molecular spectrum, will be angle dependent but for some angle will resemble the broken line. The fundamental transition (0-0) becomes the solid state quasiparticle peak. The phonon excitations develop into a broad, incoherent quasicontinuum.”



# ARPES: The One-Particle Spectral Function

A. Damascelli, Z. Hussain, Z.-X Shen, Rev. Mod. Phys. **75**, 473 (2003)



**Photoemission intensity:**  $I(\mathbf{k}, \omega) = I_0 |M(\mathbf{k}, \omega)|^2 f(\omega) A(\mathbf{k}, \omega)$

**Single-particle spectral function**

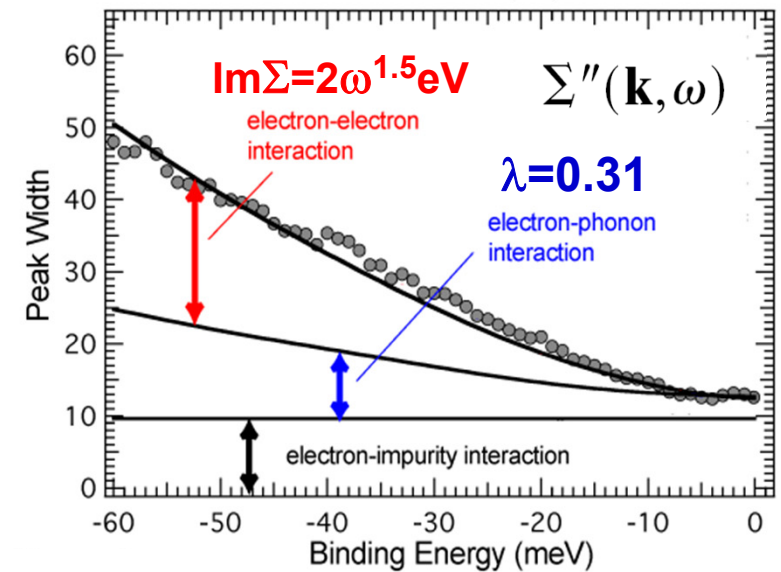
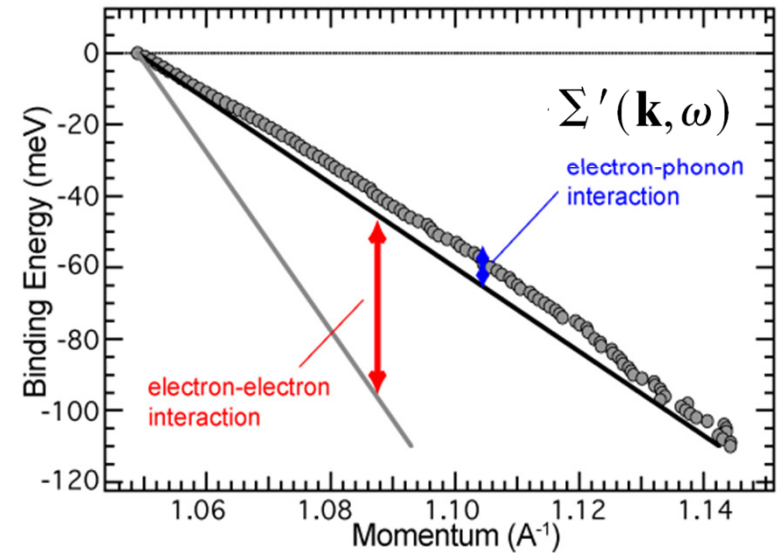
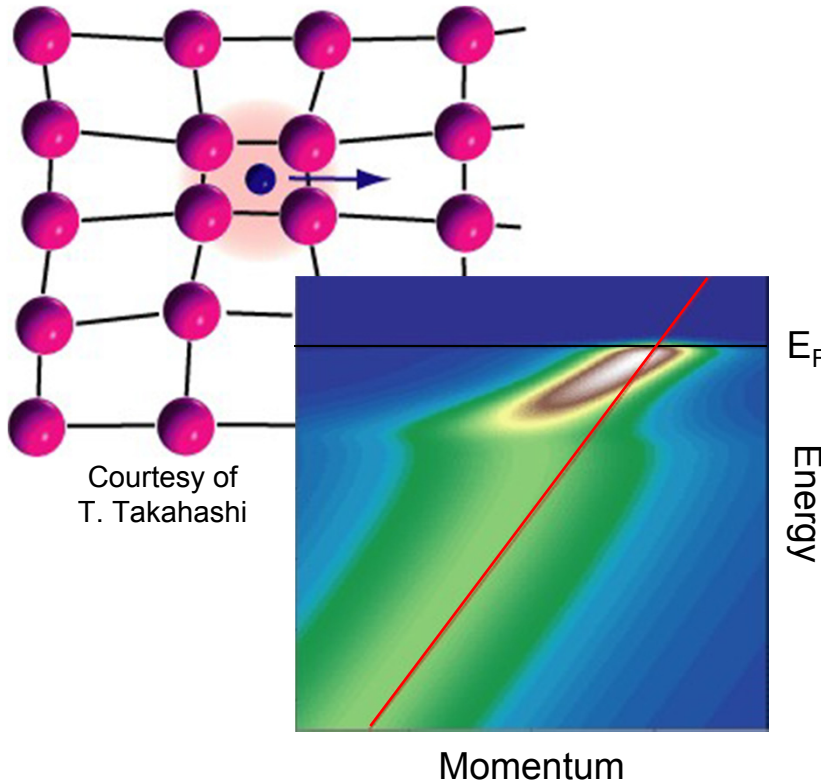
$$A(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\mathbf{k}, \omega)}{[\omega - \epsilon_{\mathbf{k}} - \Sigma'(\mathbf{k}, \omega)]^2 + [\Sigma''(\mathbf{k}, \omega)]^2}$$

$\Sigma(\mathbf{k}, \omega)$  : the “self-energy” captures the effects of interactions

# Many-Body Correlation Effects in $\text{Sr}_2\text{RuO}_4$

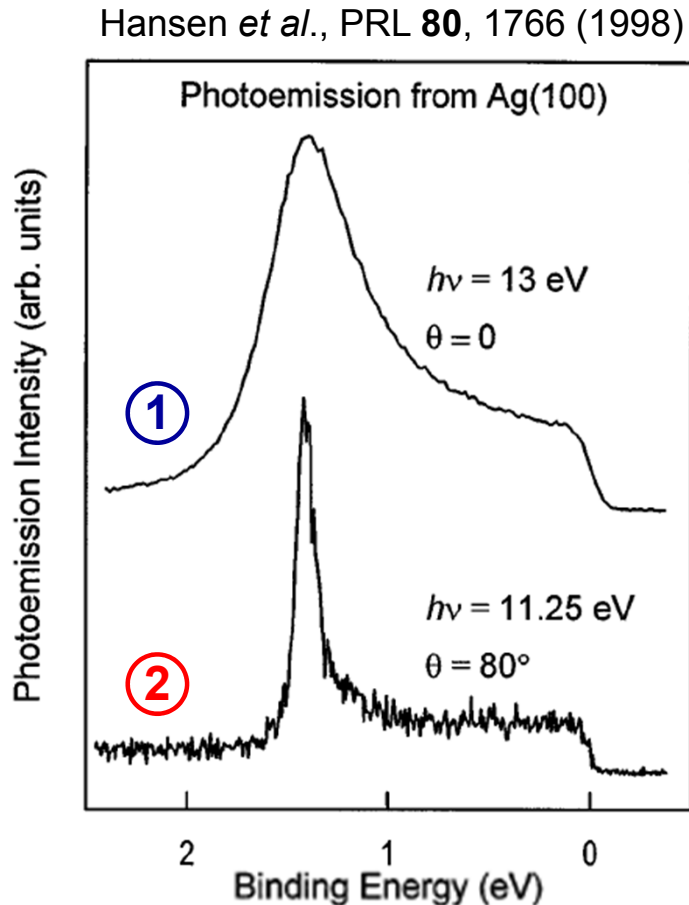
## Single-particle spectral function

$$A(\mathbf{k}, \omega) = -\frac{1}{\pi} \frac{\Sigma''(\mathbf{k}, \omega)}{[\omega - \epsilon_{\mathbf{k}} - \Sigma'(\mathbf{k}, \omega)]^2 + [\Sigma''(\mathbf{k}, \omega)]^2}$$



# ARPES: FWHM and Inverse Lifetime in 3D

FWHM of an ARPES peak } 
$$\Gamma = \frac{\frac{\Gamma_i}{|v_{i\perp}|} + \frac{\Gamma_f}{|v_{f\perp}|}}{\left| \frac{1}{v_{i\perp}} \left[ 1 - \frac{mv_{i\parallel} \sin^2 \vartheta}{\hbar k_{\parallel}} \right] - \frac{1}{v_{f\perp}} \left[ 1 - \frac{mv_{f\parallel} \sin^2 \vartheta}{\hbar k_{\parallel}} \right] \right|}$$



① if  $E_i \simeq E_F$

→  $\Gamma_i \longrightarrow 0$  →  $\Gamma \propto \Gamma_f$

② if  $|v_{i\perp}| \simeq 0$

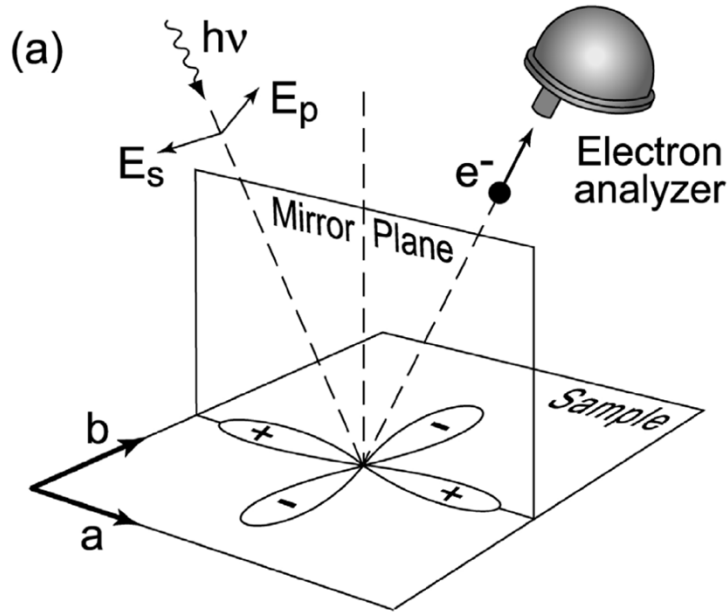
→  $\Gamma = \frac{\Gamma_i}{\left| 1 - \frac{mv_{i\parallel} \sin^2 \vartheta}{\hbar k_{\parallel}} \right|} \equiv C \Gamma_i$

if  $v_{i\parallel} < 0$ , large;  $\theta$  large;  $k_{\parallel}$  small

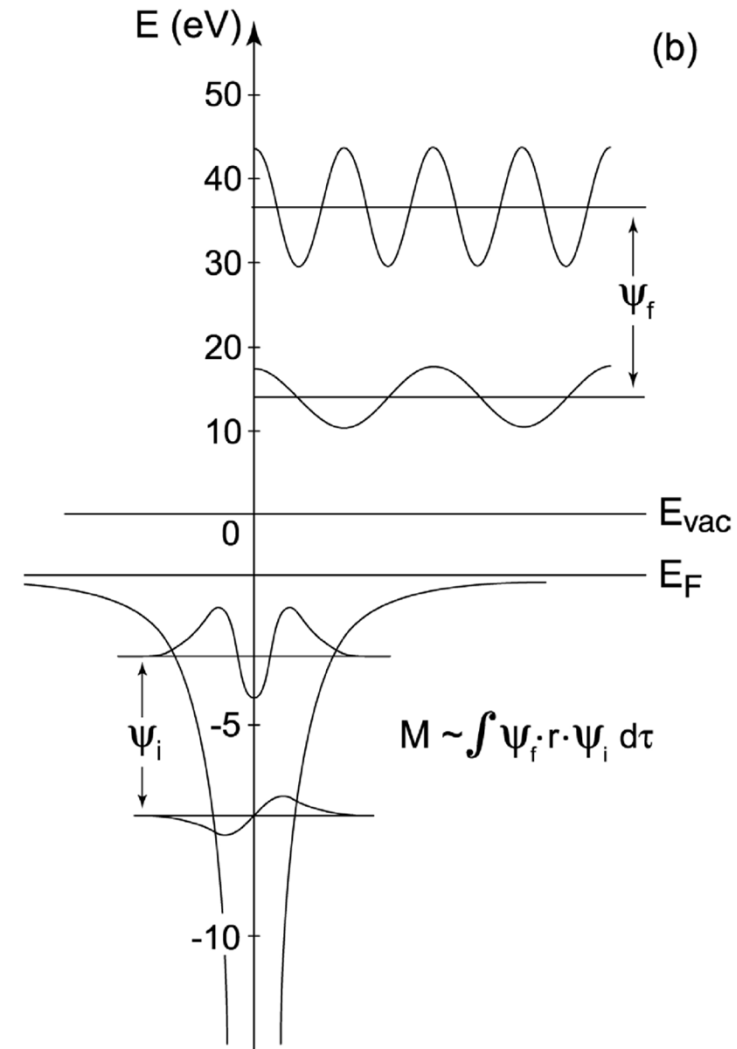
→  $C < 1$ , and  $\Gamma < \Gamma_i$

# ARPES: Matrix Elements Effects (polarization + energy)

## Photon polarization



## Photon energy



$$w_{fi} = \frac{2\pi}{\hbar} |\langle \Psi_f^N | H_{int} | \Psi_i^N \rangle|^2 \delta(E_f^N - E_i^N - h\nu)$$

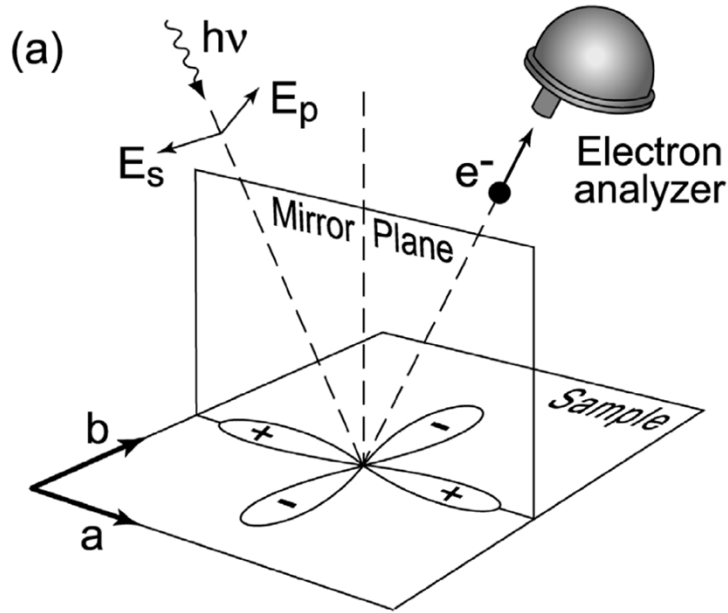
$$\Psi_i^N = \mathcal{A} \phi_i^{\mathbf{k}} \Psi_i^{N-1}$$

$$\Psi_f^N = \mathcal{A} \phi_f^{\mathbf{k}} \Psi_f^{N-1}$$

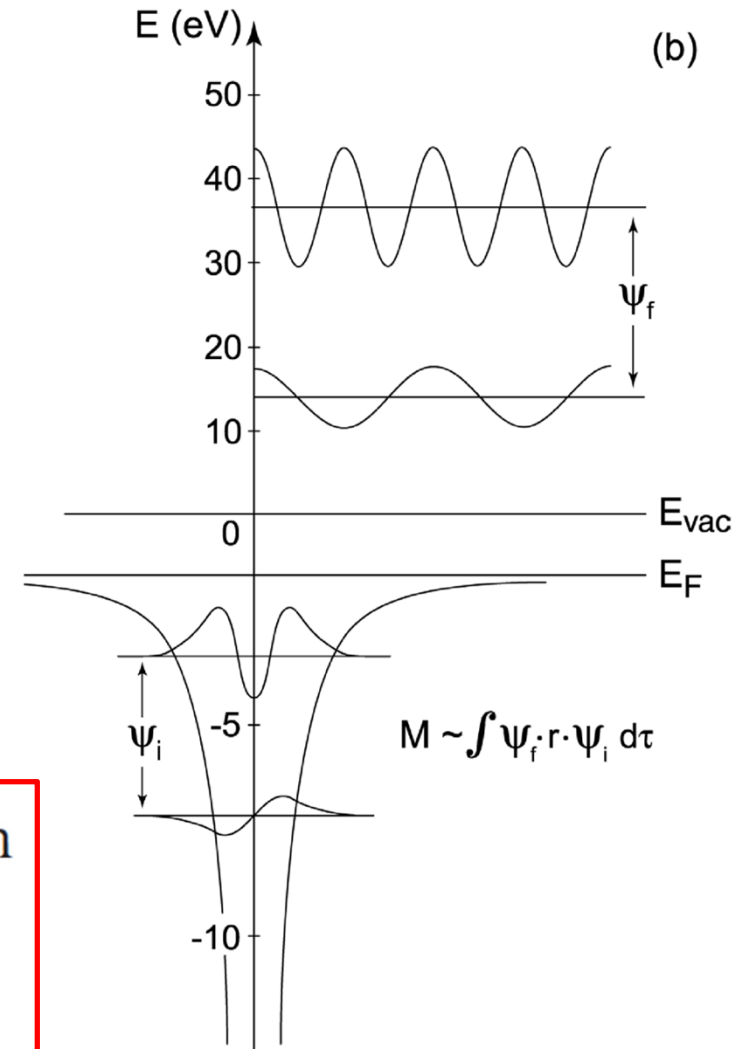
$$\langle \Psi_f^N | H_{int} | \Psi_i^N \rangle = \langle \phi_f^{\mathbf{k}} | H_{int} | \phi_i^{\mathbf{k}} \rangle \langle \Psi_m^{N-1} | \Psi_i^{N-1} \rangle$$

# ARPES: Matrix Elements Effects (polarization + energy)

## Photon polarization



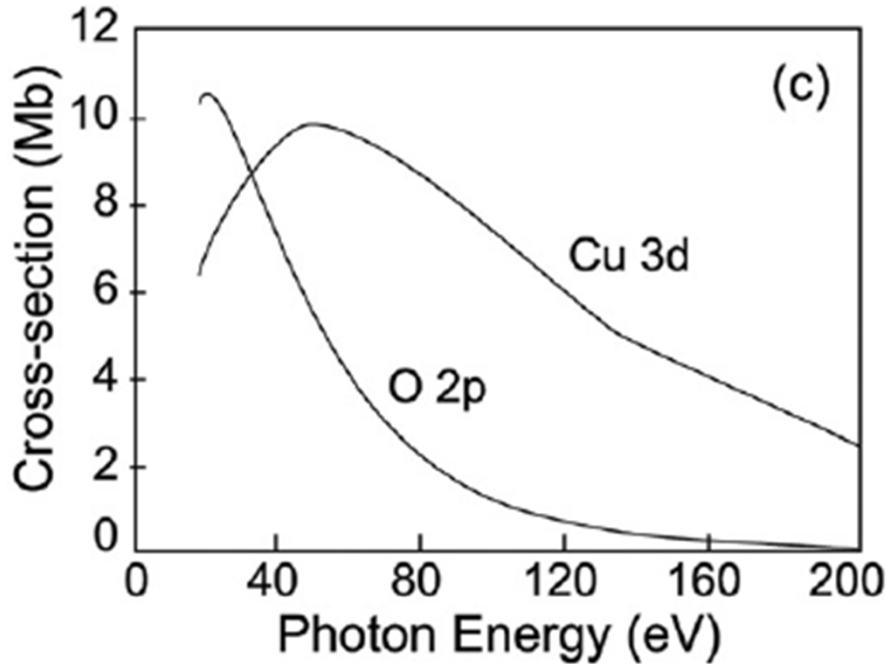
## Photon energy



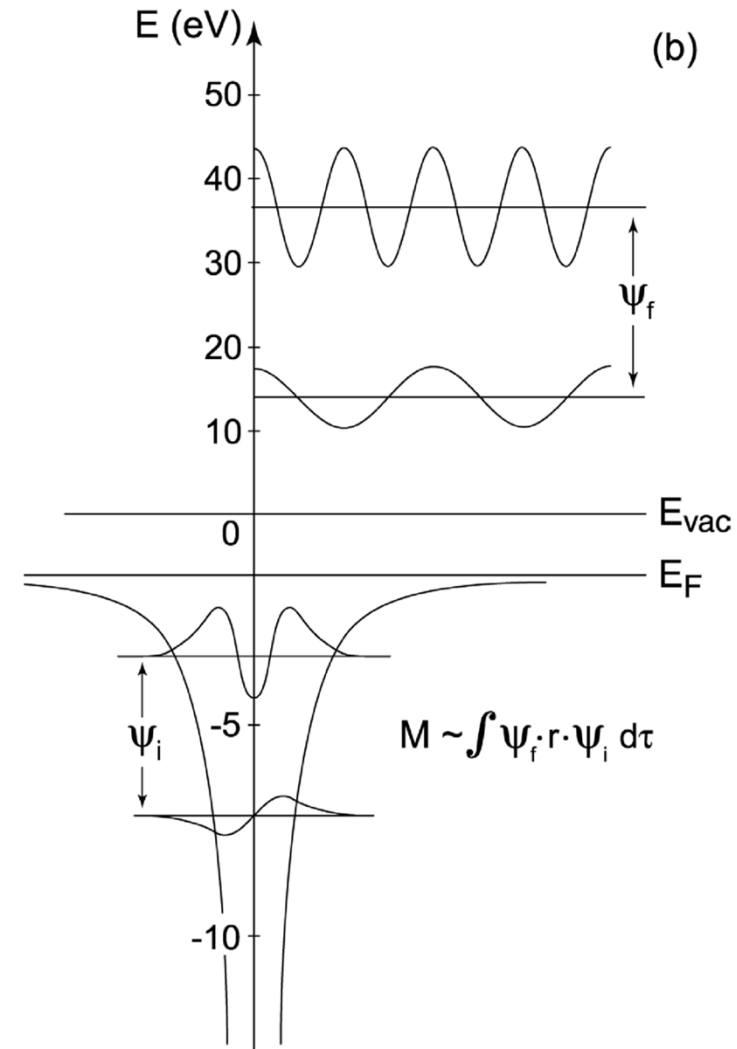
$$\left\langle \phi_f^k | A \cdot p | \phi_i^k \right\rangle \begin{cases} \phi_i^k \text{ even } \langle + | + | + \rangle \Rightarrow A \text{ even} \\ \phi_i^k \text{ odd } \langle + | - | - \rangle \Rightarrow A \text{ odd} \end{cases}$$

# ARPES: Matrix Elements Effects (polarization + energy)

One Cooper minimum in free atoms



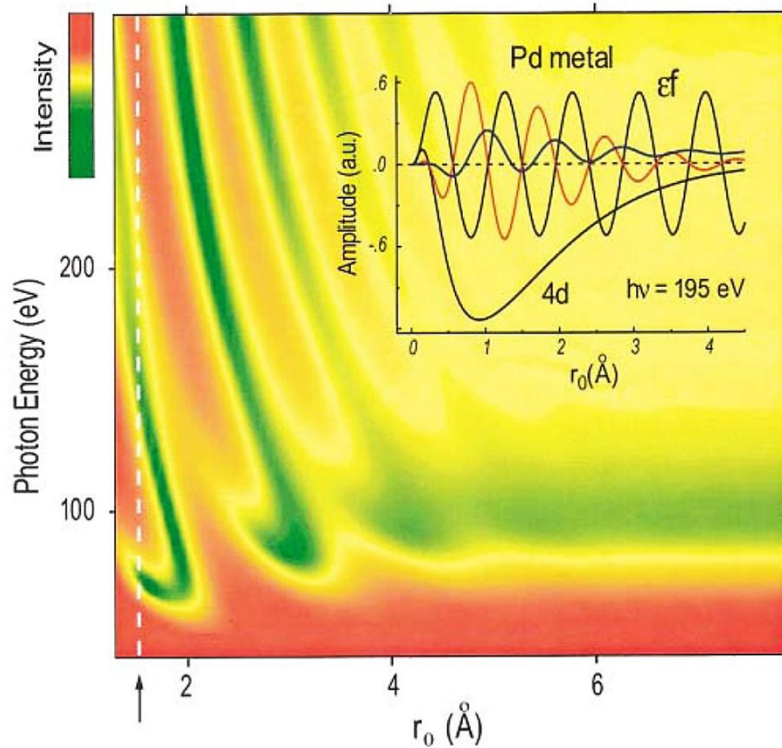
Photon energy



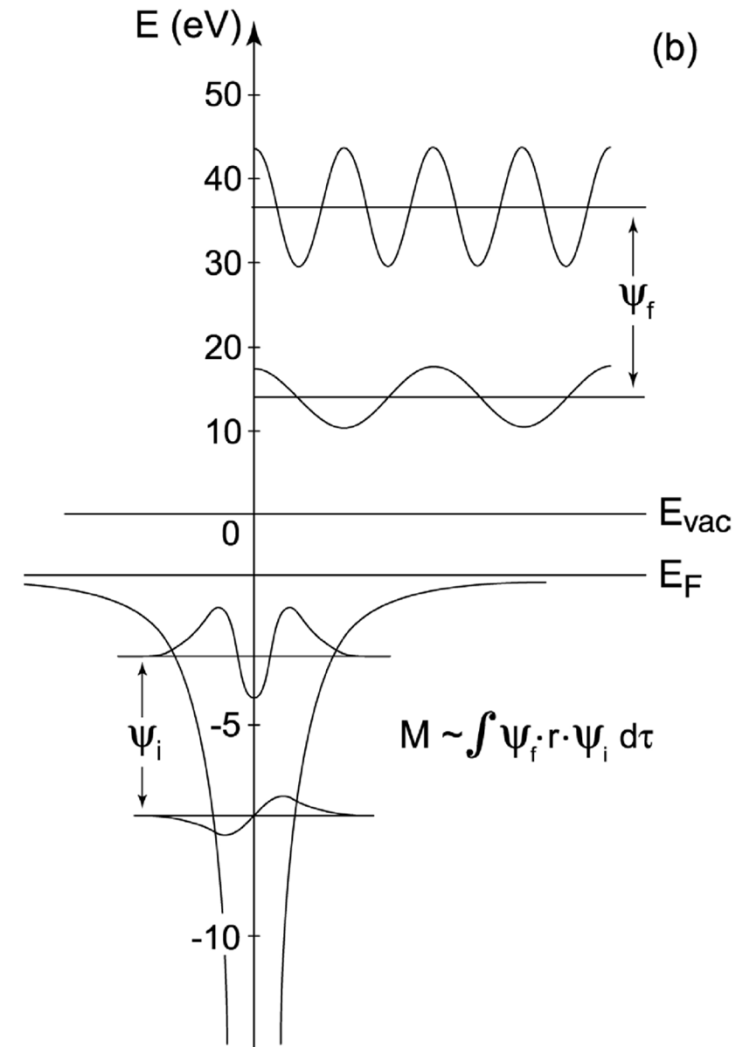
$$\langle \phi_f^k | \mathbf{A} \cdot \mathbf{p} | \phi_i^k \rangle^2 \propto |(\boldsymbol{\varepsilon} \cdot \mathbf{k}) \langle \phi_i^k | e^{i\mathbf{k}r} \rangle|^2$$

# ARPES: Matrix Elements Effects (polarization + energy)

Several Cooper minima in solids



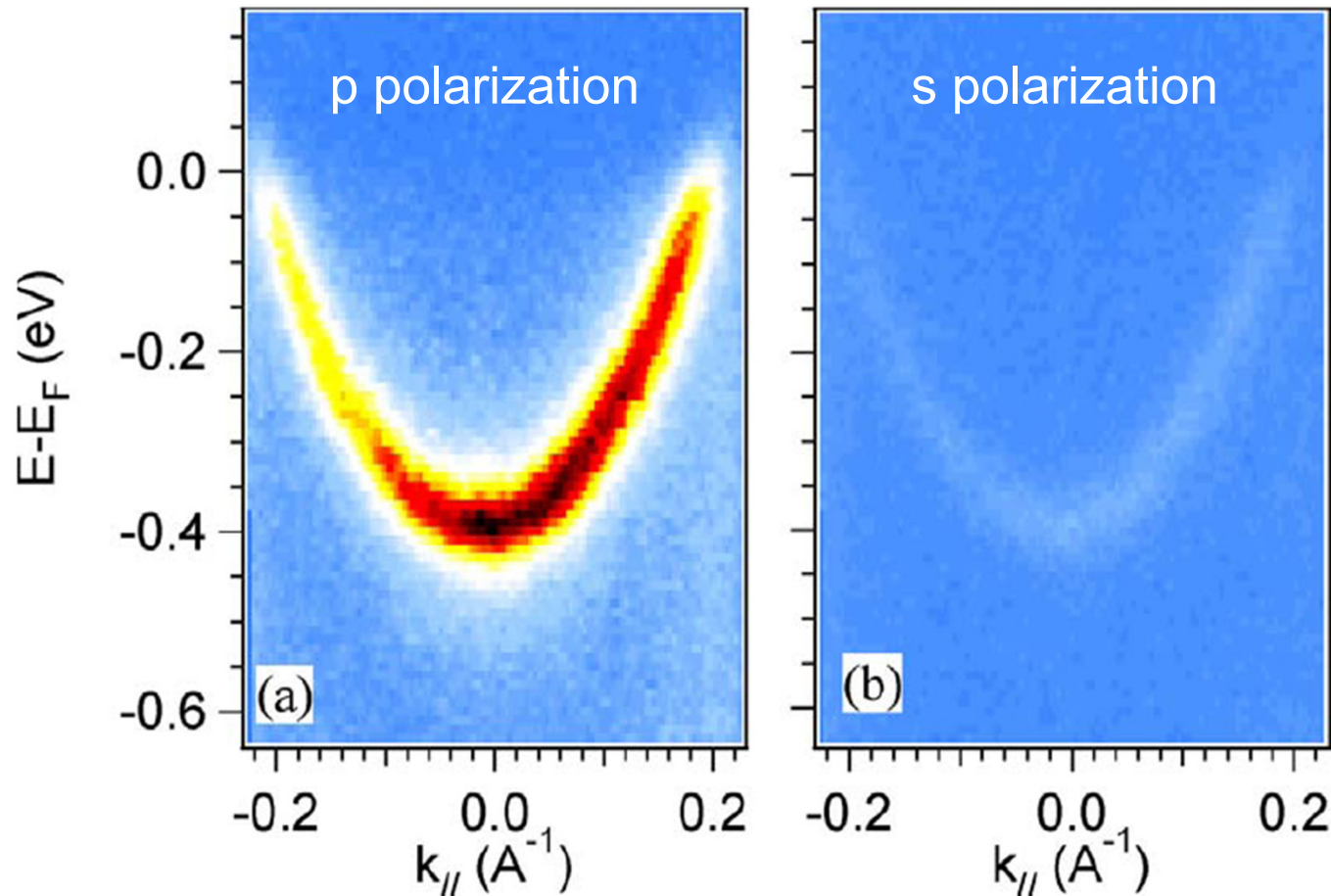
Photon energy



$$\langle \phi_f^k | \mathbf{A} \cdot \mathbf{p} | \phi_i^k \rangle^2 \propto |(\boldsymbol{\varepsilon} \cdot \mathbf{k}) \langle \phi_i^k | e^{i\mathbf{k}r} \rangle|^2$$

# ARPES: Polarization Dependence

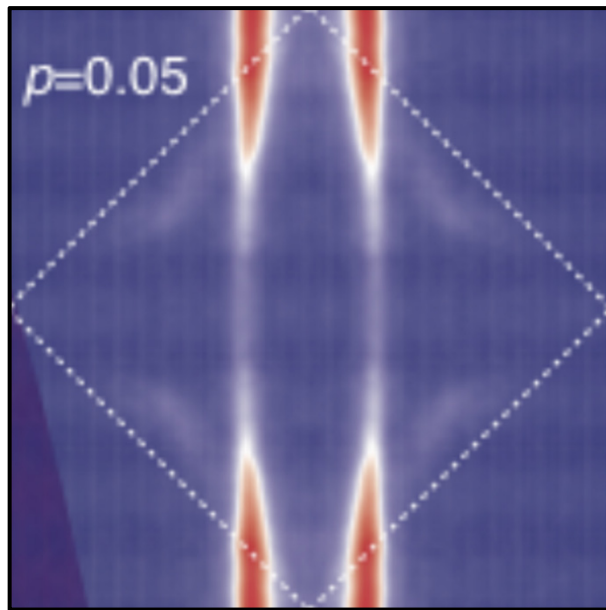
## Dispersion of the Cu(111) surface state



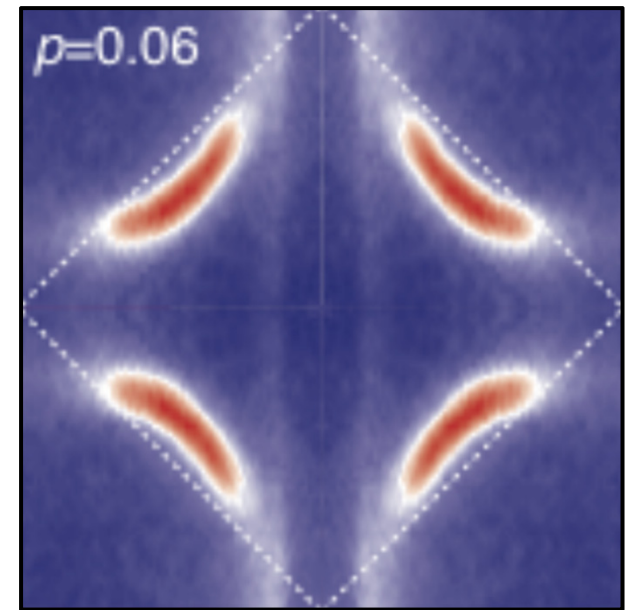
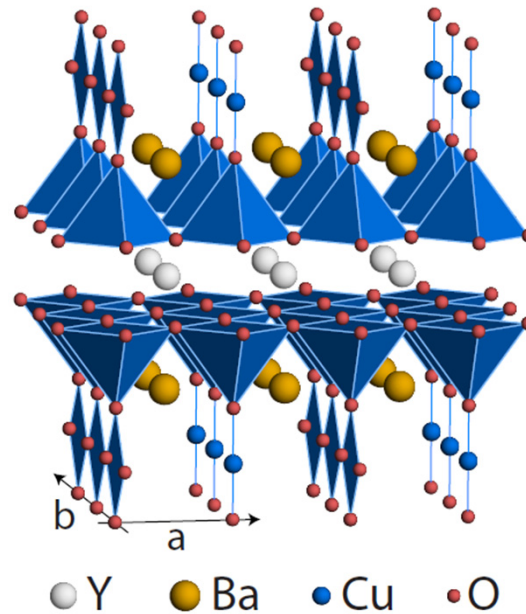


# ARPES: Polarization Dependence

## Fermi surface of underdoped YBCO

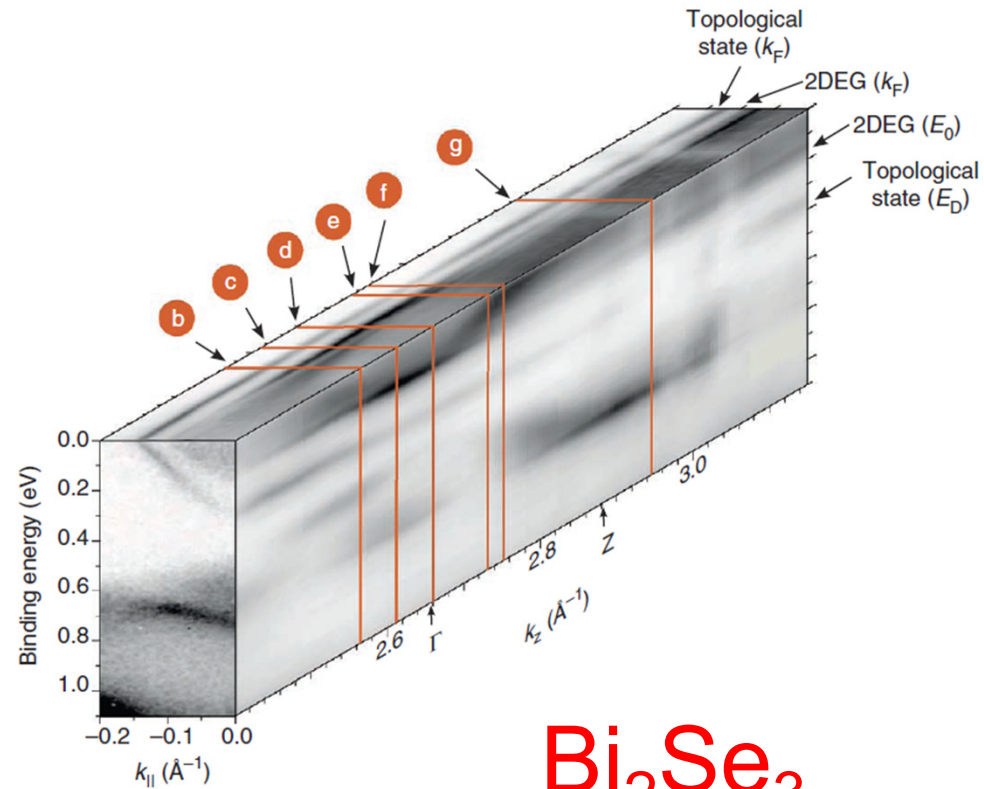
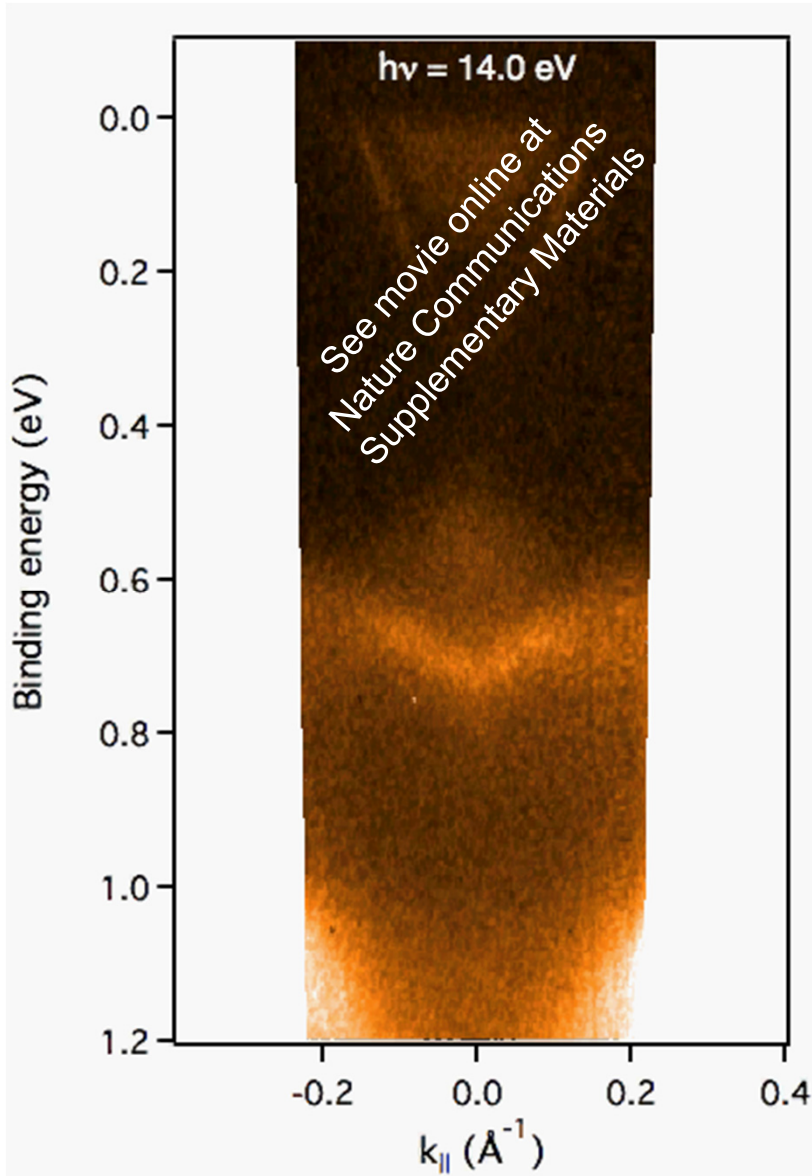


$E \parallel \text{CuO chains}$



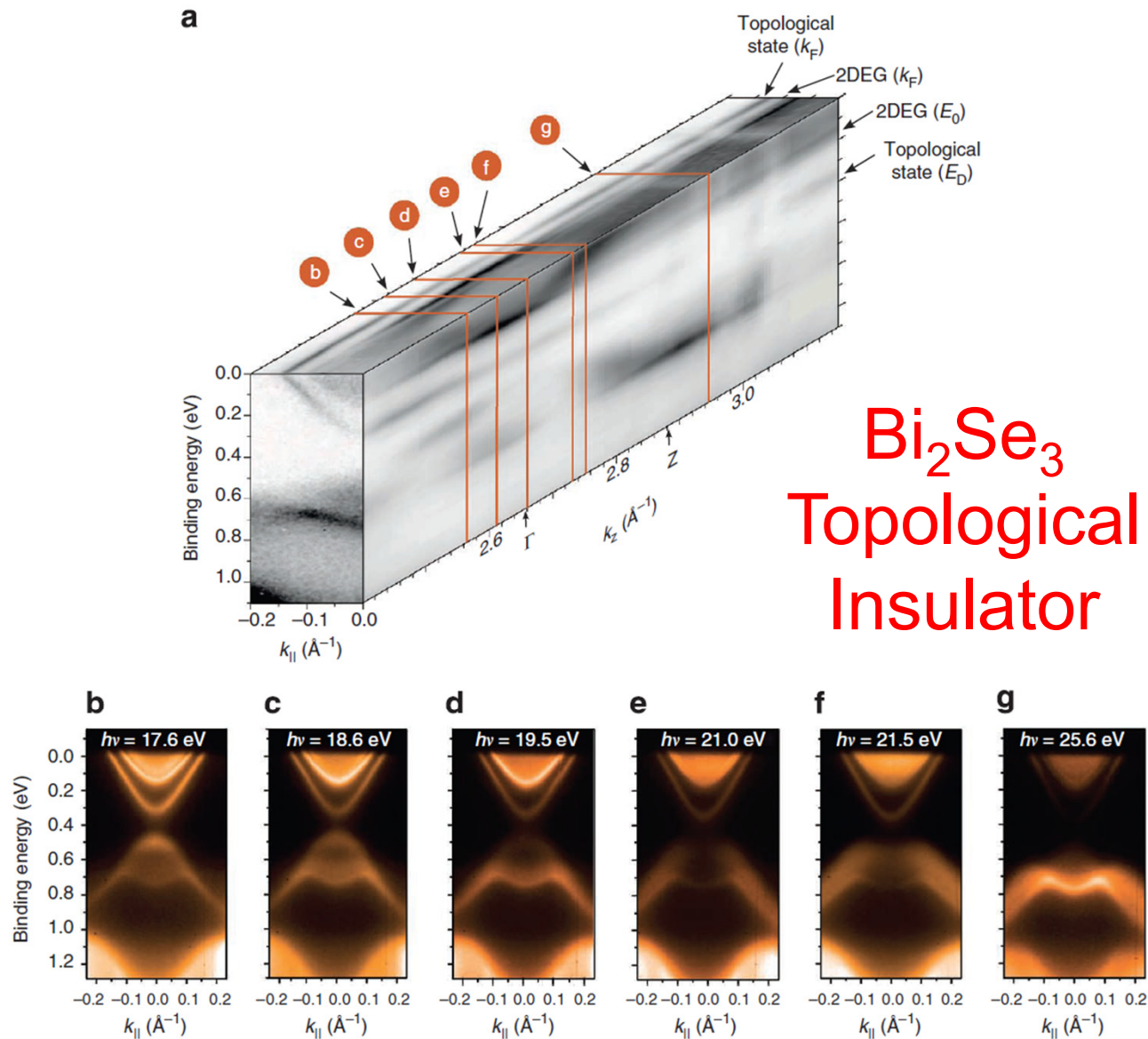
$E \perp \text{CuO chains}$

# ARPES: Photon Energy Dependence



**Bi<sub>2</sub>Se<sub>3</sub>**  
**Topological**  
**Insulator**

# ARPES: Photon Energy Dependence



Bianchi et al., Nature Comm. **1**, 128 (2010)

## Importance of Matrix Elements in the ARPES Spectra of BISCO

A. Bansil<sup>1</sup> and M. Lindroos<sup>1,2</sup>

<sup>1</sup>Physics Department, Northeastern University, Boston, Massachusetts 02115

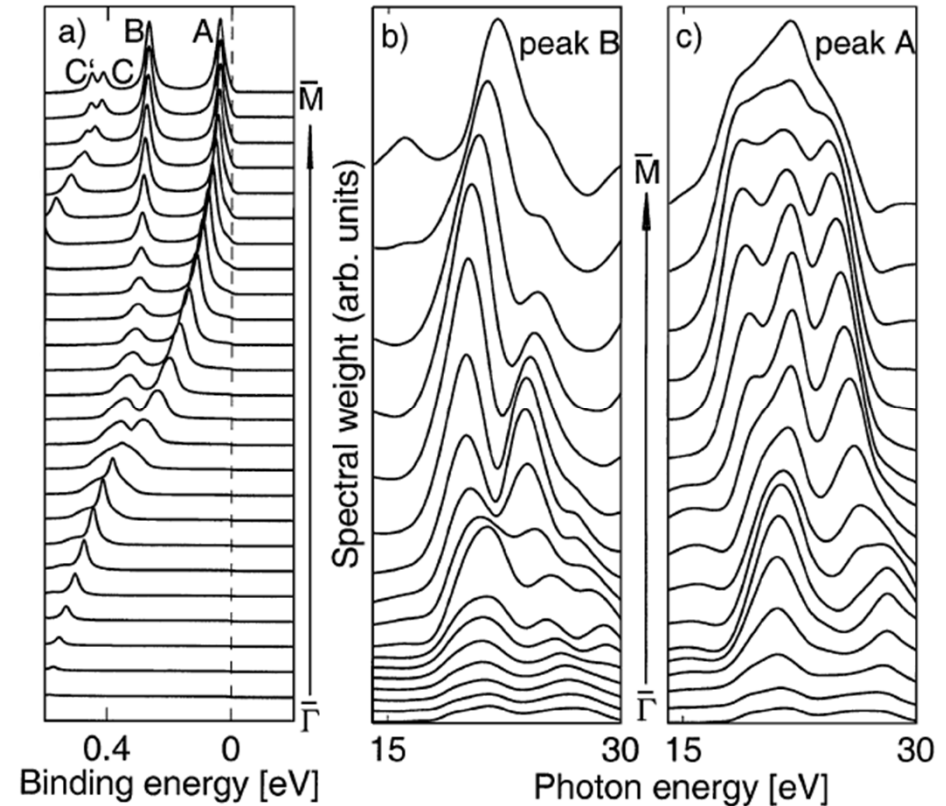
<sup>2</sup>Tampere University of Technology, P.O. Box 692, FIN-33101 Tampere, Finland

(Received 9 July 1999)

~~$$P(E, \omega) \sim |\langle \Psi_f^{\text{bulk}} | \Delta | \Psi_i^{\text{bulk}} \rangle|^2 A_i(E)$$~~

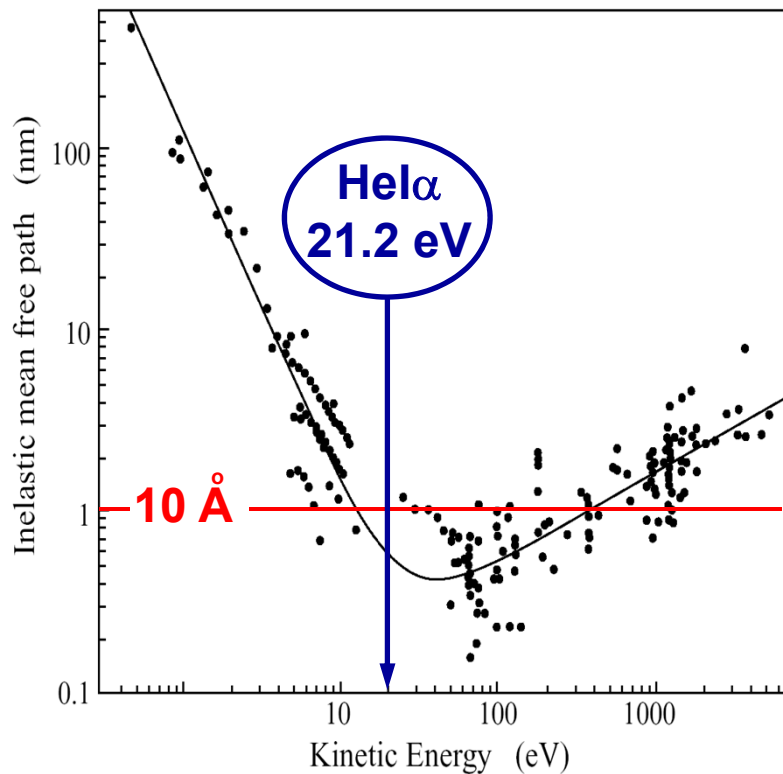
One-step model calculation + LDA

$$I(\mathbf{k}_{\parallel}, E, \hbar\omega) = \frac{1}{\pi} \text{Im} \langle \mathbf{k}_{\parallel} | G_2^+(E + \hbar\omega) \Delta G_1^+(E) \Delta^\dagger \times G_2^-(E + \hbar\omega) | \mathbf{k}_{\parallel} \rangle$$

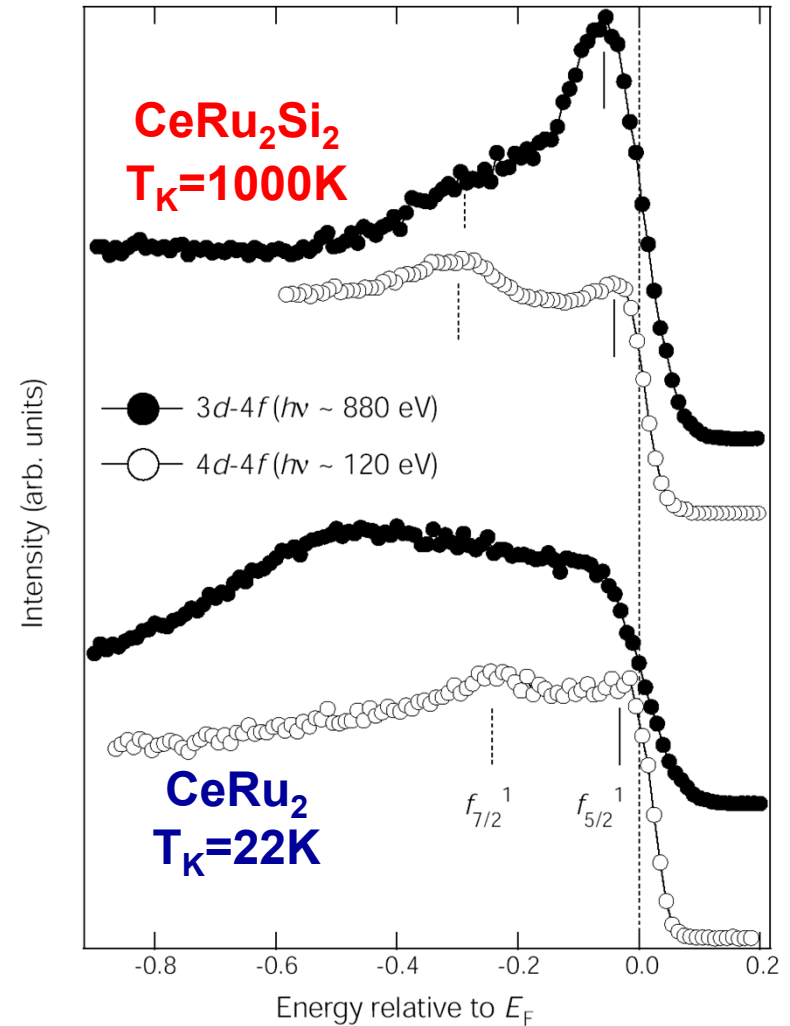


# ARPES: Surface vs Bulk Sensitivity

## Mean-free path for excited electrons



Seah, Dench *et al.*, SIA 1, 2 (1979)



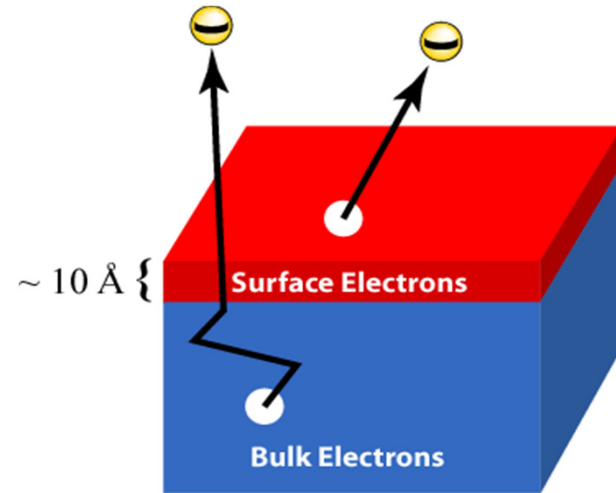
Sekiyama *et al.*, Nature **403**, 396 (2000)

# ARPES: Advantages and Limitations

## Advantages

- **Direct information about the electronic states!**
- Straightforward comparison with theory - little or no modeling.
- High-resolution information about **BOTH energy and momentum**
- **Surface-sensitive probe**
- Sensitive to “**many-body**” effects
- Can be applied to small samples (100  $\mu\text{m}$  x 100  $\mu\text{m}$  x 10 nm)

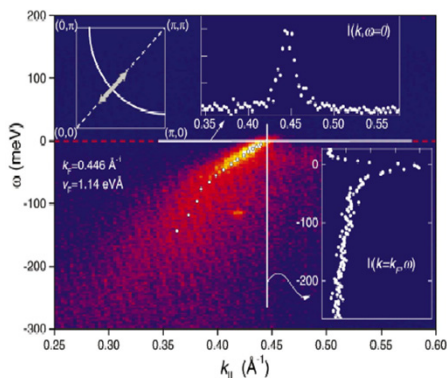
## Limitations



- **Not bulk sensitive**
- Requires clean, atomically flat surfaces in **ultra-high vacuum**
- Cannot be studied as a function of pressure or magnetic field

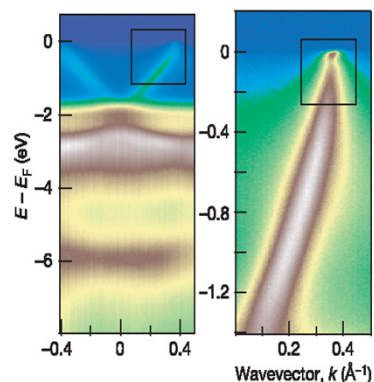
# ARPES: Widespread Impact in Complex Materials

## HTSC's



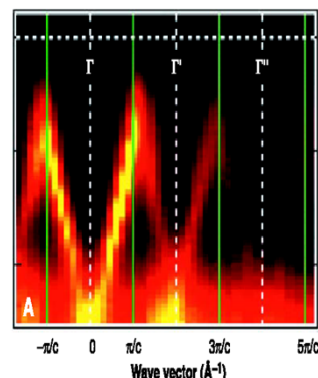
Science 1999

## CMR's



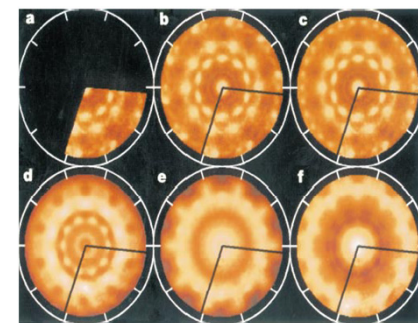
Nature 2005

## CDW's



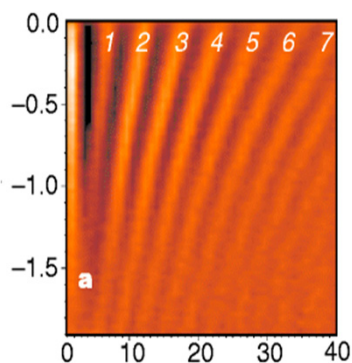
Science 2000

## Quasicrystals



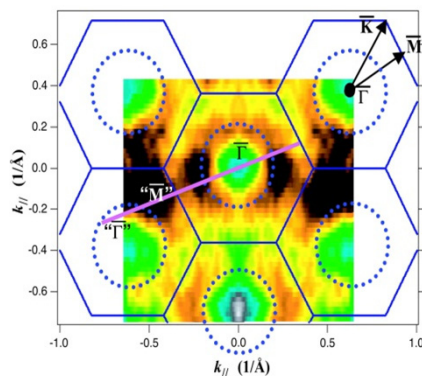
Nature 2000

## Quantum Wells



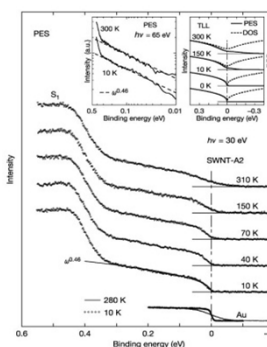
Nature 1999

## C<sub>60</sub>



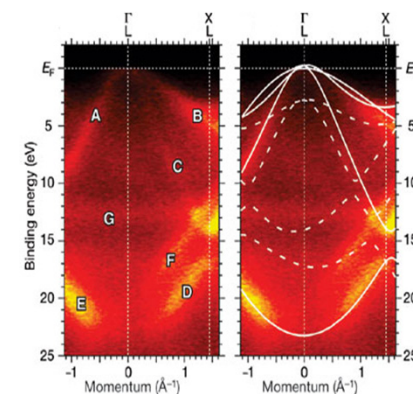
Science 2003

## Nanotubes



Nature 2003

## Diamond



Nature 2005



UNIVERSITY OF BRITISH COLUMBIA



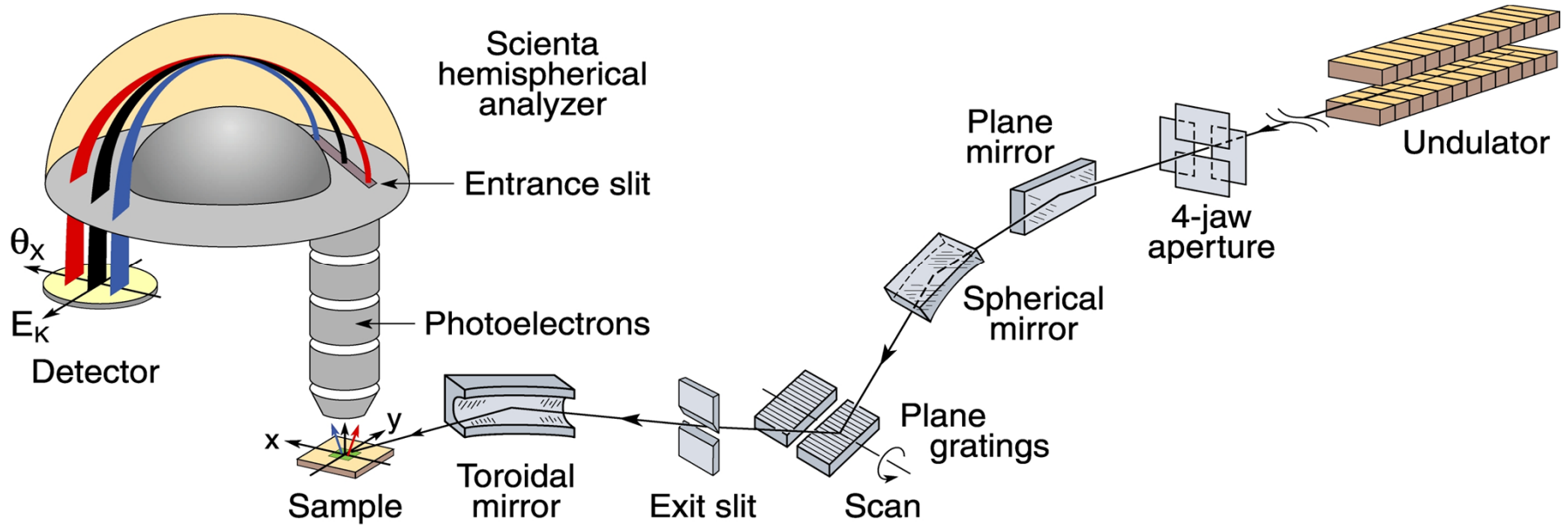
# Outline Part I

## ARPES: Technique and developments

CUSO Lecture – Lausanne 02/2011



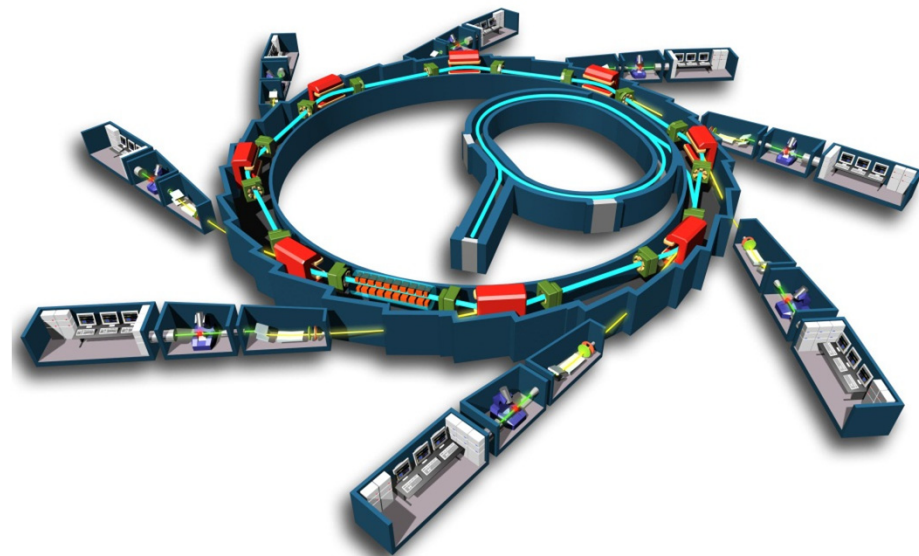
# Angle-Resolved Photoemission Spectroscopy



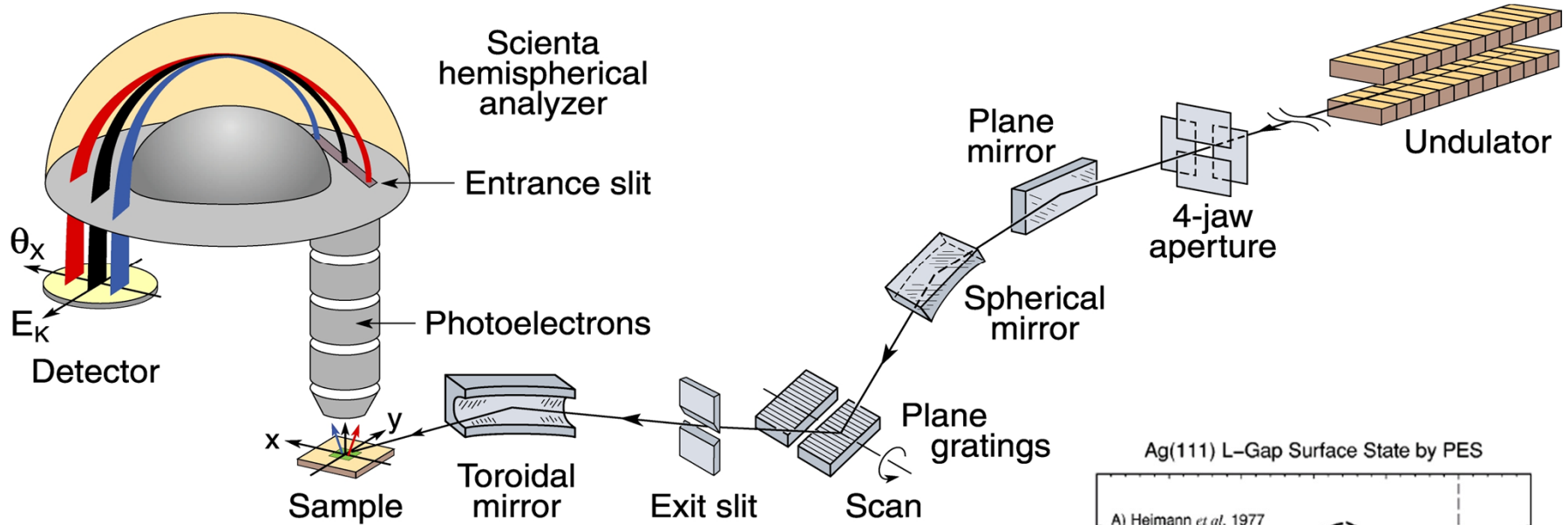
## Parallel multi-angle recording

- Improved energy resolution
- Improved momentum resolution
- Improved data-acquisition efficiency

	$\Delta E$ (meV)	$\Delta\theta$
past	20-40	$2^\circ$
now	1-10	$0.2^\circ$



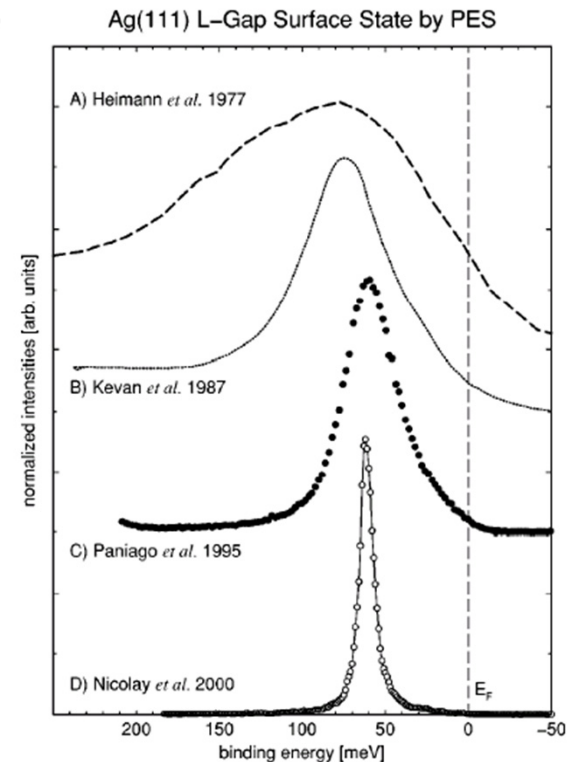
# Angle-Resolved Photoemission Spectroscopy



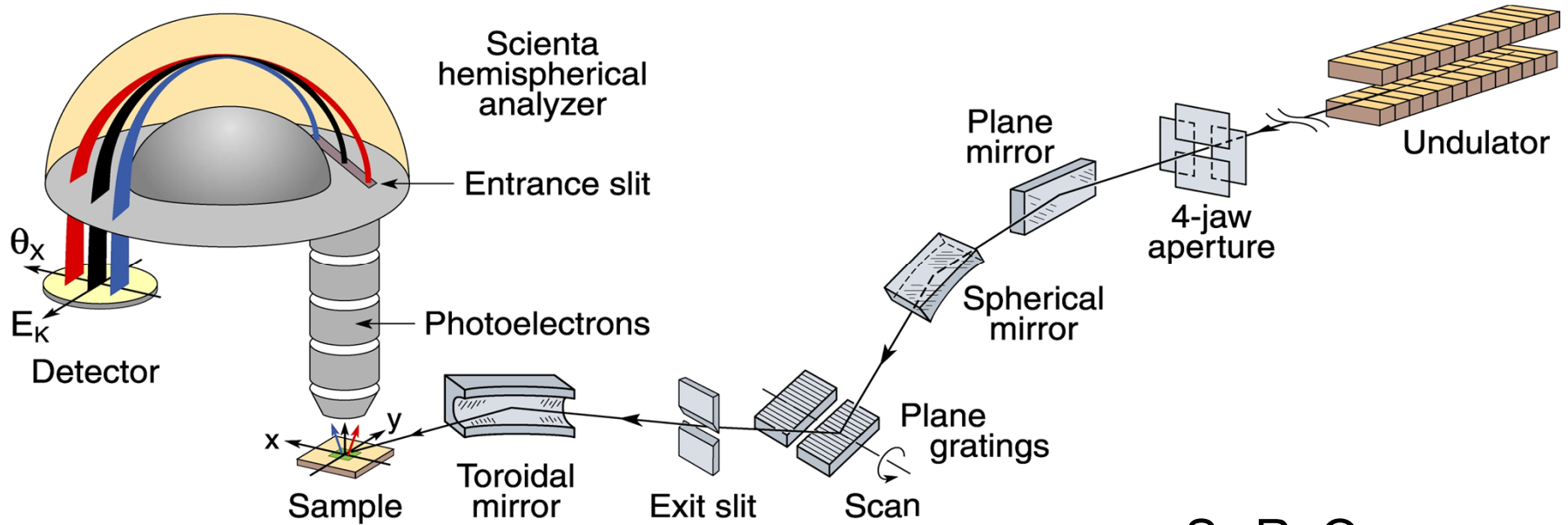
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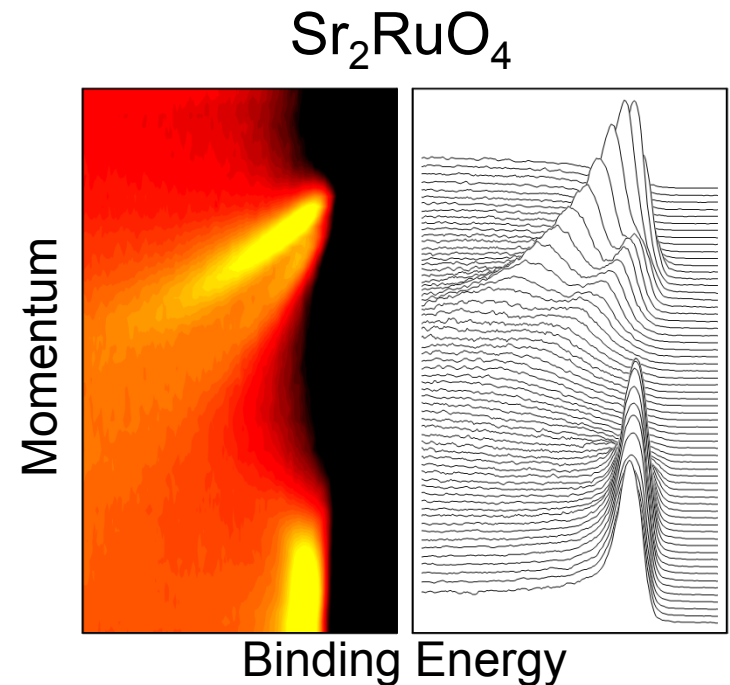
# Angle-Resolved Photoemission Spectroscopy



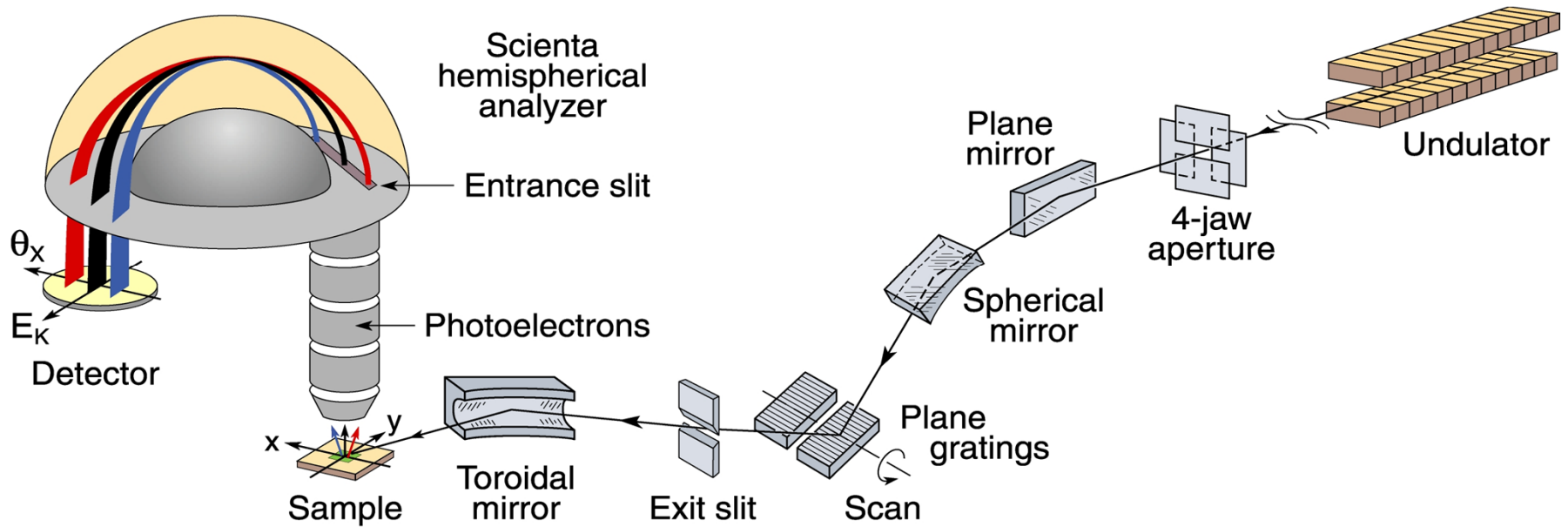
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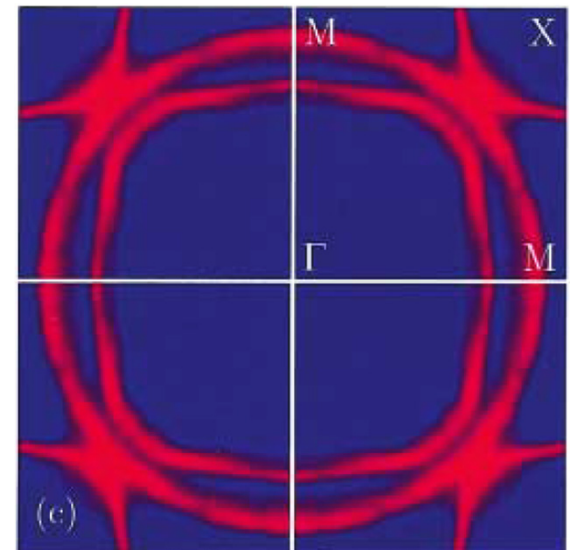
# Angle-Resolved Photoemission Spectroscopy



## Parallel multi-angle recording

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	$\Delta E$ (meV)	$\Delta\theta$
past	20-40	$2^\circ$
now	1-10	$0.2^\circ$



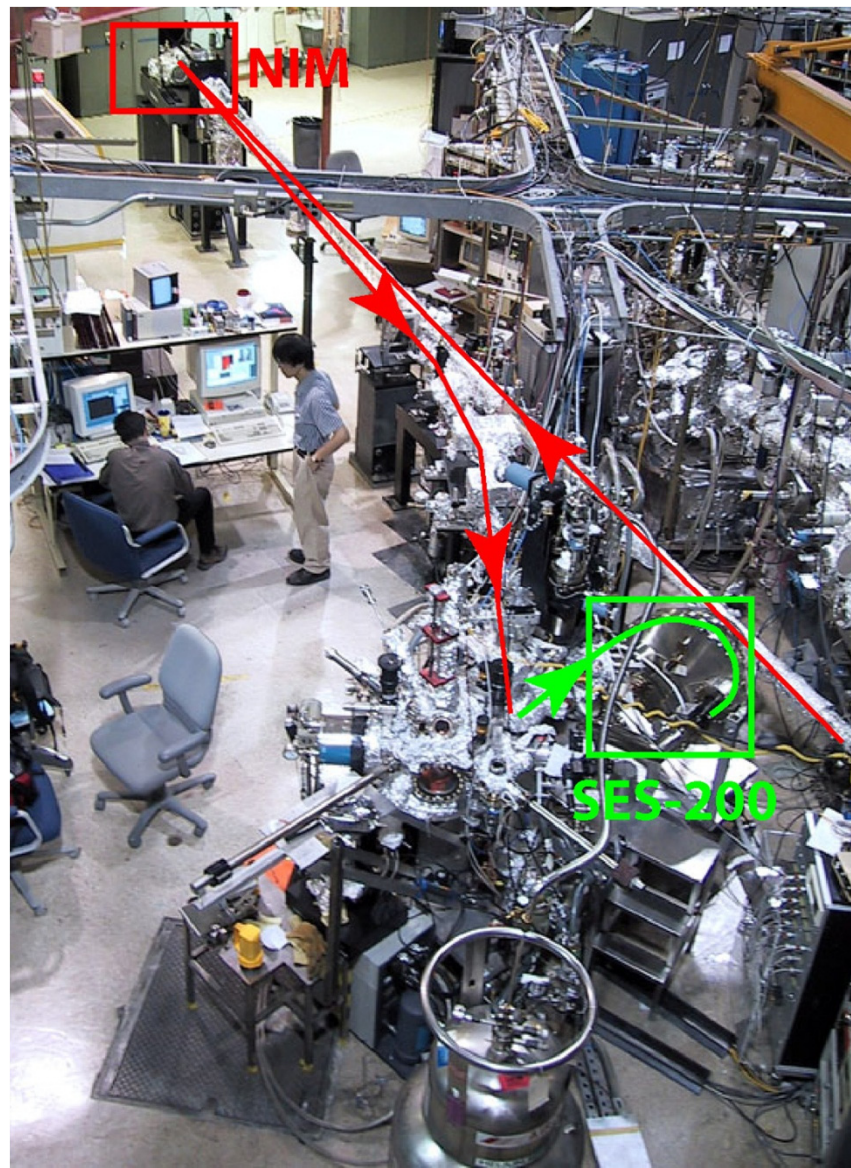
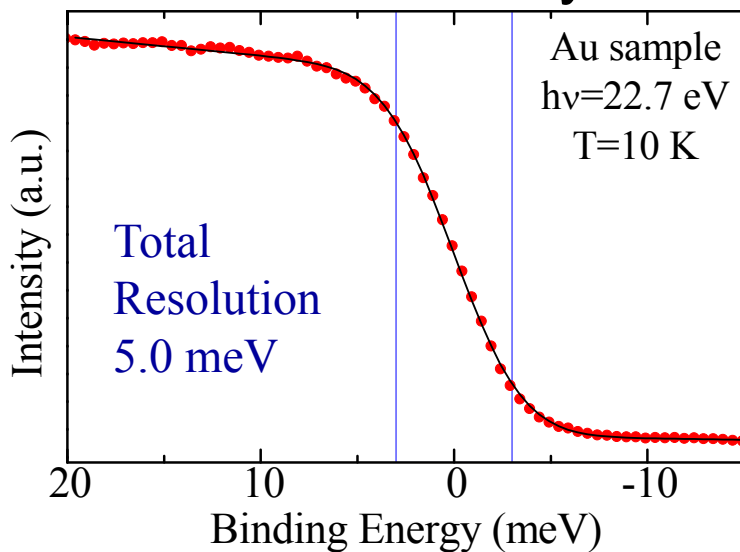
# Angle-Resolved Photoemission Spectroscopy

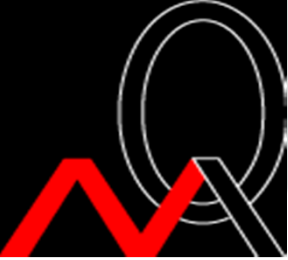
STANFORD SYNCHROTRON RADIATION LABORATORY



$\Delta E$ (meV)	$\Delta\theta$
1-10	0.2°

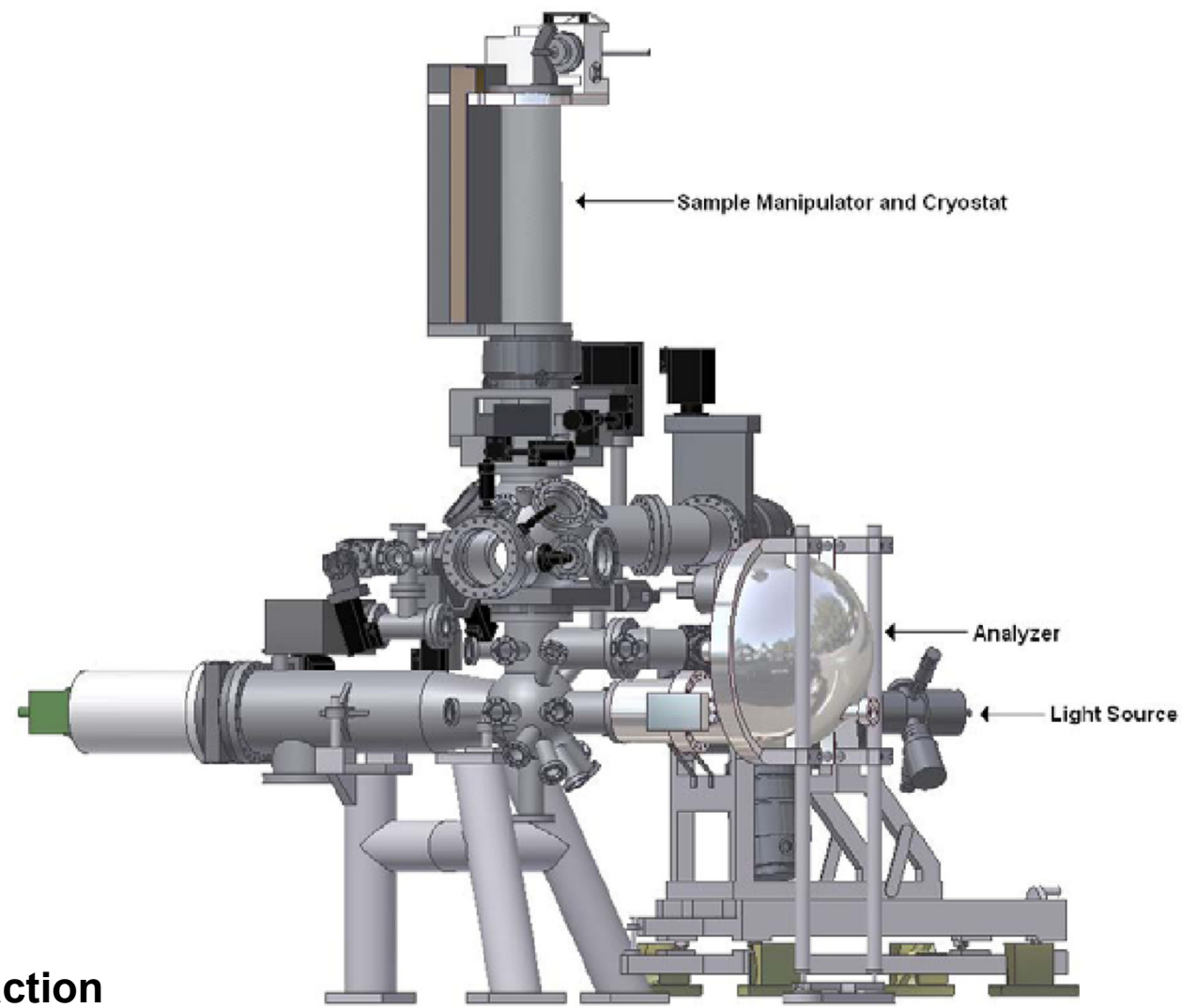
## NIM/SCIENTA System

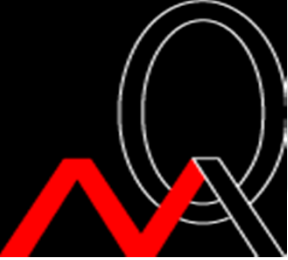




# ARPES ON COMPLEX SYSTEMS

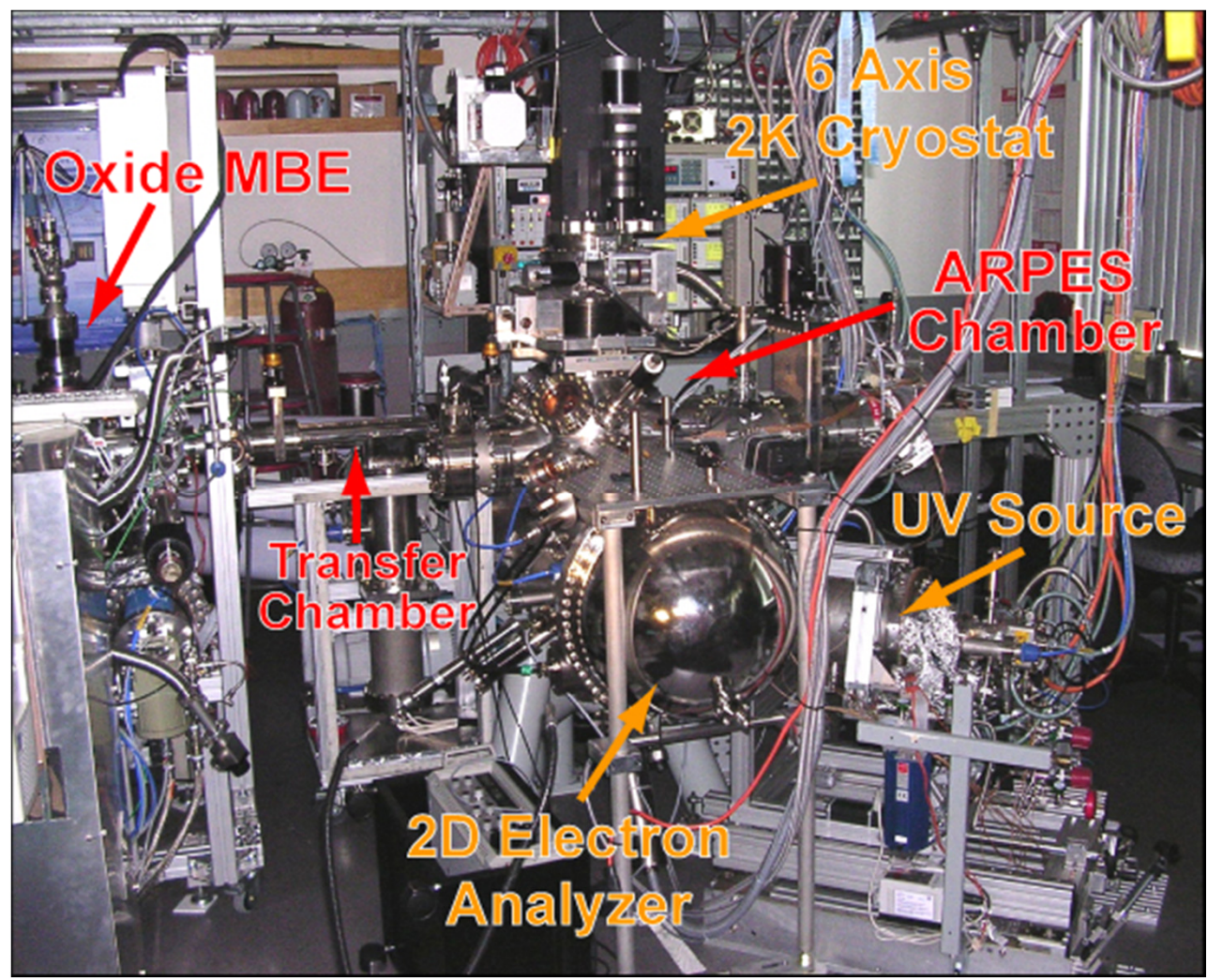
- High energy resolution  
 $\Delta E < 1 \text{ meV}$
- High angular precision  
 $\pm 0.05^\circ$
- Low base temperature  
 $\sim 2 \text{ K}$
- Photon energies  
 $\text{H}_2, \text{He}, \text{Ne}$
- Polarization control  
linear
- Ultra-high vacuum  
 $\sim 10^{-11} \text{ torr}$
- Surface / Thin films
- Low Energy Electron Diffraction

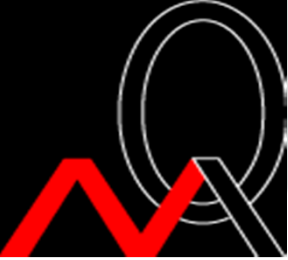




# ARPES ON COMPLEX SYSTEMS

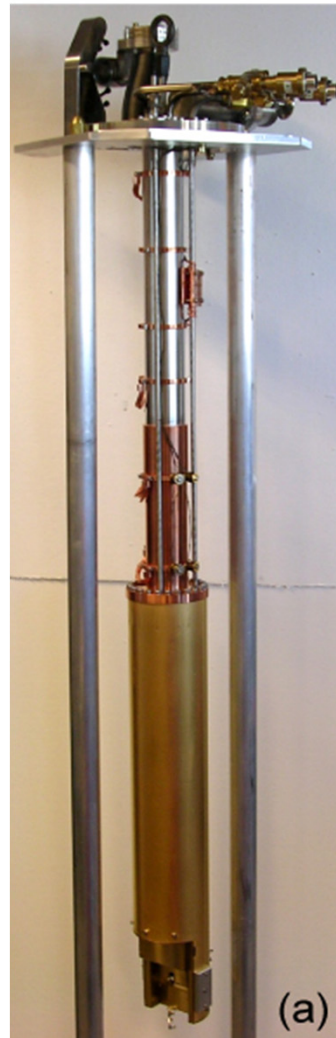
- High energy resolution  
 $\Delta E < 1 \text{ meV}$
- High angular precision  
 $\pm 0.05^\circ$
- Low base temperature  
 $\sim 2 \text{ K}$
- Photon energies  
 $\text{H}_2, \text{He}, \text{Ne}$
- Polarization control  
linear
- Ultra-high vacuum  
 $\sim 10^{-11} \text{ torr}$
- Surface / Thin films
- LEED



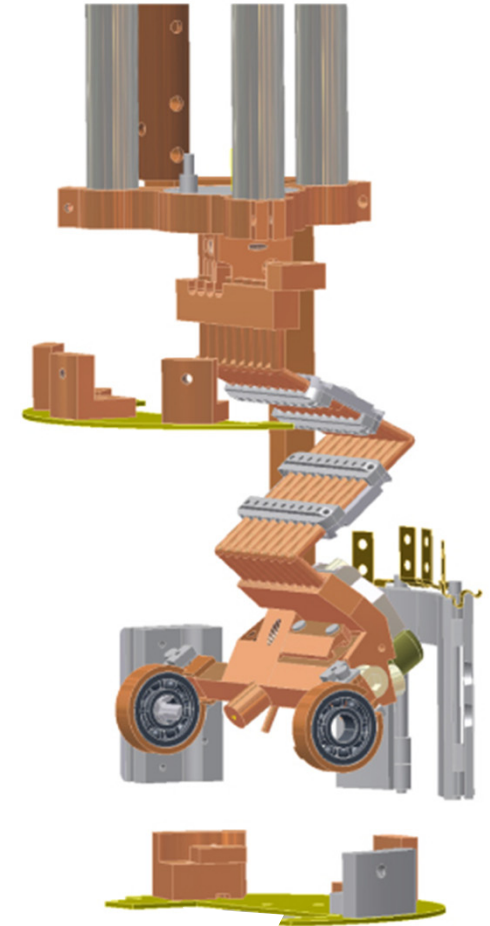
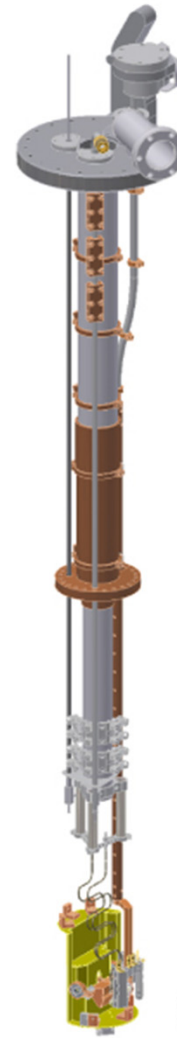


# ARPES ON COMPLEX SYSTEMS

- High energy resolution  
 $\Delta E < 1 \text{ meV}$
- High angular precision  
 $\pm 0.05^\circ$
- Low base temperature  
 $\sim 2 \text{ K}$
- Photon energies  
 $\text{H}_2, \text{He}, \text{Ne}$
- Polarization control  
linear
- Ultra-high vacuum  
 $\sim 10^{-11} \text{ torr}$
- Surface / Thin films
- LEED

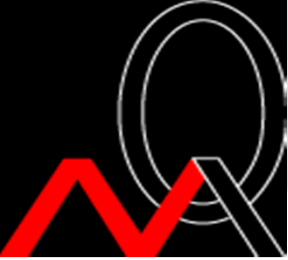


(a)

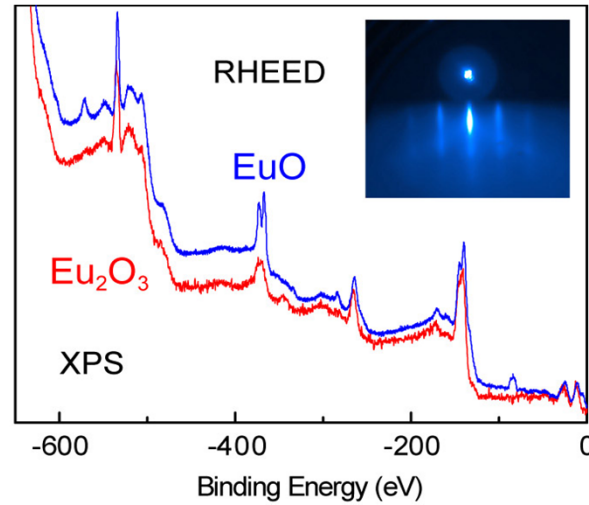
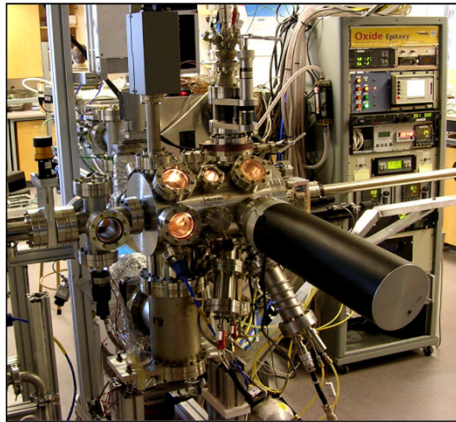


**5 1/2 axes manipulator  
2.7 K on the sample**





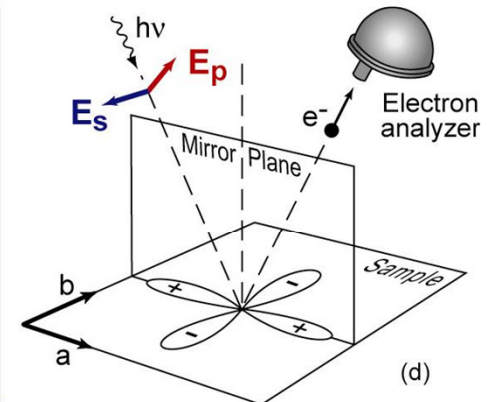
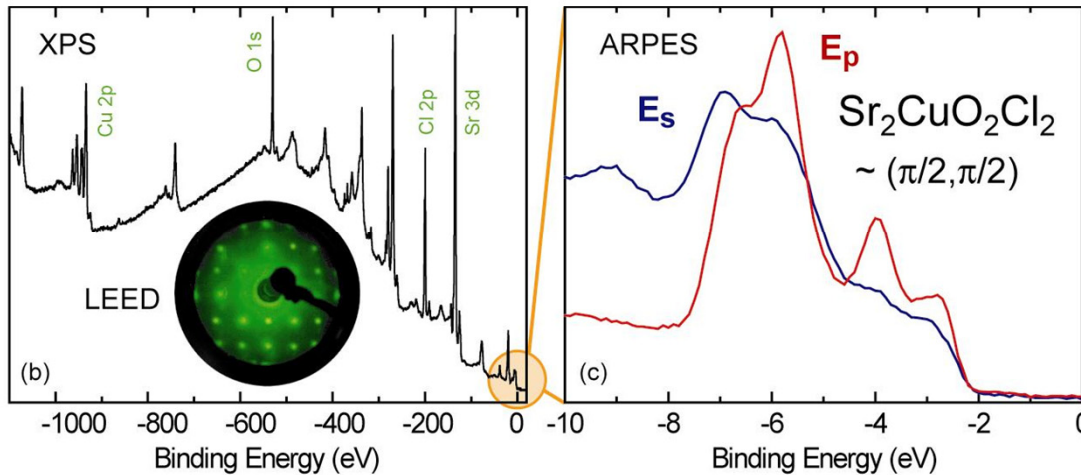
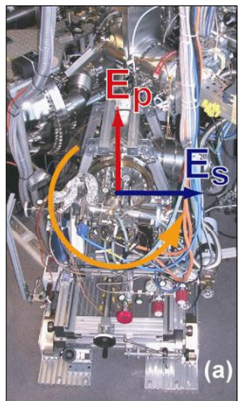
# ARPES ON COMPLEX SYSTEMS



**MBE Growth**

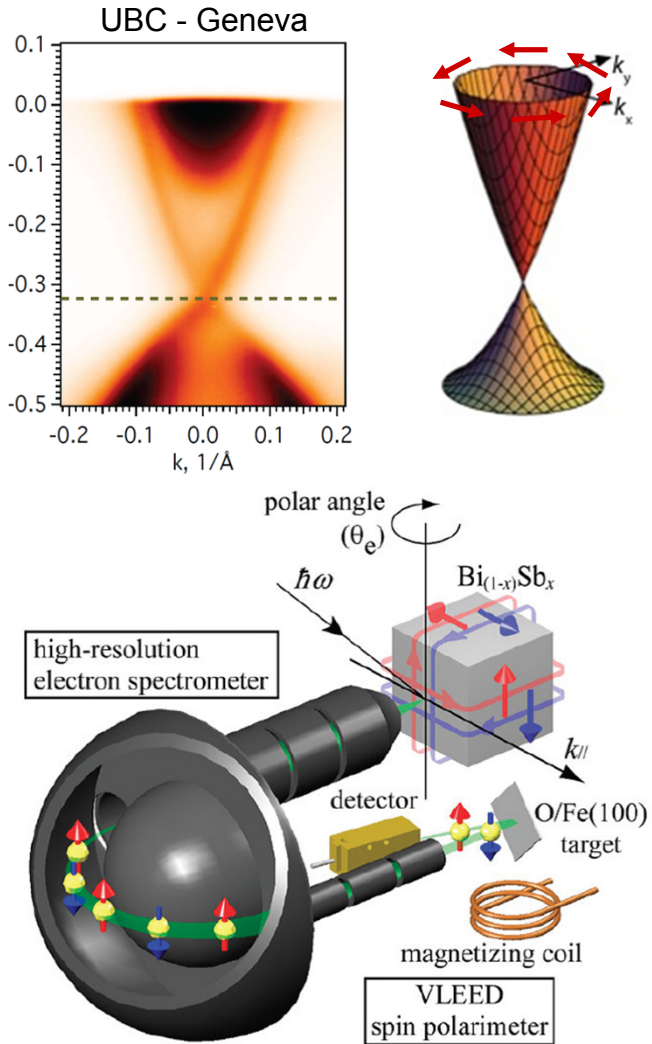
**Characterization  
Structure – chemistry**

**ARPES  
Polarization - Energy**

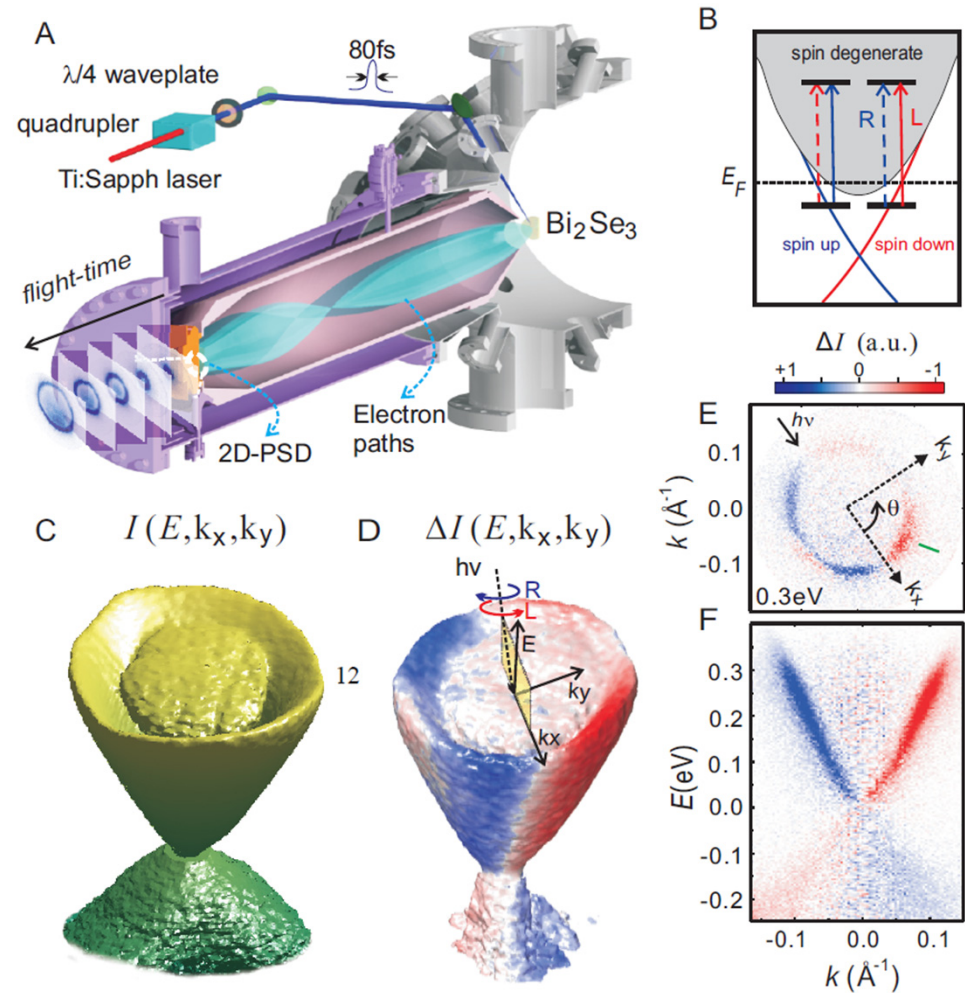


# New Developments: ARPES + Spin + Time

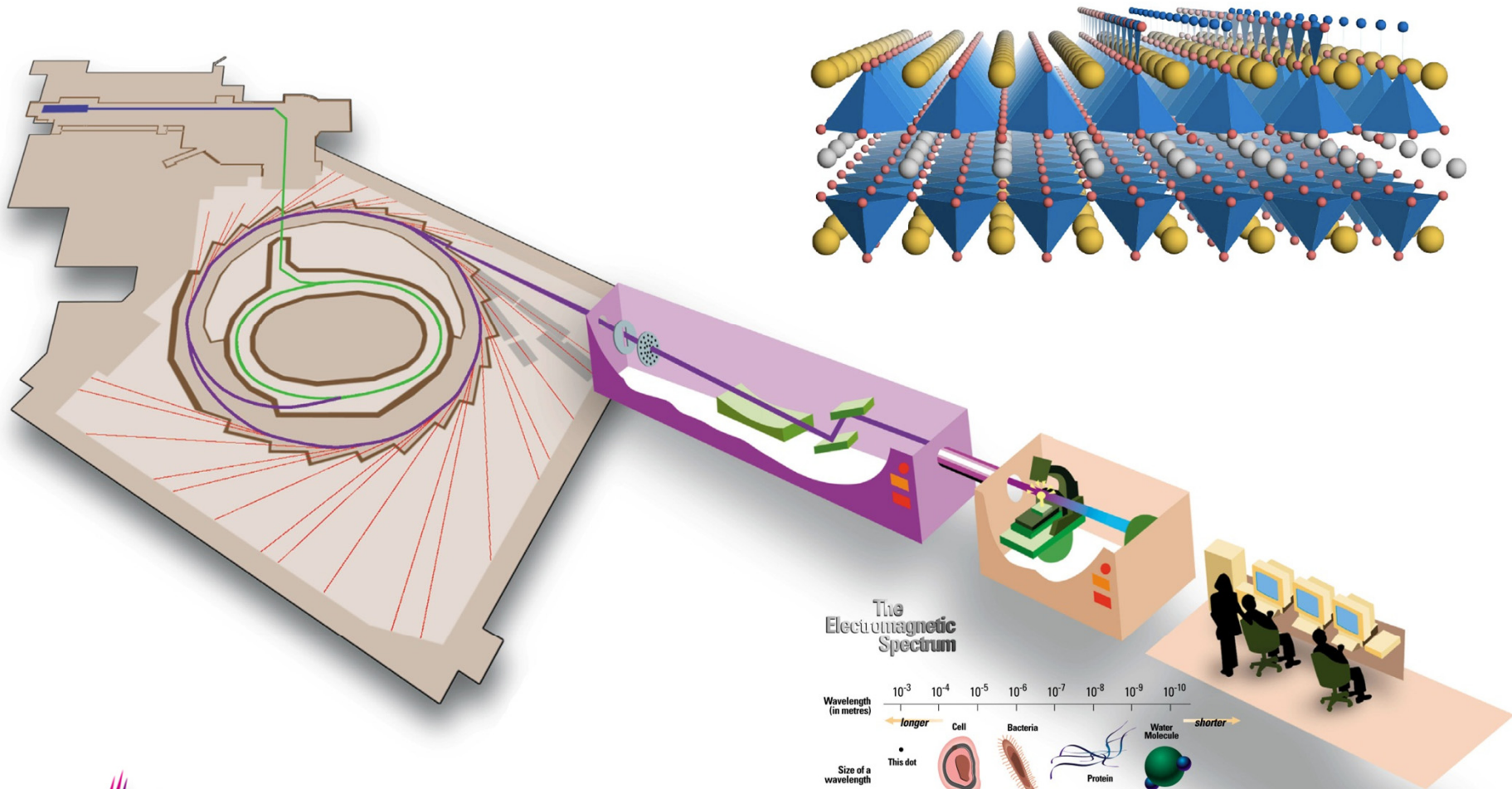
## ARPES+Spin polarimeter



## ARPES+Time of Flight



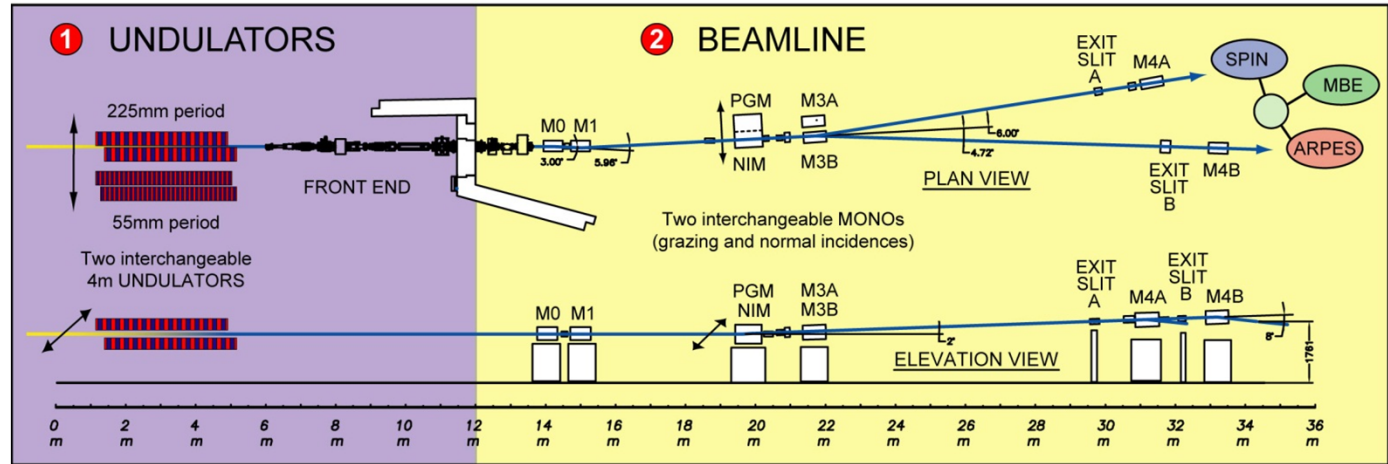
# Quantum Materials Spectroscopy Center at CLS



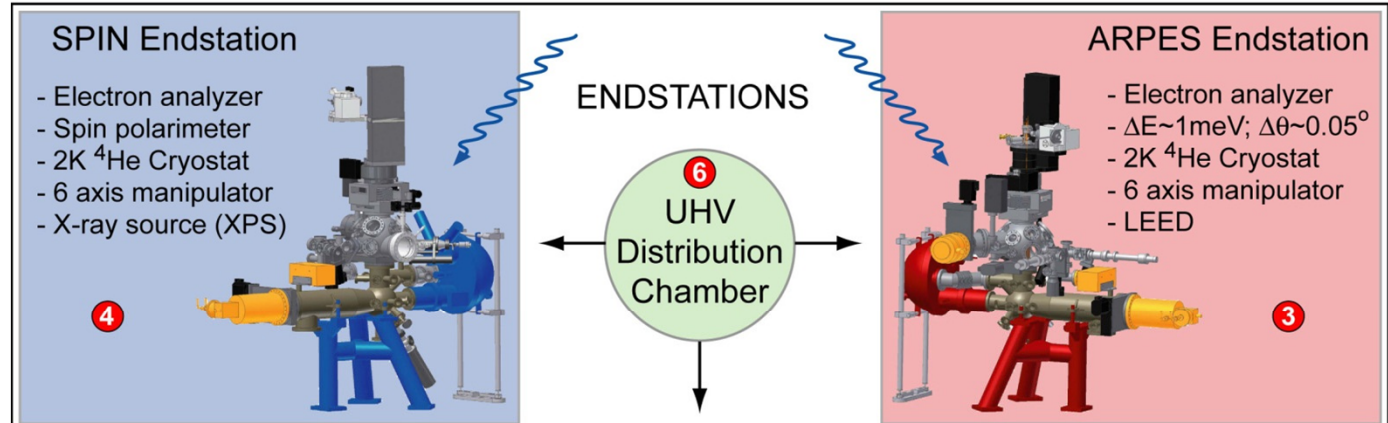
**Canadian Light Source Inc.**

# Quantum Materials Spectroscopy Center at CLS

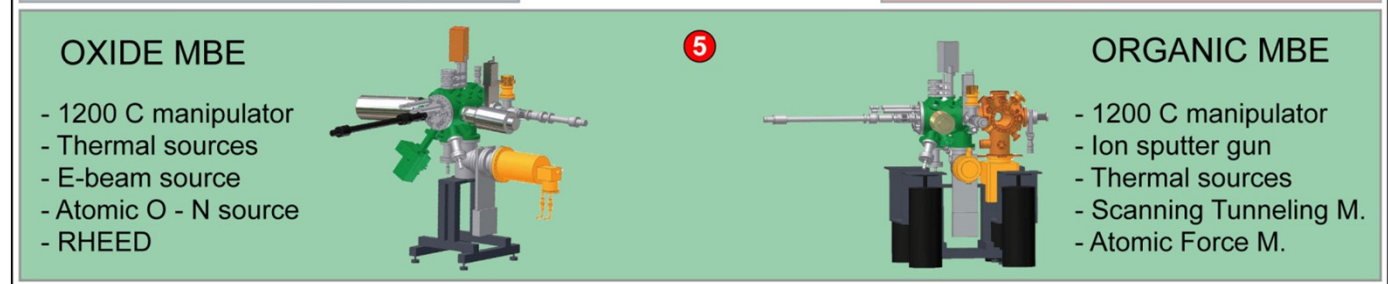
- Broad energy range
- Polarization control
- Resolving power
- Maximum flux



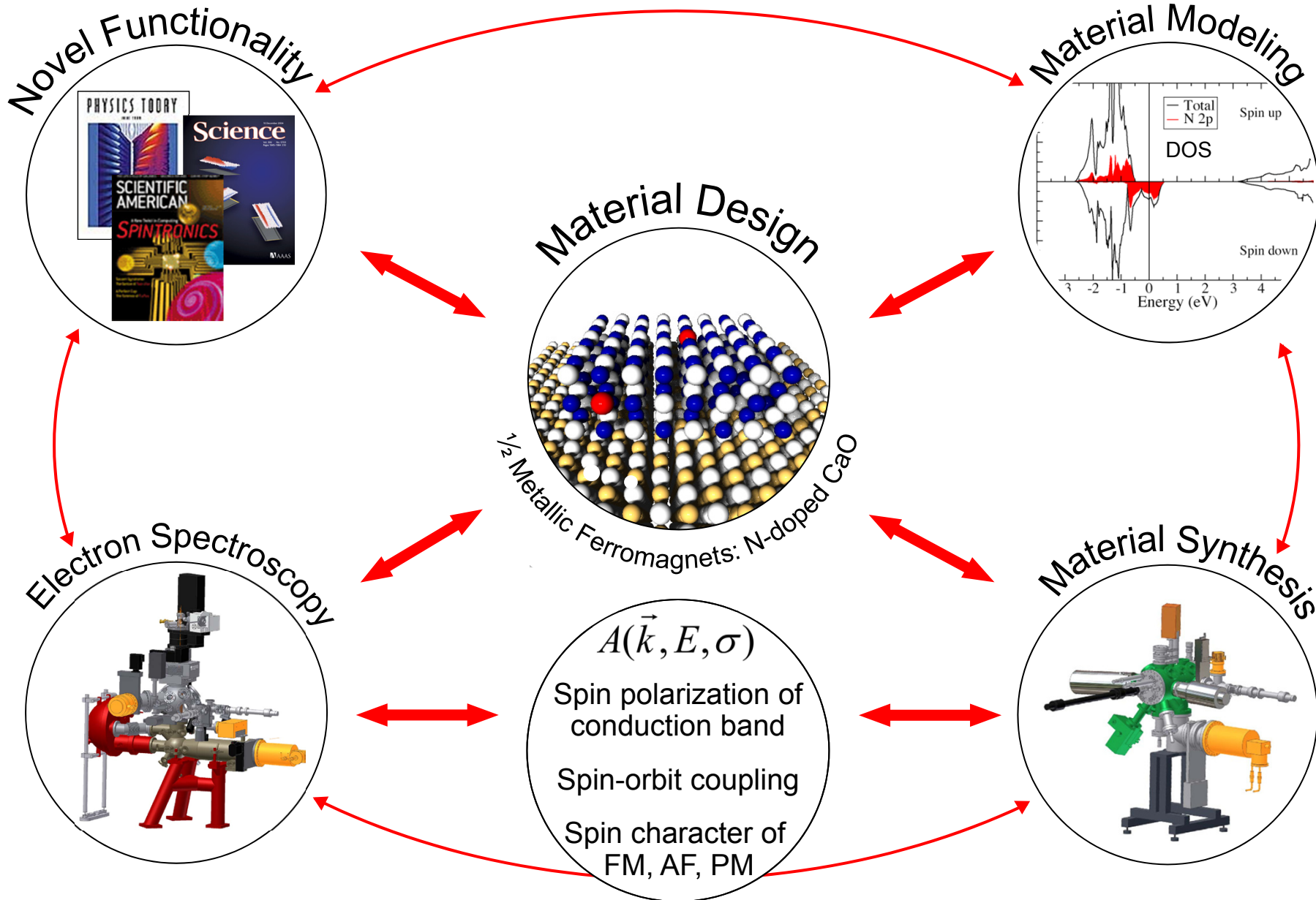
- High-res. ARPES
- Spin polarimeter
- Motion Accuracy
- Low Temperature



- Oxide MBE
- Organic MBE
- LEED/RHEED
- STM/AFM/XPS



# Novel Complex Materials and Functionalities





# Outline Part I

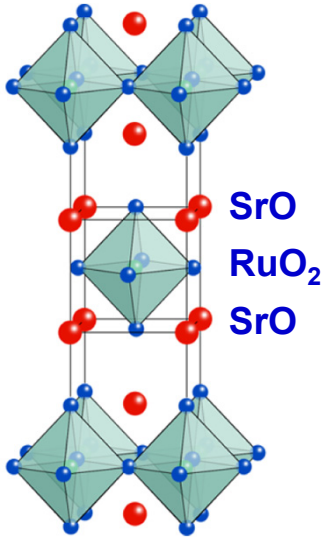
Bulk, surface, and

Fermi surfaces:  $\text{Sr}_2\text{RuO}_4$

CUSO Lecture – Lausanne 02/2011

# Sr<sub>2</sub>RuO<sub>4</sub>: basic properties

## 2D perovskite

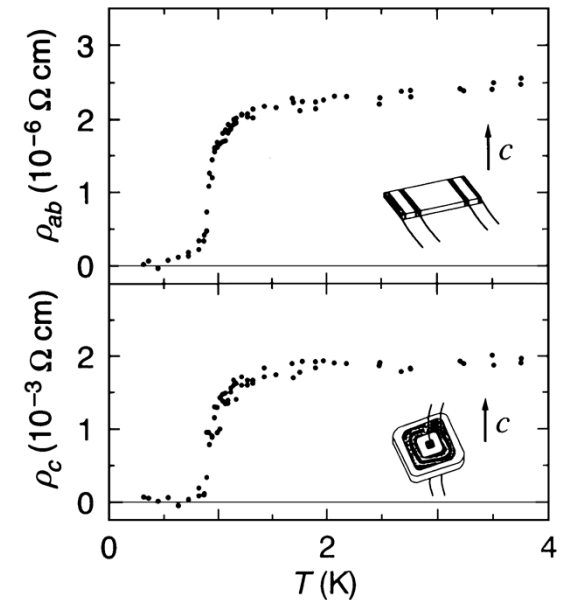


## Unconventional superconductivity

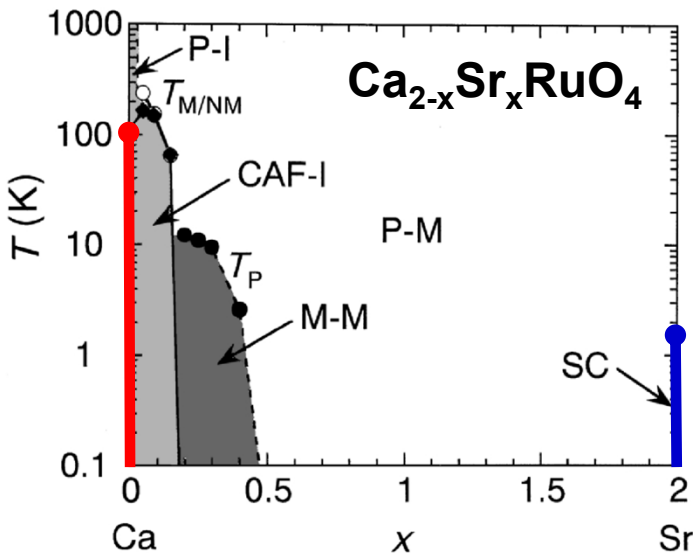
- Pairing mechanism ?
- Order parameter ?
- FM-AF fluctuations ?

Rice & Sigrist, JPCM 7, L643 (1995)

Maeno et al., Nature 372, 532 (1994)



Nakatsuji & Maeno, PRL 84, 2666 (2000)



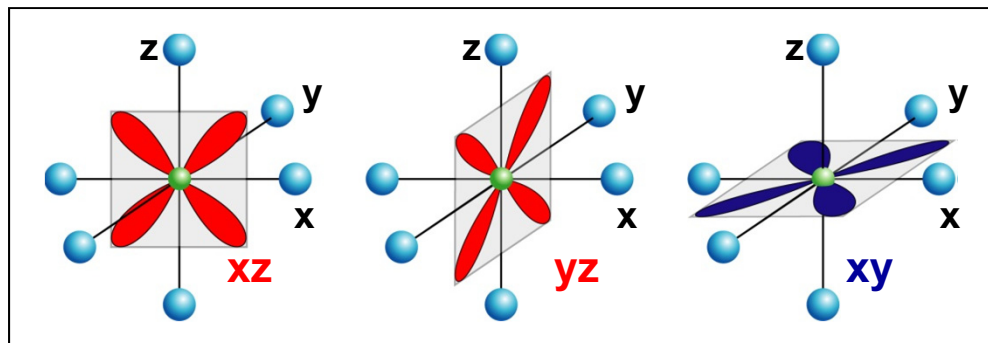
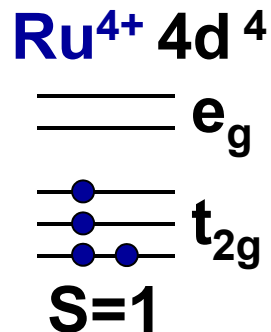
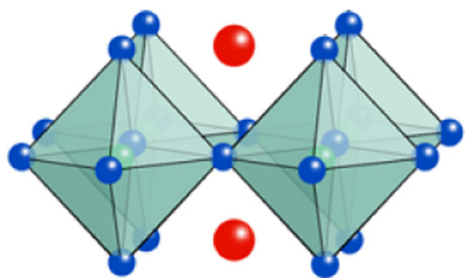
## Lattice-magnetism interplay Orbital degrees of freedom

**Sr<sub>2</sub>RuO<sub>4</sub>** : 2D **Fermi Liquid** ( $\rho_c/\rho_{ab}=850$ )

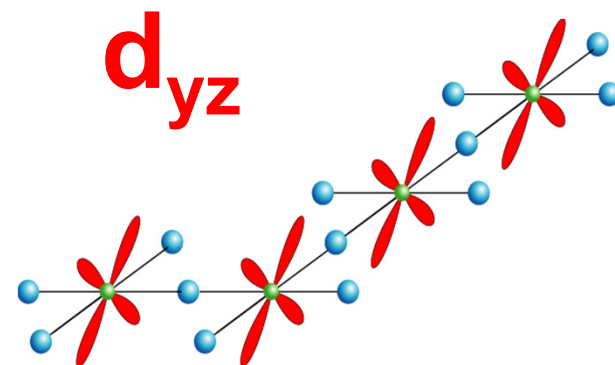
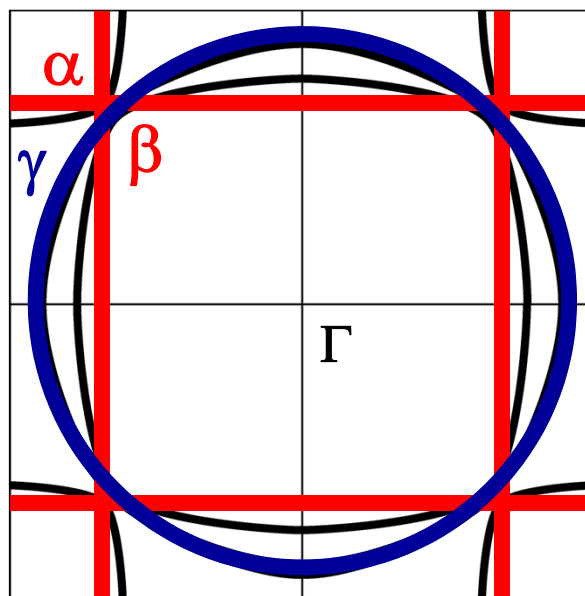
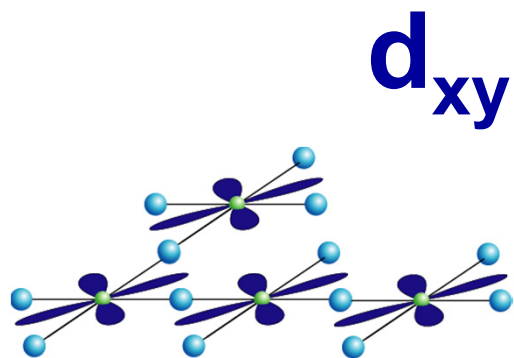
**Ca<sub>2</sub>RuO<sub>4</sub>** : insulating **Anti-Ferromagnet**

**SrRuO<sub>3</sub>** : metallic **Ferromagnet**

# 1D ( $d_{xz,yz}$ ) versus 2D ( $d_{xy}$ ) Superconductivity ?



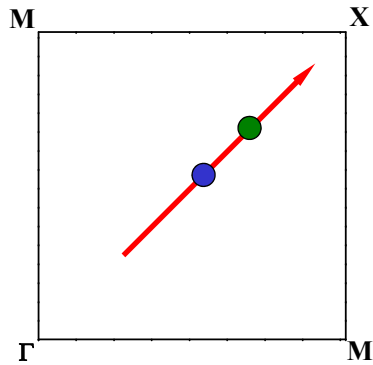
► Band structure calculation: **3 t<sub>2g</sub>** bands crossing **E<sub>F</sub>**



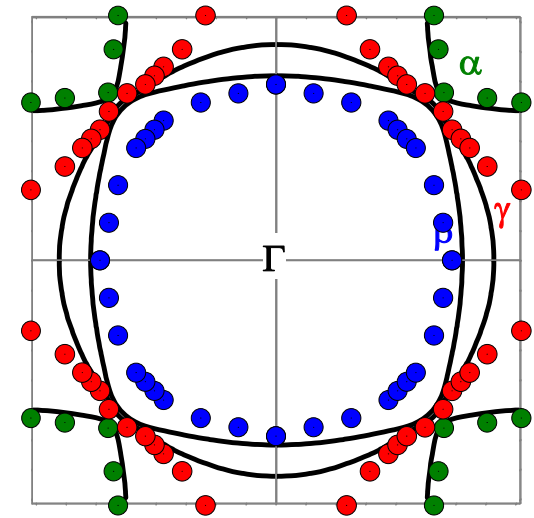
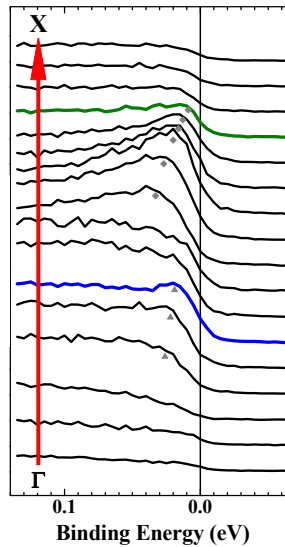


# Fermi Surface Topology of $\text{Sr}_2\text{RuO}_4$

## ARPES : circa 1996

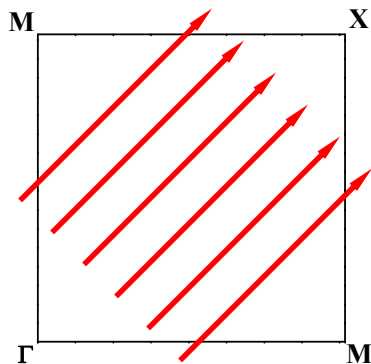


D.H. Lu *et al.*, PRL **76**, 4845 (1996)

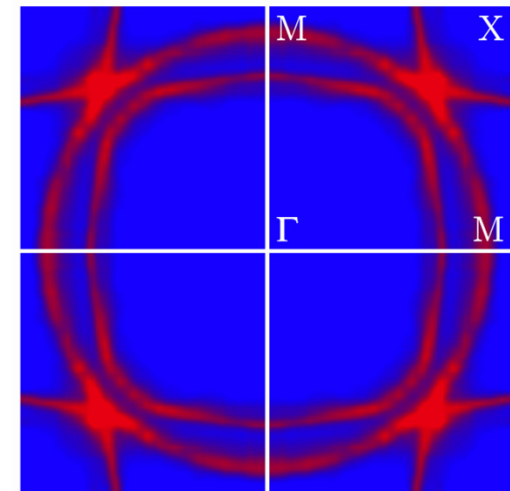
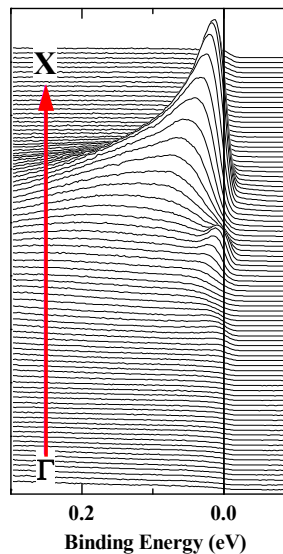


D.J. Singh, PRB **52**, 1358 (1995)

## ARPES : present day

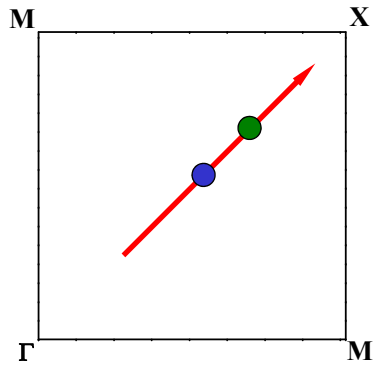


A. Damascelli *et al.*, PRL **85**, 5194 (2000)

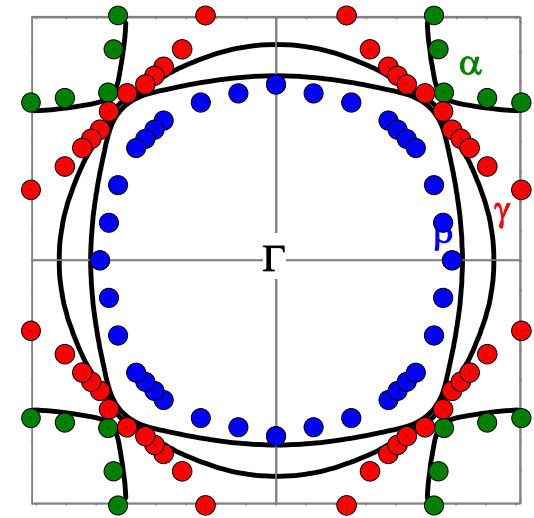
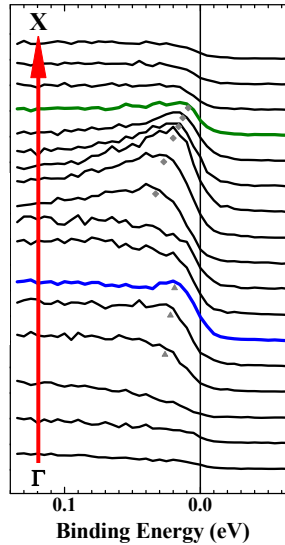


# Fermi Surface Topology of $\text{Sr}_2\text{RuO}_4$

## ARPES : circa 1996

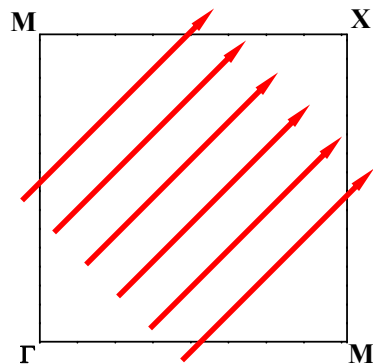


D.H. Lu *et al.*, PRL **76**, 4845 (1996)



D.J. Singh, PRB **52**, 1358 (1995)

## ARPES : present day

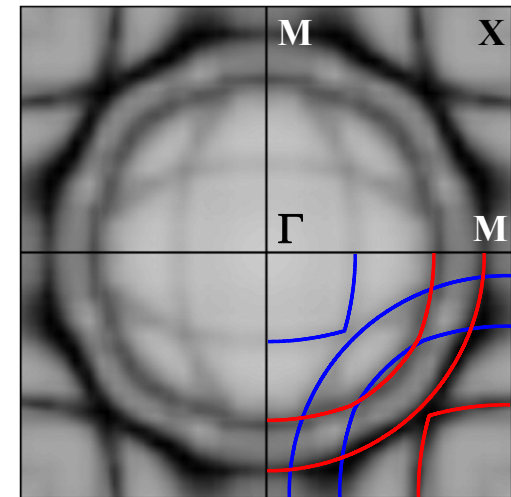
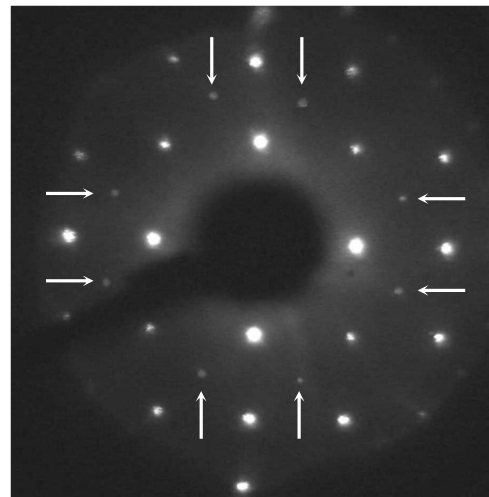


A. Damascelli *et al.*, PRL **85**, 5194 (2000)

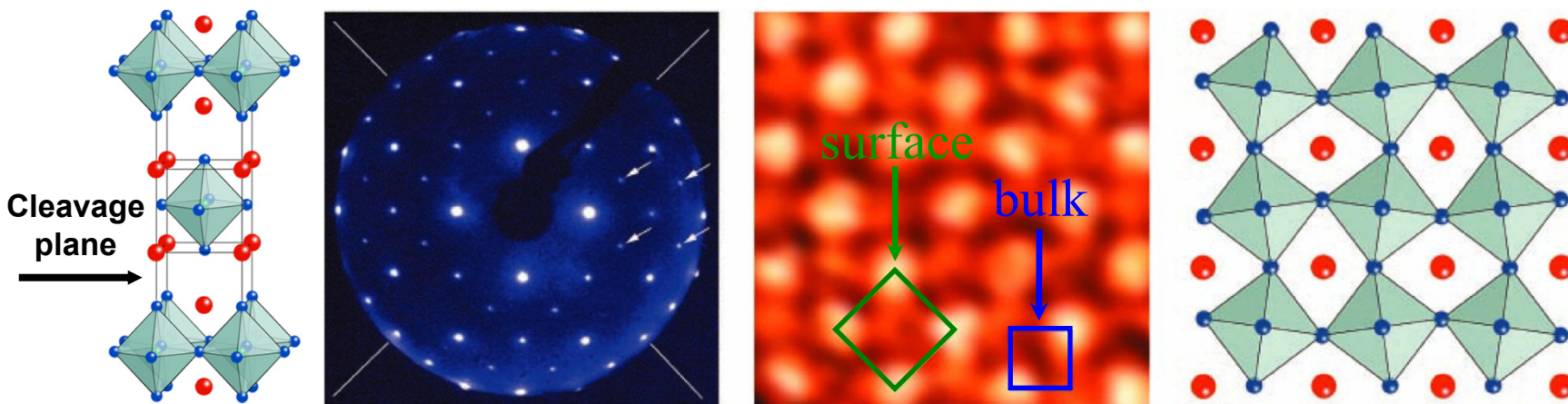
Surface instability



Band folding



# Surface reconstruction of cleaved $\text{Sr}_2\text{RuO}_4$



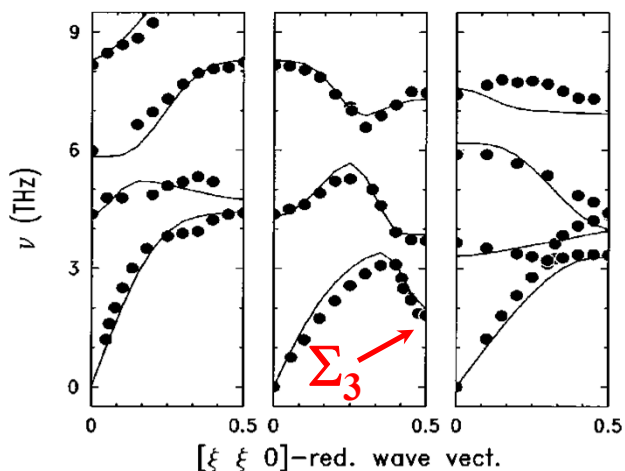
R. Matzdorf *et al.*, Science **289**, 746 (2000)

Rotation of the  $\text{RuO}_6$  octahedra around the c axis

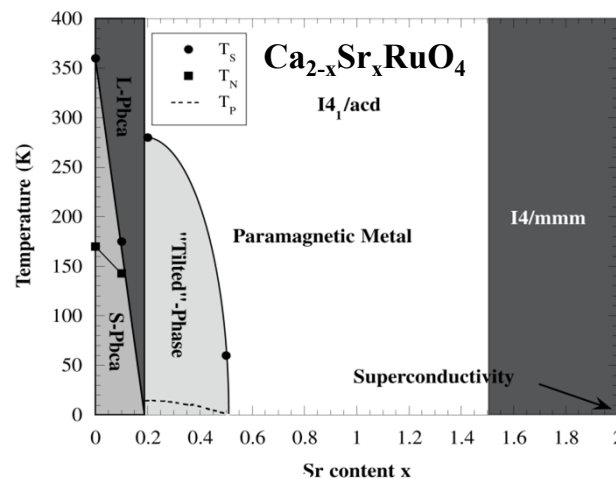
Soft  $\Sigma_3$  phonon branch



Rotation instability of  $\text{Ca}_{2-x}\text{Sr}_x\text{RuO}_4$



M. Braden *et al.*, PRB **57**, 1236 (1998)

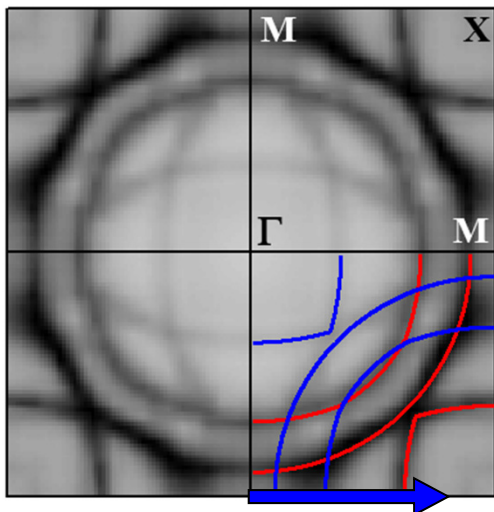


O. Friedt *et al.*, PRB **63**, 174432 (2001)

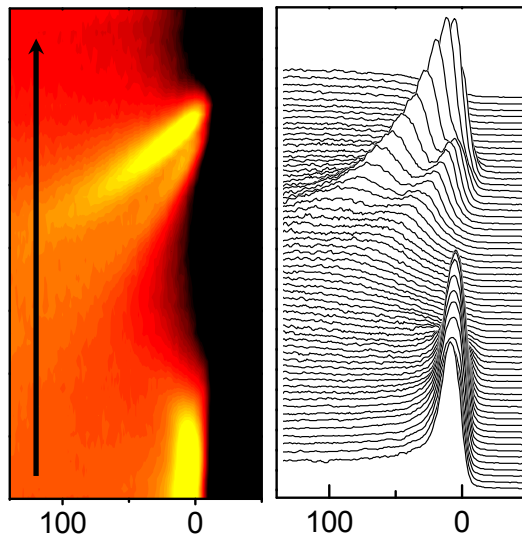
# Surface electronic structure of $\text{Sr}_2\text{RuO}_4$

On samples cleaved at **180 K**  
the **surface**-related features are  
**suppressed**

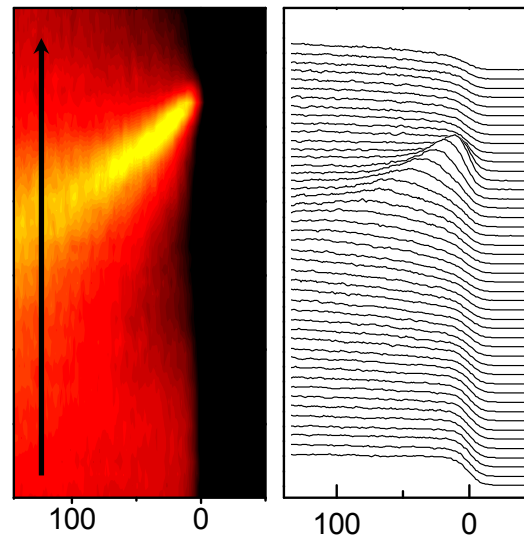
$E_F$  mapping  
 $\pm 10$  meV



Cold cleave  
 $T=10$  K



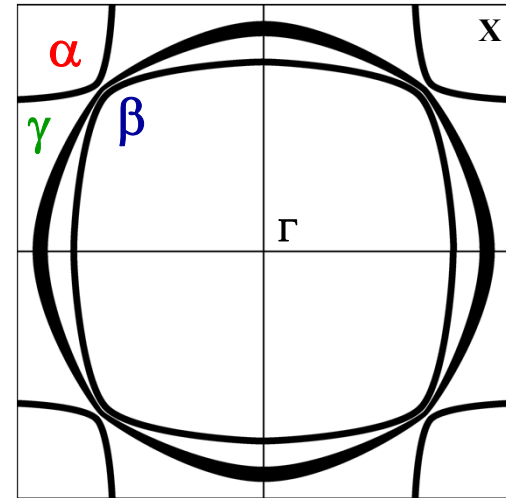
Hot cleave  
 $T=180$  K



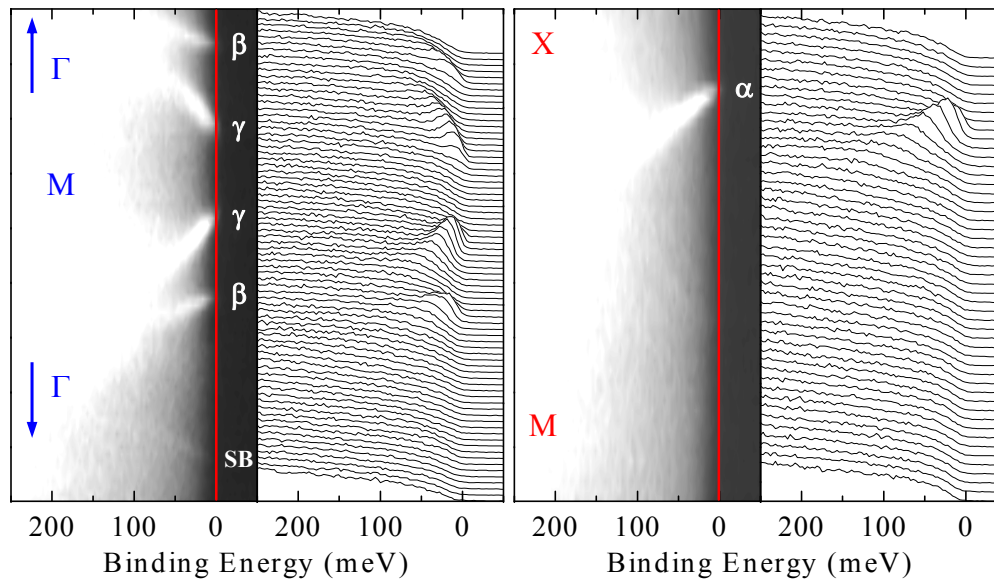
# Bulk electronic structure of $\text{Sr}_2\text{RuO}_4$

What do we learn about the **bulk** electronic structure?

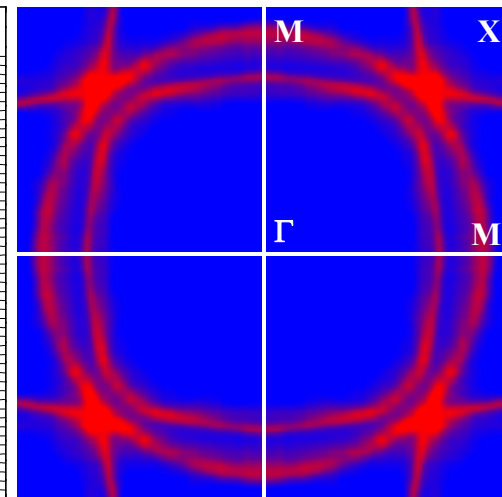
- **FS** topology
- Fermi **velocity**
- Effective **mass**



I.I. Mazin *et al.*, PRL **79**, 733 (1997)



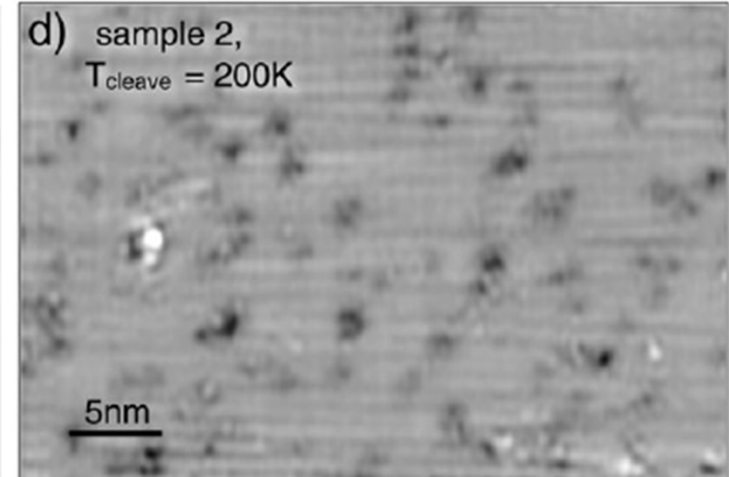
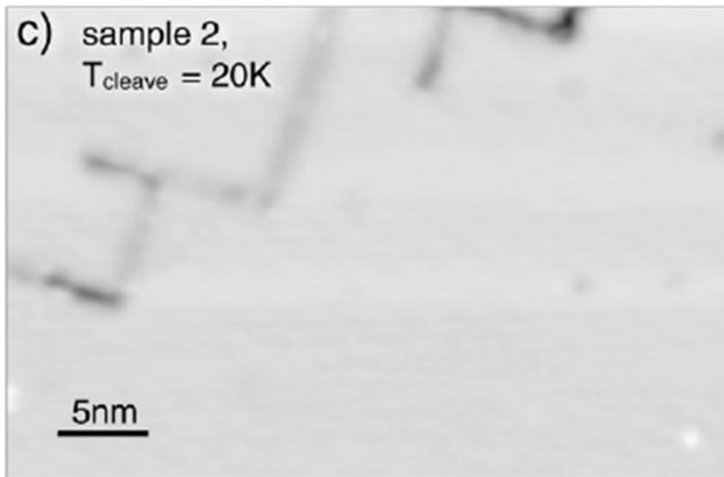
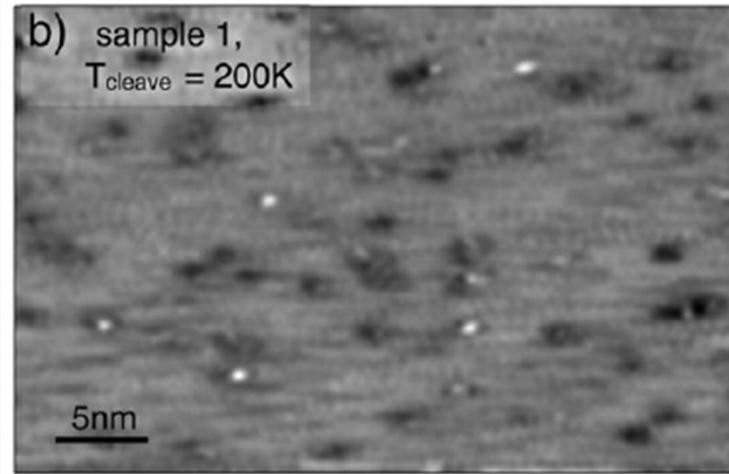
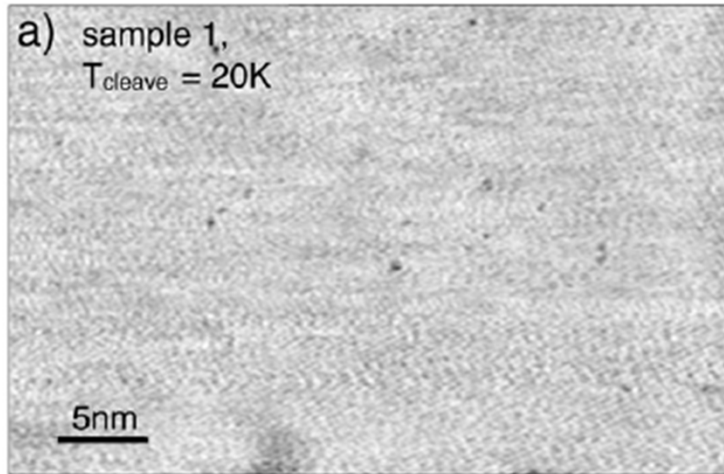
A. Damascelli *et al.*, PRL **85**, 5194 (2000)



$\text{Sr}_2\text{RuO}_4$  cleaved at 180 K  
 $T=10$  K  $h\nu=28$  eV

# Cleaving-Temperature Dependence of $\text{Sr}_2\text{RuO}_4$ Surfaces

## Temperature dependent STM



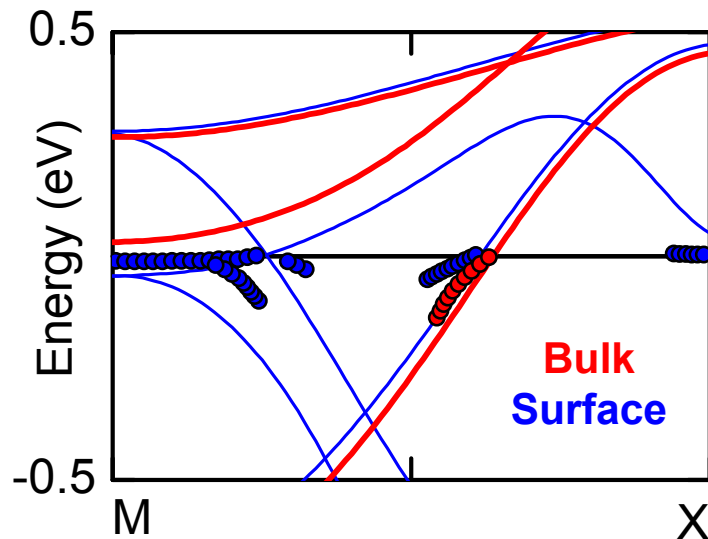
$\sim 0.002$  defects/ $\text{nm}^2$

$0.056 \pm 0.01$  defects/ $\text{nm}^2$

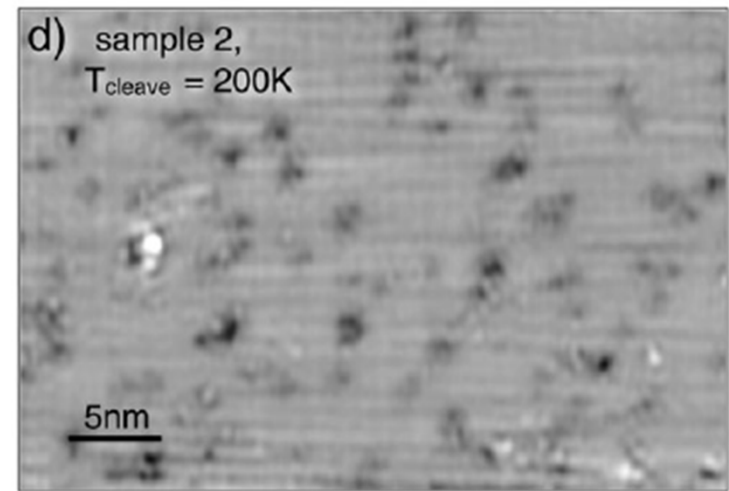
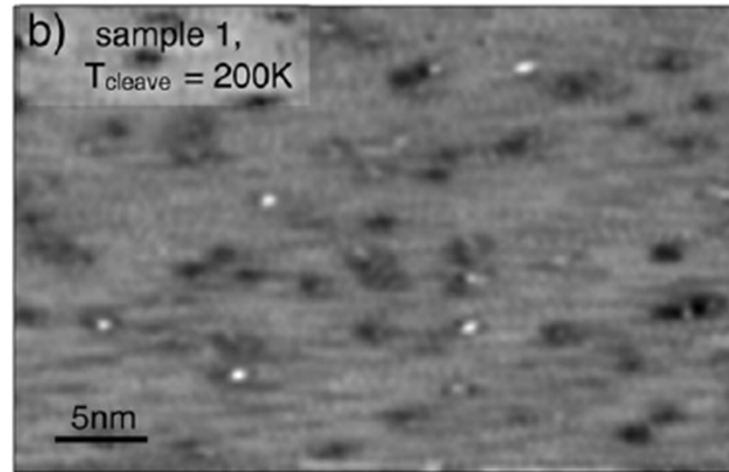
# Cleaving-Temperature Dependence of $\text{Sr}_2\text{RuO}_4$ Surfaces

## Temperature dependent STM

Larger scattering for surface ARPES features



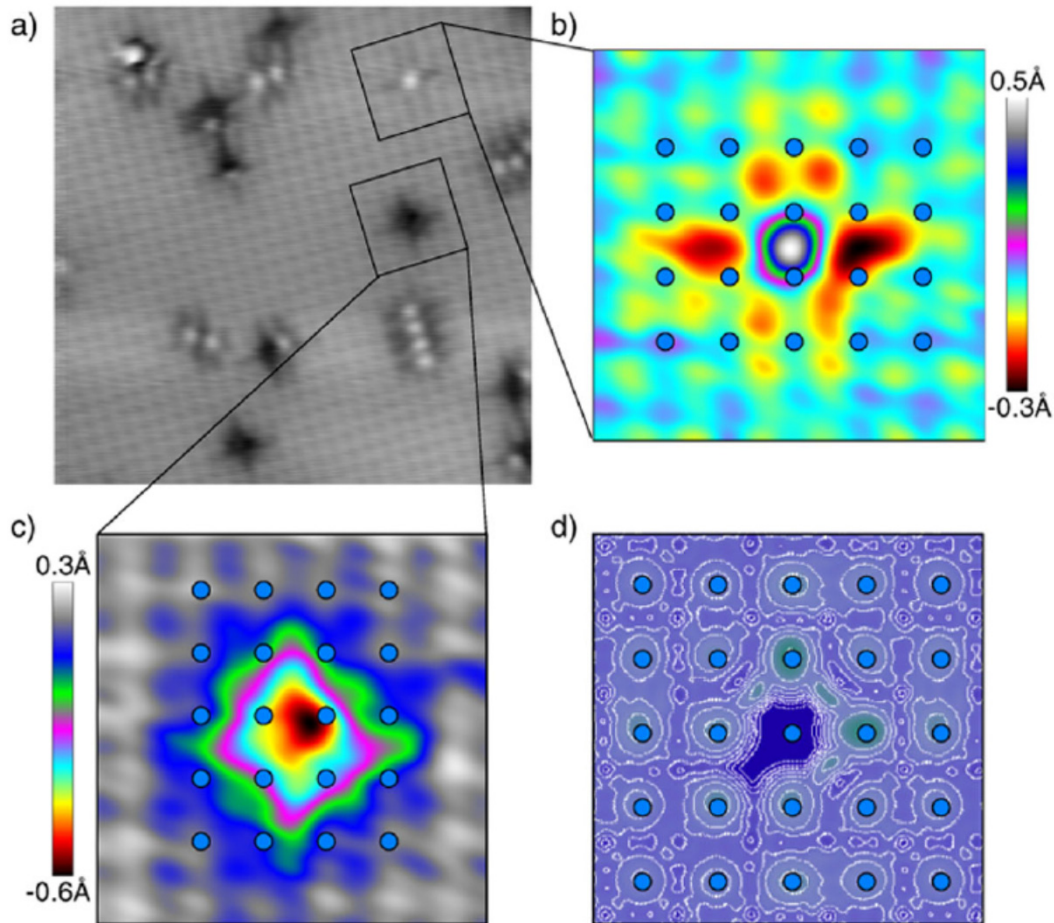
K.M. Shen, A. Damascelli *et al.*,  
PRB **64**, 180502(R) (2001)



$0.056 \pm 0.01$  defects/ $\text{nm}^2$

# Cleaving-Temperature Dependence of $\text{Sr}_2\text{RuO}_4$ Surfaces

## Temperature dependent STM



**Two types of defects:**

(b) Protrusion

(c) Hole

**Blue dots:** Sr locations on the SrO surface termination.

(d) **Charge density:**

DFT calculated contour at a height of 2.13 Å, for a missing charge neutral SrO molecule.



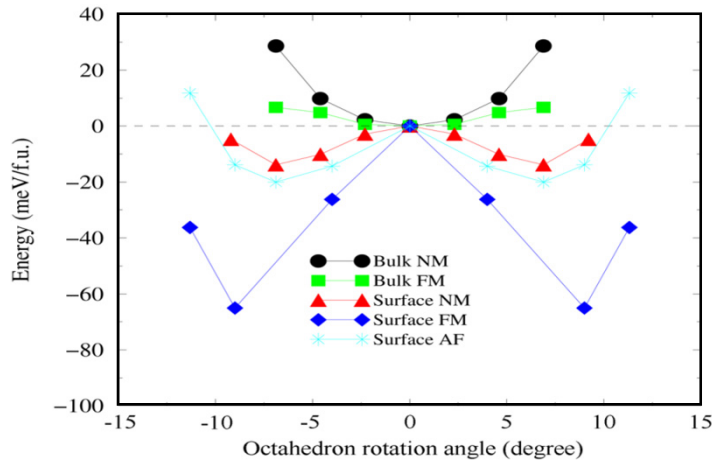
# Surface Ferromagnetism in $\text{Sr}_2\text{RuO}_4$ ?

## Surface Reconstruction $\longleftrightarrow$ Surface Ferromagnetism

R. Matzdorf, Z. Fang, et al., Science **289**, 746 (2000)

### First principle calculations

- **NM surface**: rotation of  $\text{RuO}_6$  ( $R=6.5^\circ$ )
- **FM surface**:  $R=9.0^\circ$ ,  $\Delta E=-51\text{meV}$
- GGA favors **FM** in the **bulk** (4meV)

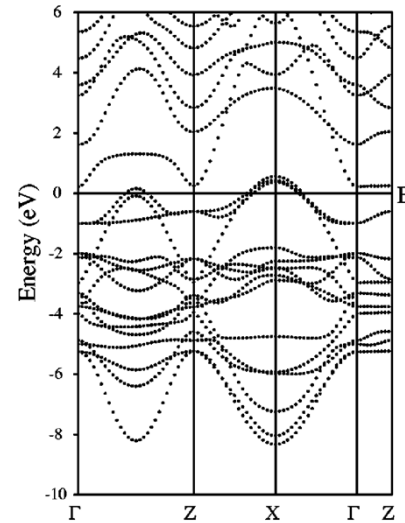


### FM surface

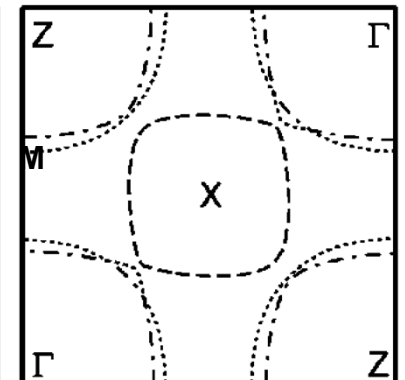
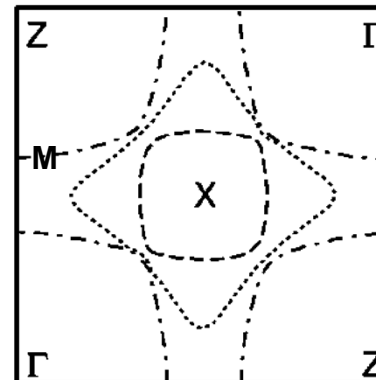
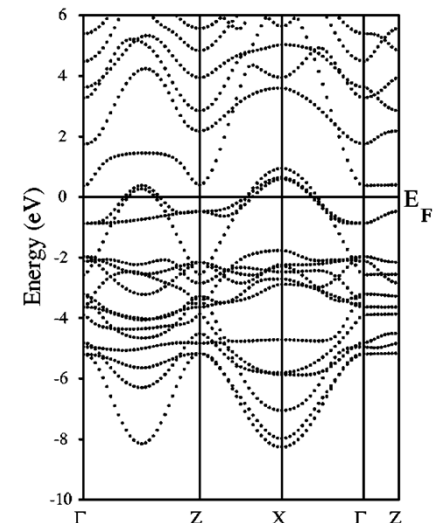
Exchange splitting: **500 meV**  
Magnetic moment: **1.0  $\mu_B$ /Ru**

Z. Fang, K. Terakura, PRB **64**, 20509 (2001)

### Majority spin channel



### Minority spin channel



P.K. de Boer et al., PRB **59**, 9894 (1999)

# Superconductivity at the Surface ?

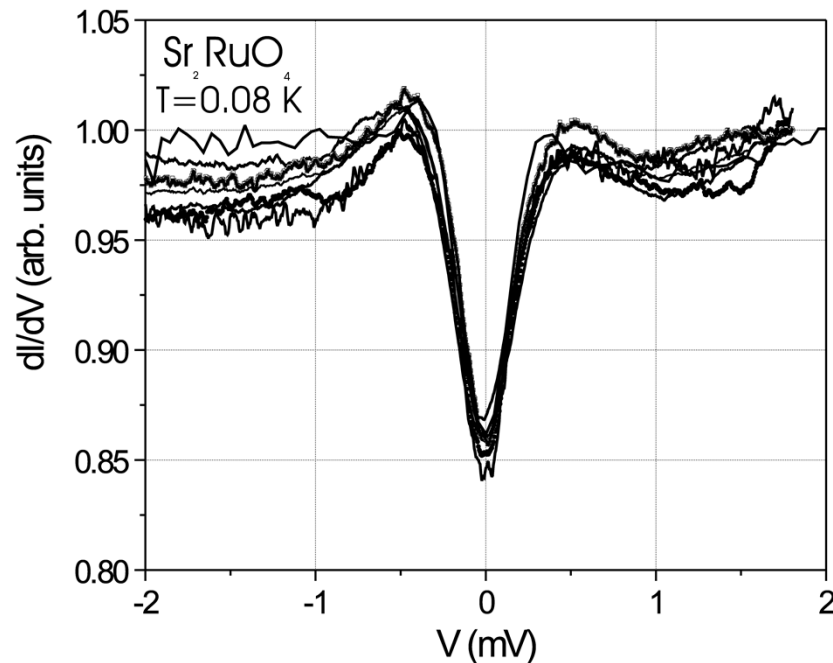
## STM results

M.D. Upward *et al.*, PRB **65**, 220512 (2002)

DOS suppression within 500  $\mu\text{V}$

Gap closes for  $T > 1.5\text{K}$  ;  $B > 700\text{G}$

$$2\Delta_{\text{max}}/kT_{\text{c}} \sim 8.0$$

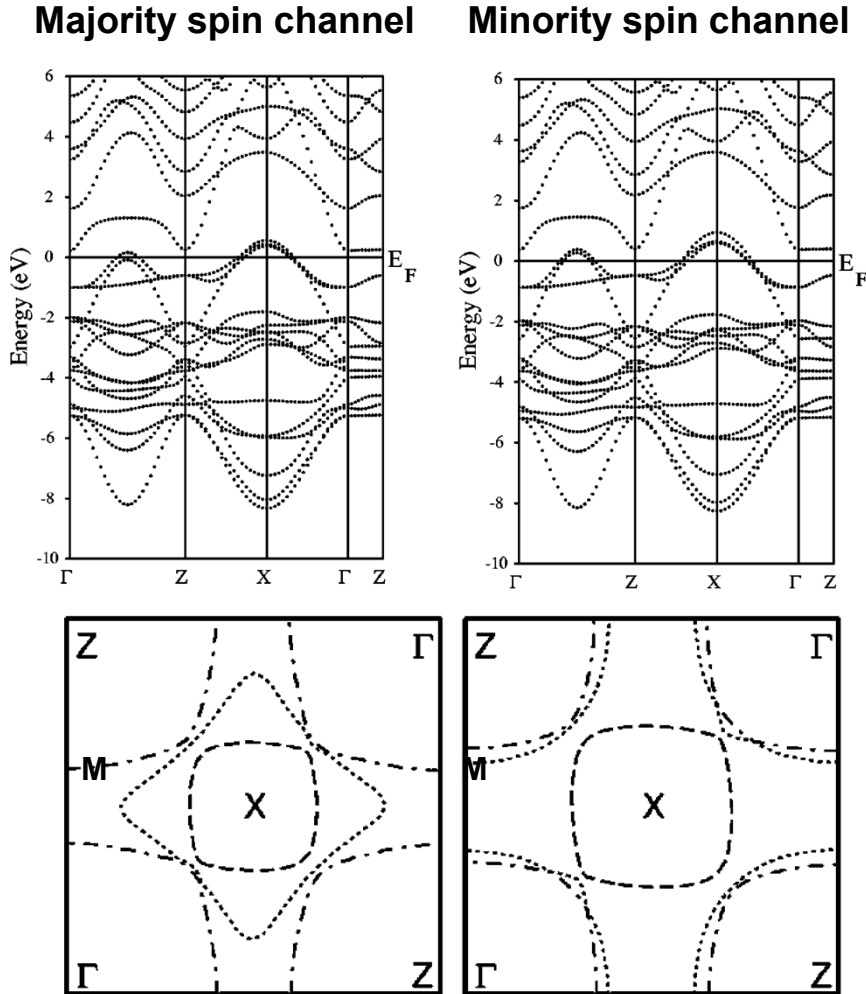


► Opening of a SC gap ◀

# Surface Ferromagnetism in $\text{Sr}_2\text{RuO}_4$ ?

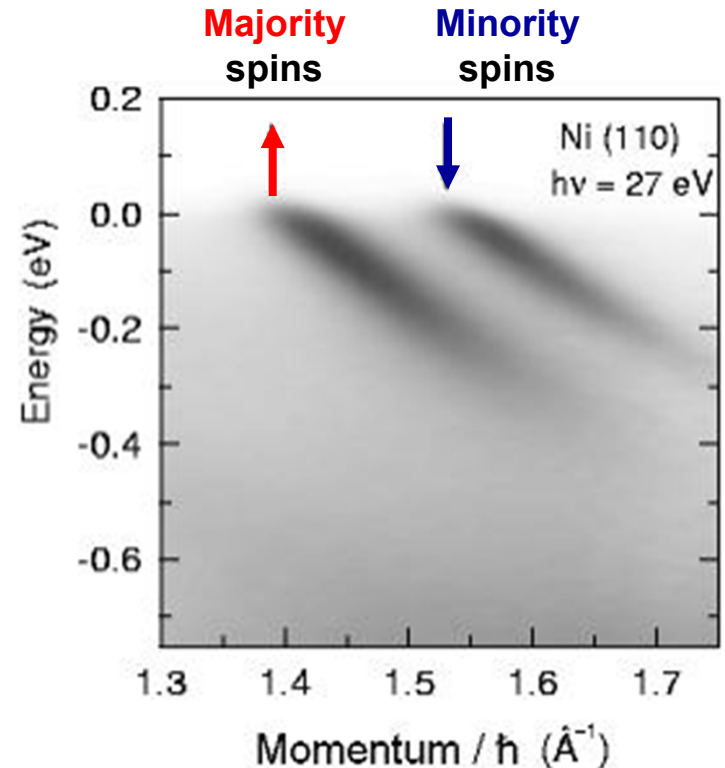
## Surface Reconstruction $\longleftrightarrow$ Surface Ferromagnetism

R. Matzdorf, Z. Fang, et al., Science **289**, 746 (2000)



P.K. de Boer *et al.*, PRB **59**, 9894 (1999)

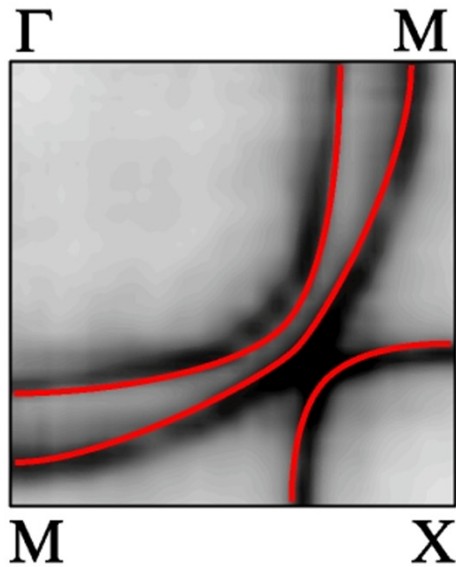
## Spin-split Fermi-level crossings of the conduction band in Ni



Petrovykh *et al.*, APL **73**, 3459 (1998)

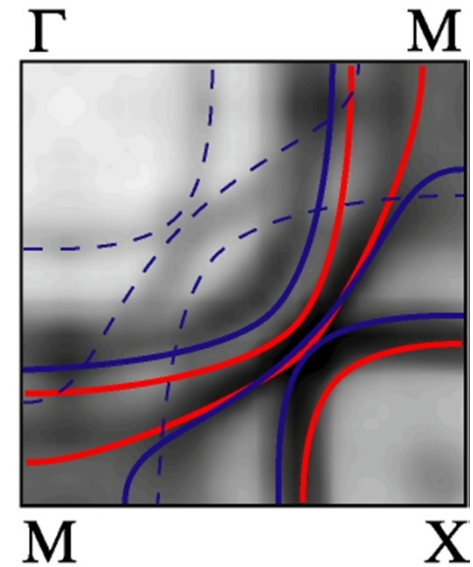
# Bulk and Surface FS of $\text{Sr}_2\text{RuO}_4$

Hot cleave  
 $T=180\text{ K}$



Bulk

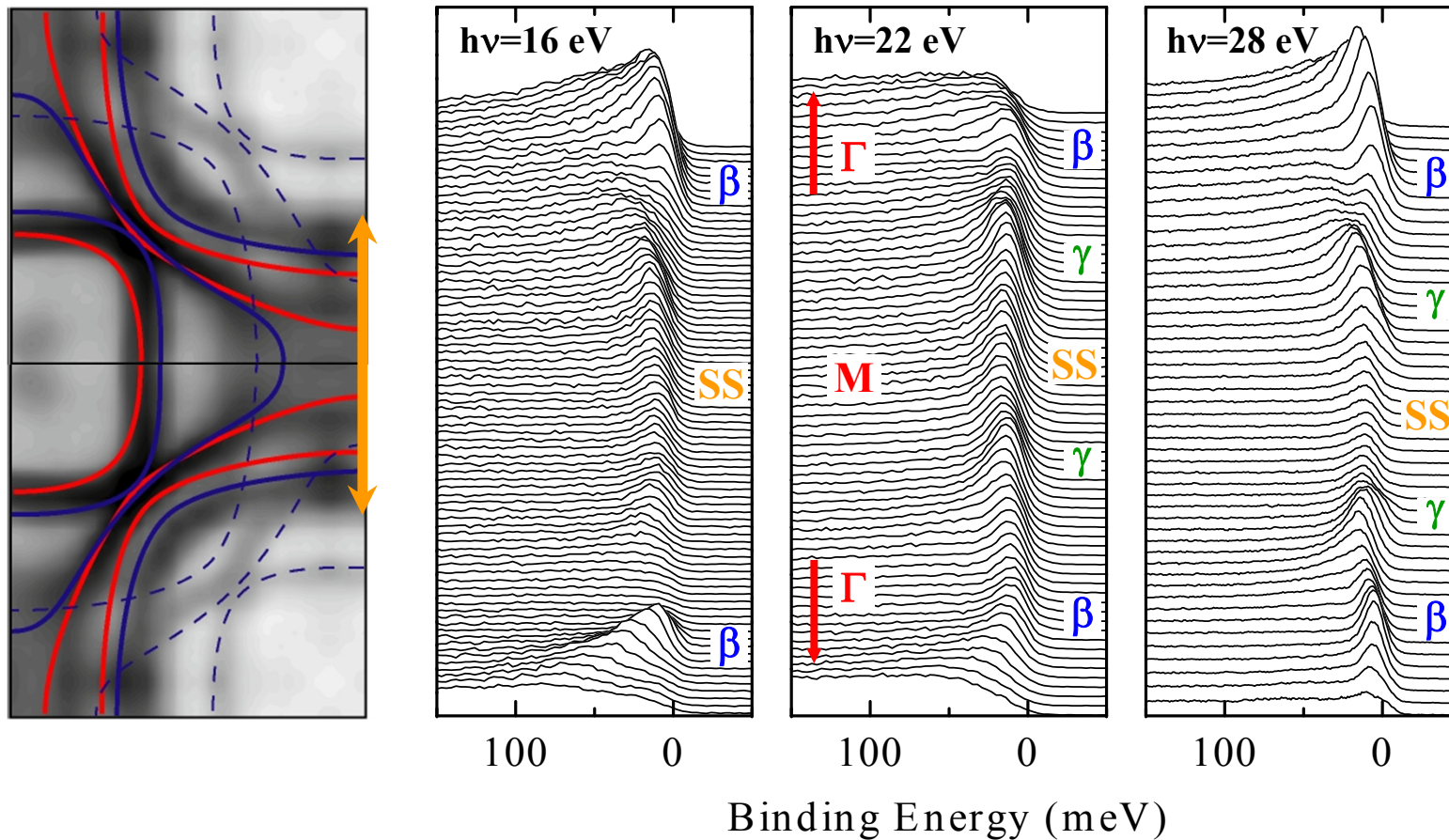
Cold cleave  
 $T=10\text{ K}$



Bulk  
Surface

**Bulk** and **reconstructed surface** features  
NO evidence for surface ferromagnetism

# Photon Energy Dependence in $\text{Sr}_2\text{RuO}_4$



# What is the role of spin-orbit coupling in Ru-oxides? In $\text{Sr}_2\text{RuO}_4$ it has been effectively mostly ignored!

PRL **101**, 026406 (2008)

PHYSICAL REVIEW LETTERS

week ending  
11 JULY 2008

## **Strong Spin-Orbit Coupling Effects on the Fermi Surface of $\text{Sr}_2\text{RuO}_4$ and $\text{Sr}_2\text{RhO}_4$**

M. W. Haverkort,<sup>1</sup> I. S. Elfimov,<sup>2</sup> L. H. Tjeng,<sup>1</sup> G. A. Sawatzky,<sup>2</sup> and A. Damascelli<sup>2</sup>

<sup>1</sup>*II. Physikalisches Institut, Universität zu Köln, Zùlpicher Straße 77, 50937 Köln, Germany*

<sup>2</sup>*Department of Physics and Astronomy, University of British Columbia, Vancouver, British Columbia, Canada V6T 1Z1*

(Received 29 February 2008; published 11 July 2008)

PRL **101**, 026408 (2008)

PHYSICAL REVIEW LETTERS

week ending  
11 JULY 2008

## **Coulomb-Enhanced Spin-Orbit Splitting: The Missing Piece in the $\text{Sr}_2\text{RhO}_4$ Puzzle**

Guo-Qiang Liu, V. N. Antonov, O. Jepsen, and O. K. Andersen.

*Max-Planck Institut für Festkörperforschung, D-70569 Stuttgart, Germany*

(Received 2 April 2008; published 11 July 2008)

# Eigenstates with Spin-Orbit Coupling

Starting from degenerate  $t_{2g}$  orbitals

$$\sqrt{1/2} (-d_{xz} - i d_{yz}) = d_1$$

$$\sqrt{1/2} (d_{xz} - i d_{yz}) = d_{-1}$$

$$d_{xy}$$

3-orbitals with orbital momentum 0, +/- 1  
like  $p$ -orbitals

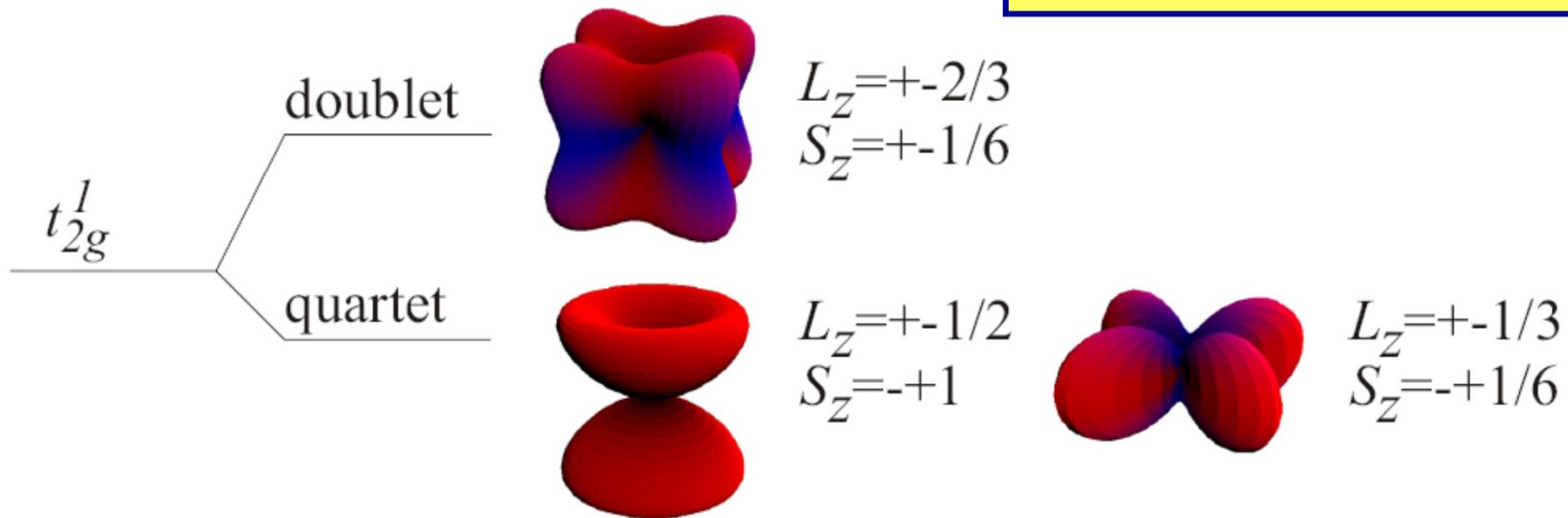
$$H = \zeta \sum_i \mathbf{l}_i \cdot \mathbf{s}_i$$

Atomic relativistic SOC

$$\text{Ru}^{4+} \quad \zeta = 161 \text{ meV}$$

$$\text{Rh}^{4+} \quad \zeta = 191 \text{ meV}$$

Earnshaw, JCS **601**, 3132 (1961)





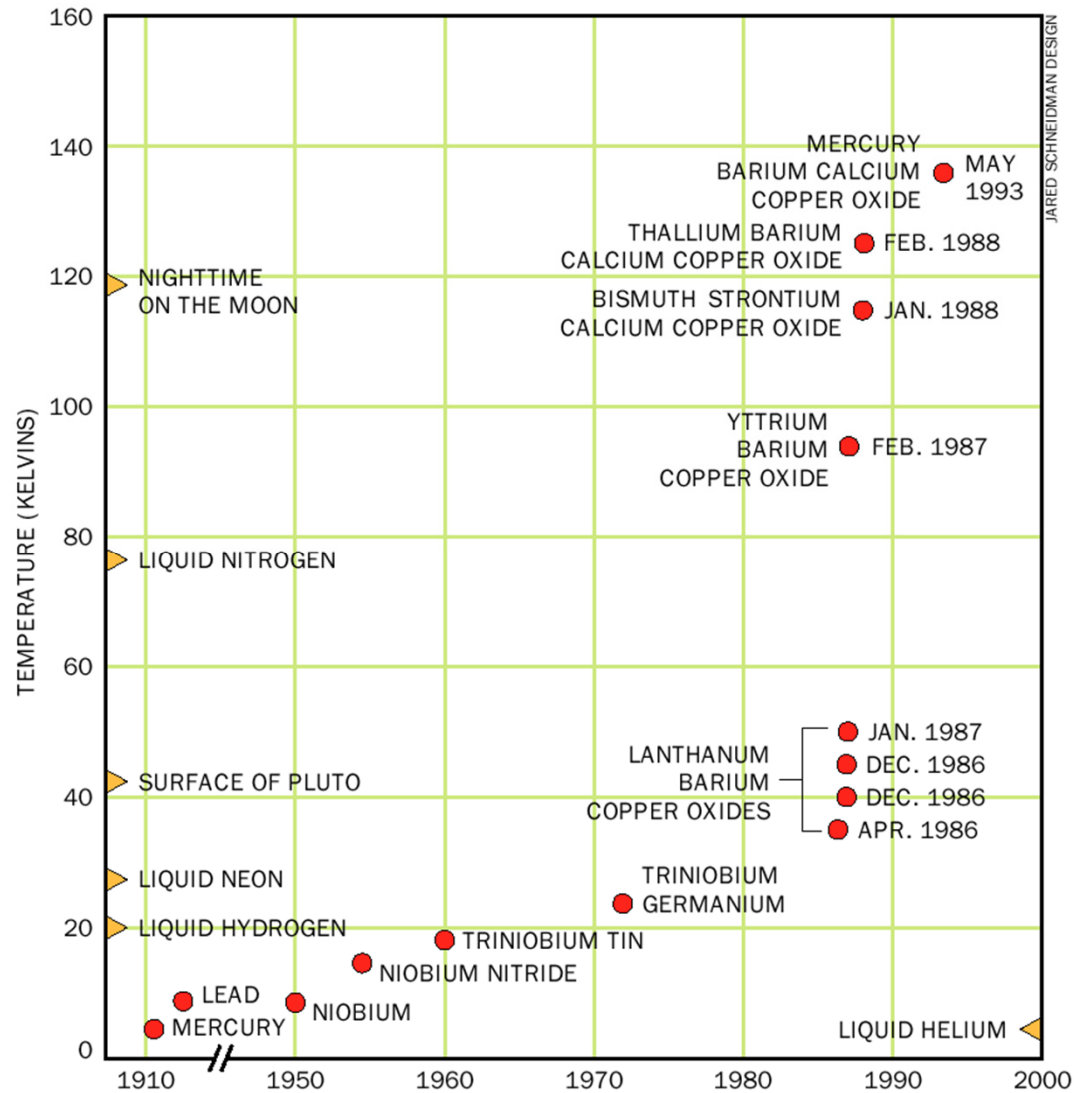
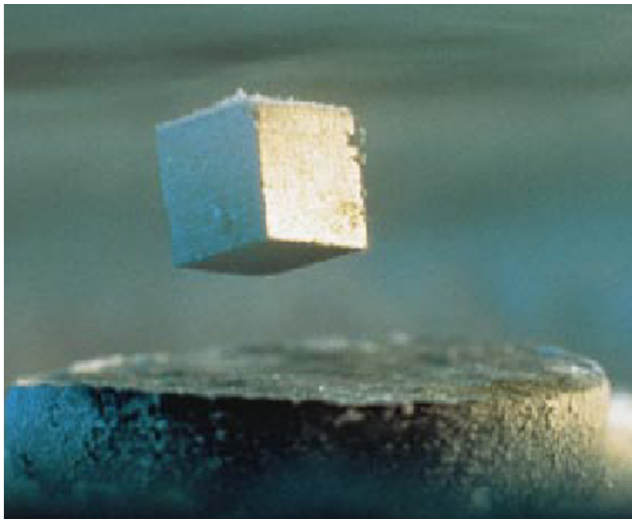
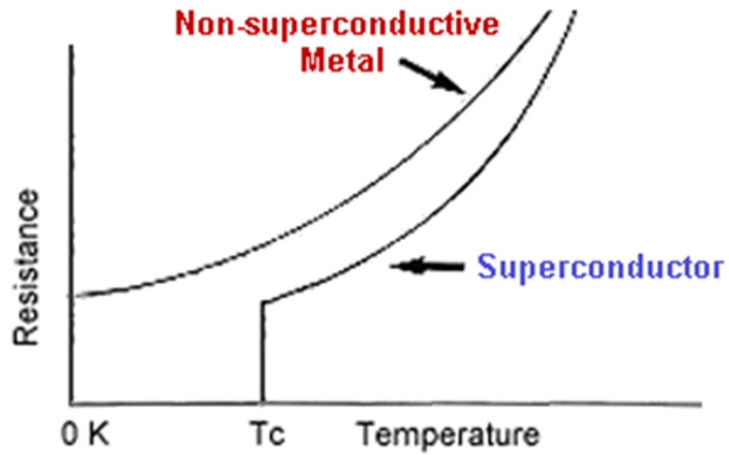
# Outline Part I

## Superconducting gap: BCS and HTSC

CUSO Lecture – Lausanne 02/2011

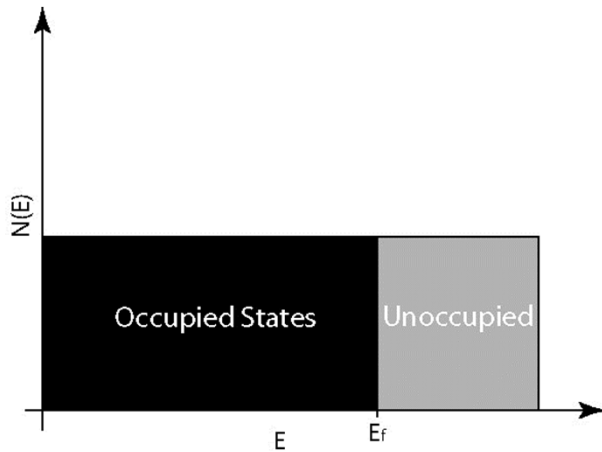


# Superconductivity

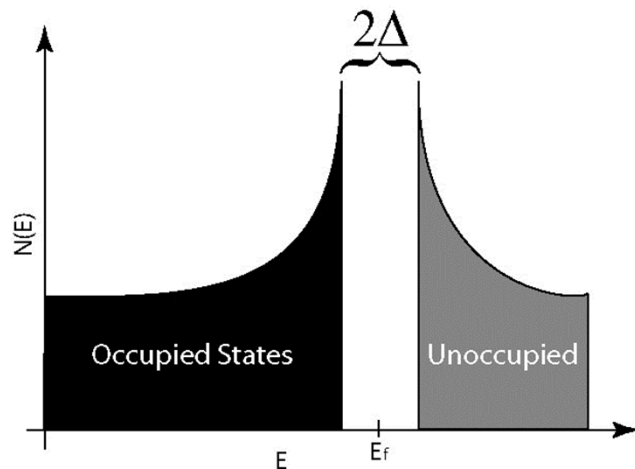


# “Classic Low-temperature” Superconductors

Metallic Density of States



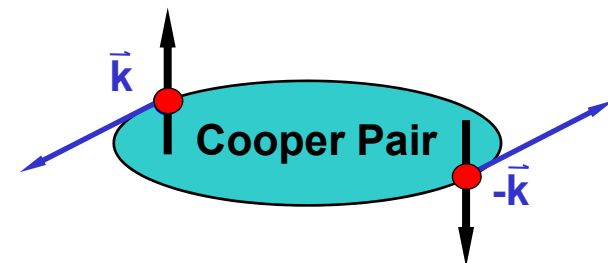
Superconducting Density of States



**Superconductivity** can only be seen on low energy scales and needs **high resolution!**

## Superconductivity

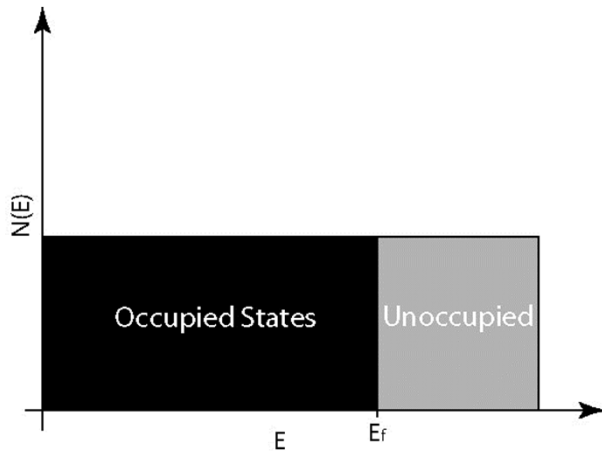
2-electron  
bound state



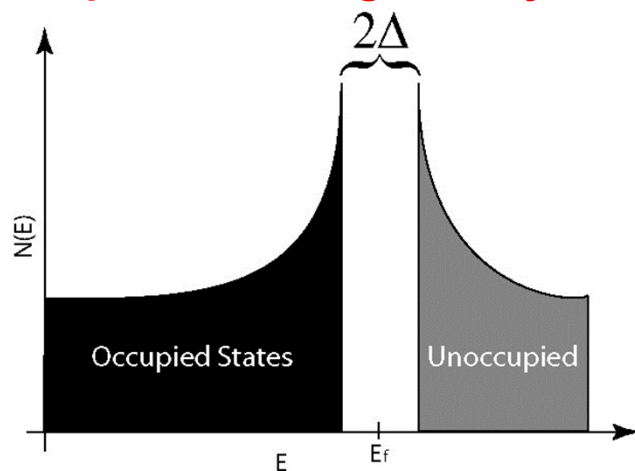
spin-singlet pairing

# “Classic Low-temperature” Superconductors

## Metallic Density of States

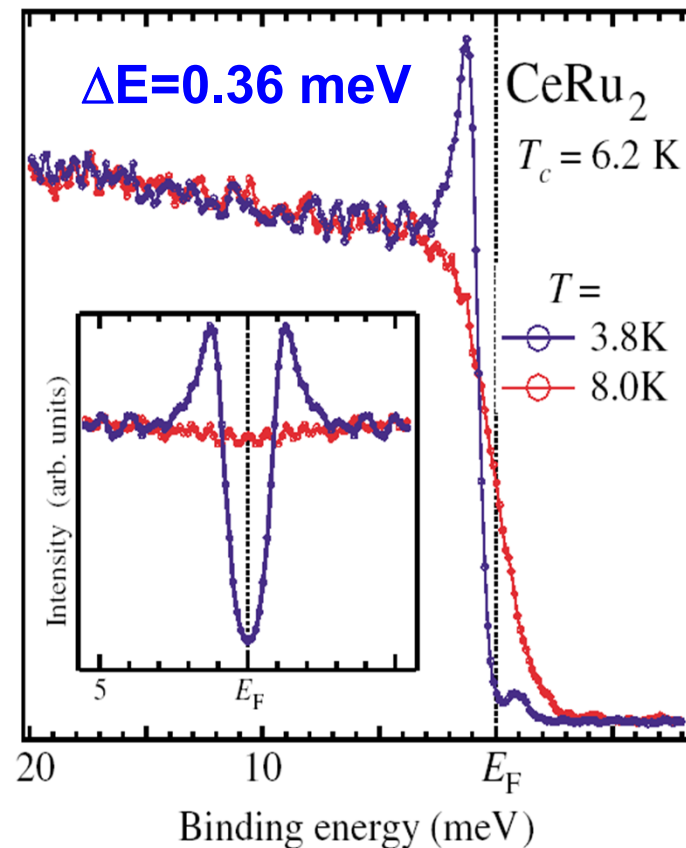


## Superconducting Density of States



**Superconductivity** can only be seen on low energy scales and needs **high resolution!**

Kiss et al., PRL **94**, 057001 (2005)



# High-Temperature Superconductors

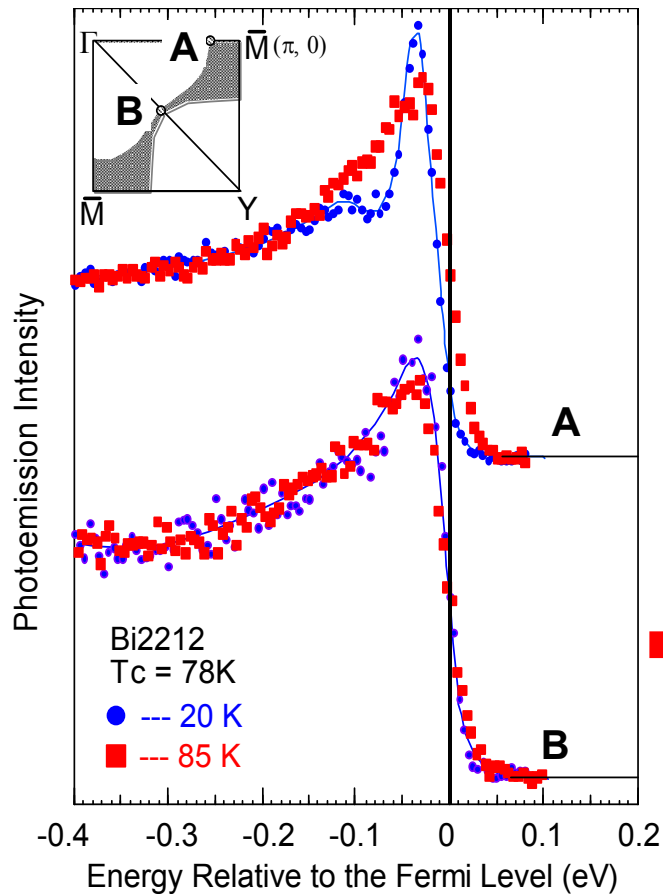
VOLUME 70, NUMBER 10

PHYSICAL REVIEW LETTERS

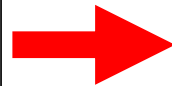
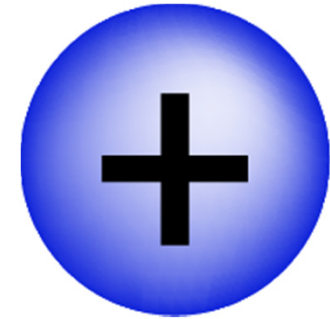
8 MARCH 1993

## Anomalous Large Gap Anisotropy in the $a$ - $b$ Plane of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

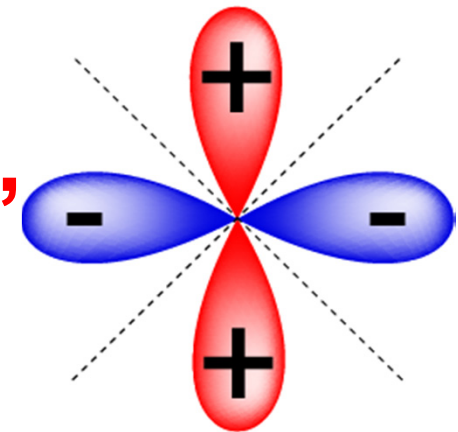
Z.-X. Shen,<sup>(1),(2)</sup> D. S. Dessau,<sup>(1),(2)</sup> B. O. Wells,<sup>(1),(2),(a)</sup> D. M. King,<sup>(2)</sup> W. E. Spicer,<sup>(2)</sup> A. J. Arko,<sup>(3)</sup>  
D. Marshall,<sup>(2)</sup> L. W. Lombardo,<sup>(1)</sup> A. Kapitulnik,<sup>(1)</sup> P. Dickinson,<sup>(1)</sup> S. Doniach,<sup>(1)</sup> J. DiCarlo,<sup>(1),(2)</sup>  
A. G. Loeser,<sup>(1),(2)</sup> and C. H. Park<sup>(1),(2)</sup>



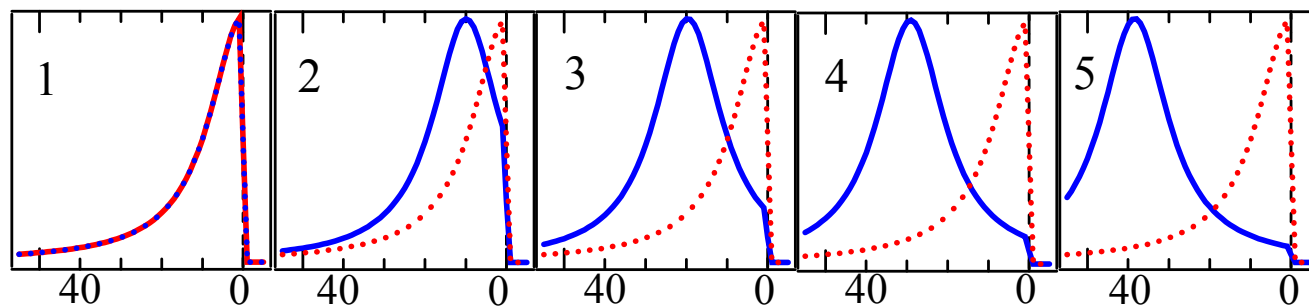
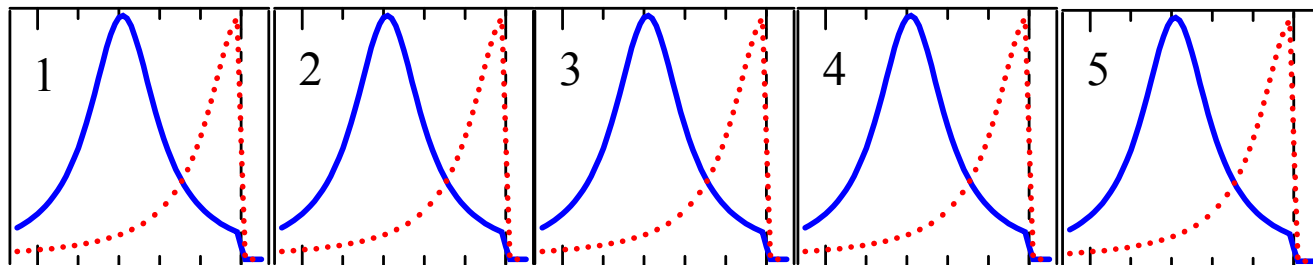
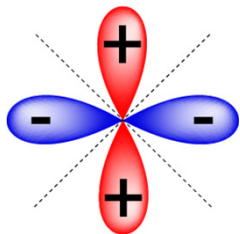
“s-wave”



“d-wave”

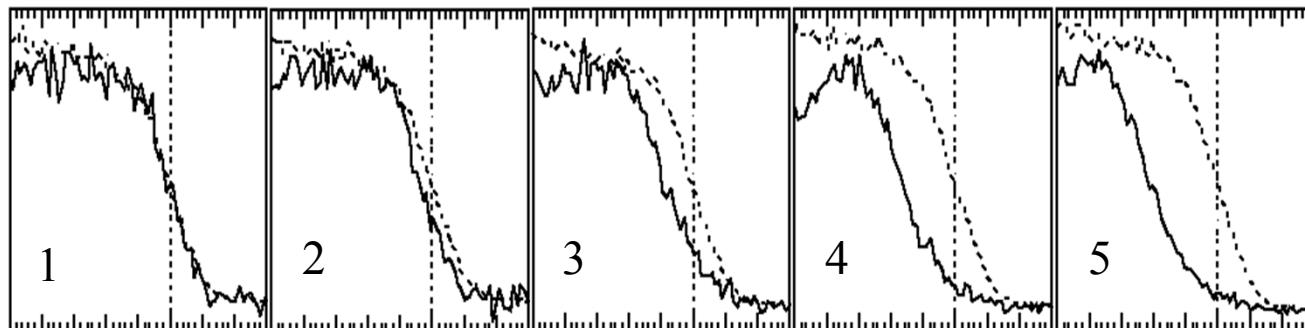
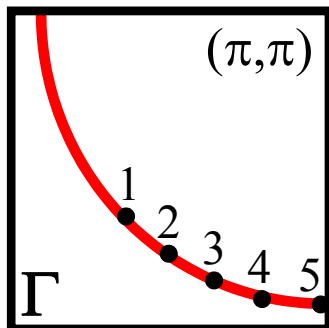


# High-Tc Superconductors: s-wave vs. d-wave gap



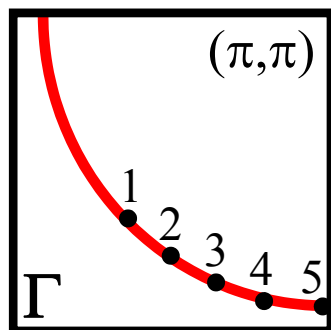
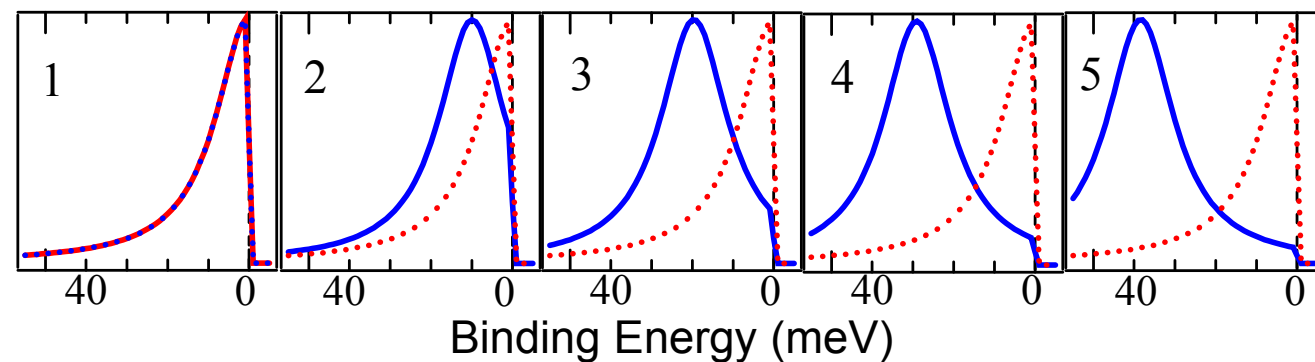
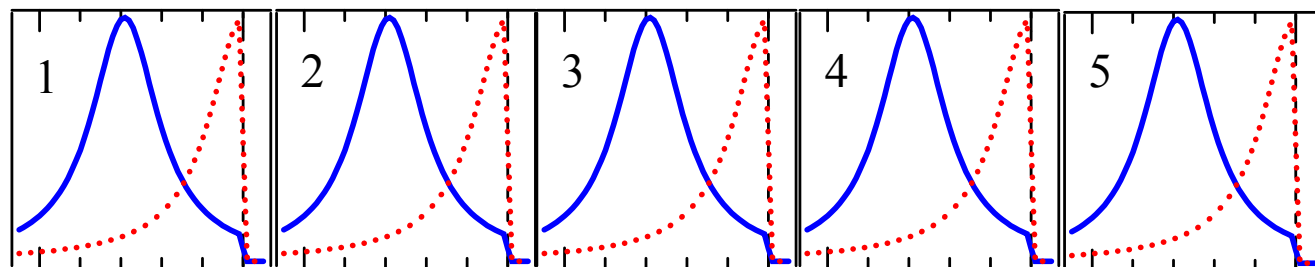
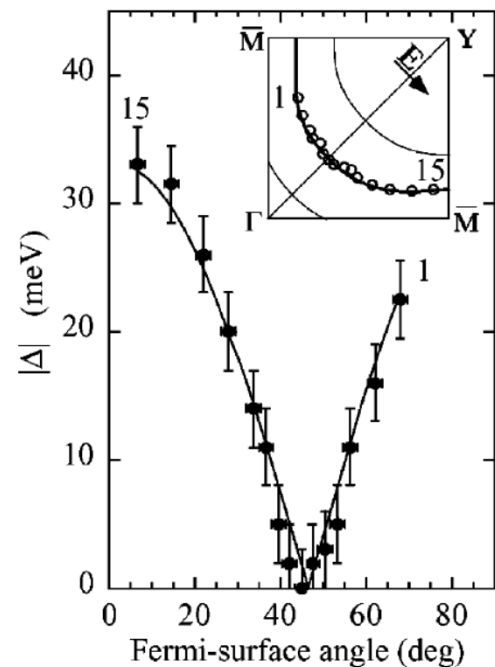
Binding Energy (meV)

Ding et al. PRB **54**, R9678 (1996)

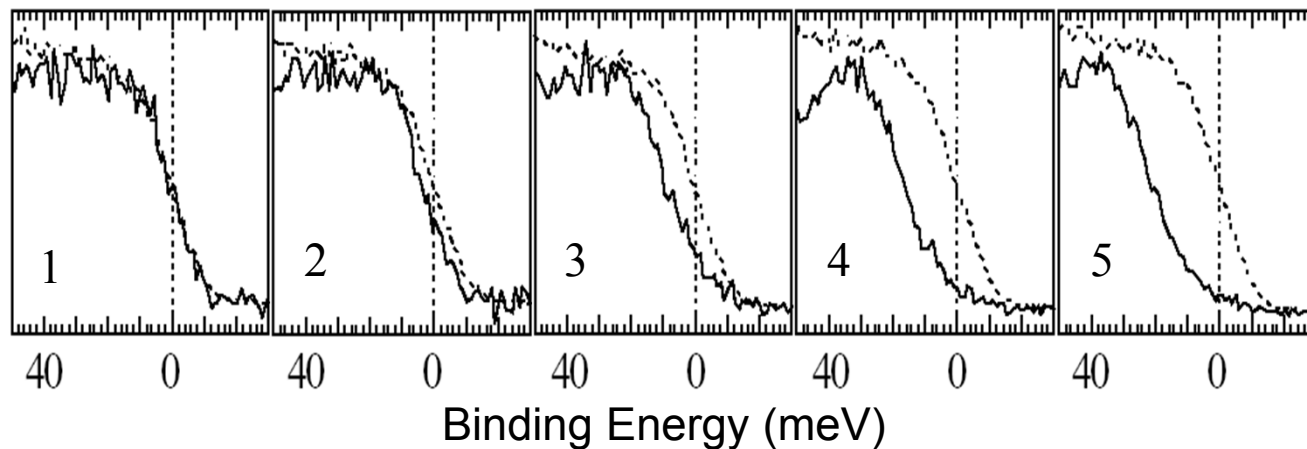


Binding Energy (meV)

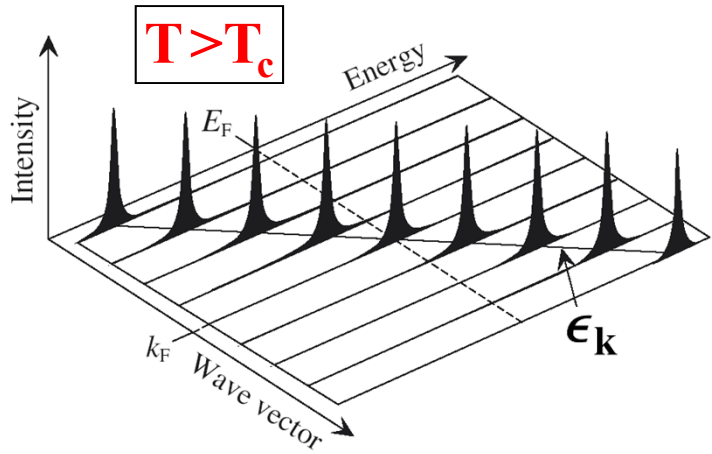
# High-Tc Superconductors: s-wave vs. d-wave gap



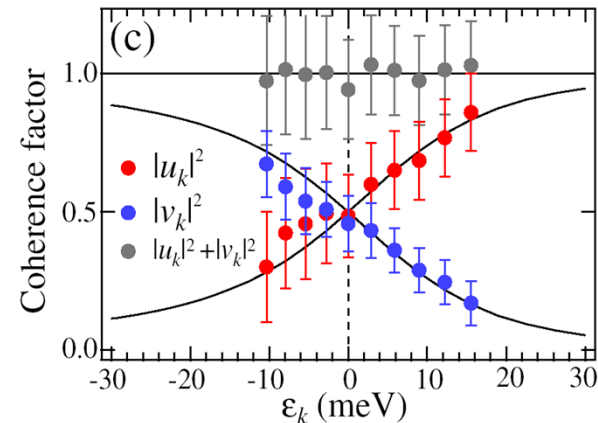
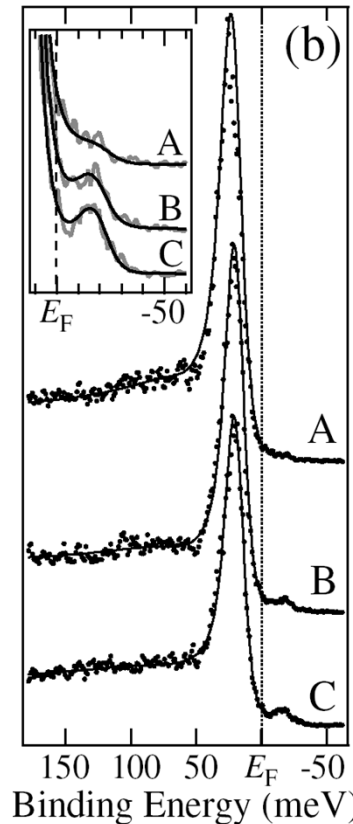
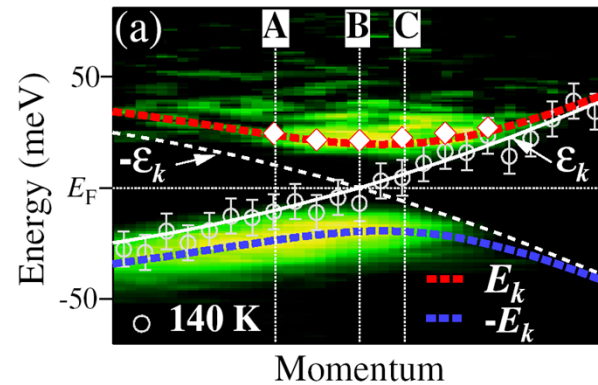
Ding et al. PRB **54**, R9678 (1996)



# High-Tc Superconductors: Bogoliubov QP in Bi2223

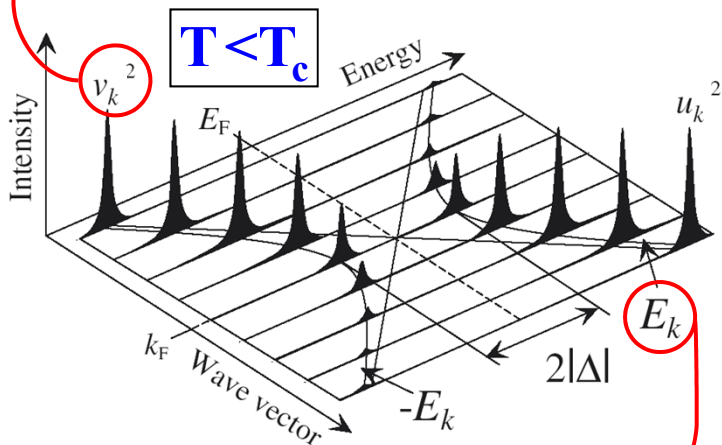


$$A_{\text{BCS}}(k, \omega) = \frac{1}{\pi} \left\{ \frac{|u_{\mathbf{k}}|^2 \Gamma}{(\omega - E_{\mathbf{k}})^2 + \Gamma^2} + \frac{|v_{\mathbf{k}}|^2 \Gamma}{(\omega + E_{\mathbf{k}})^2 + \Gamma^2} \right\}$$



Matsui *et al.*, PRL **90**, 217002 (2003)

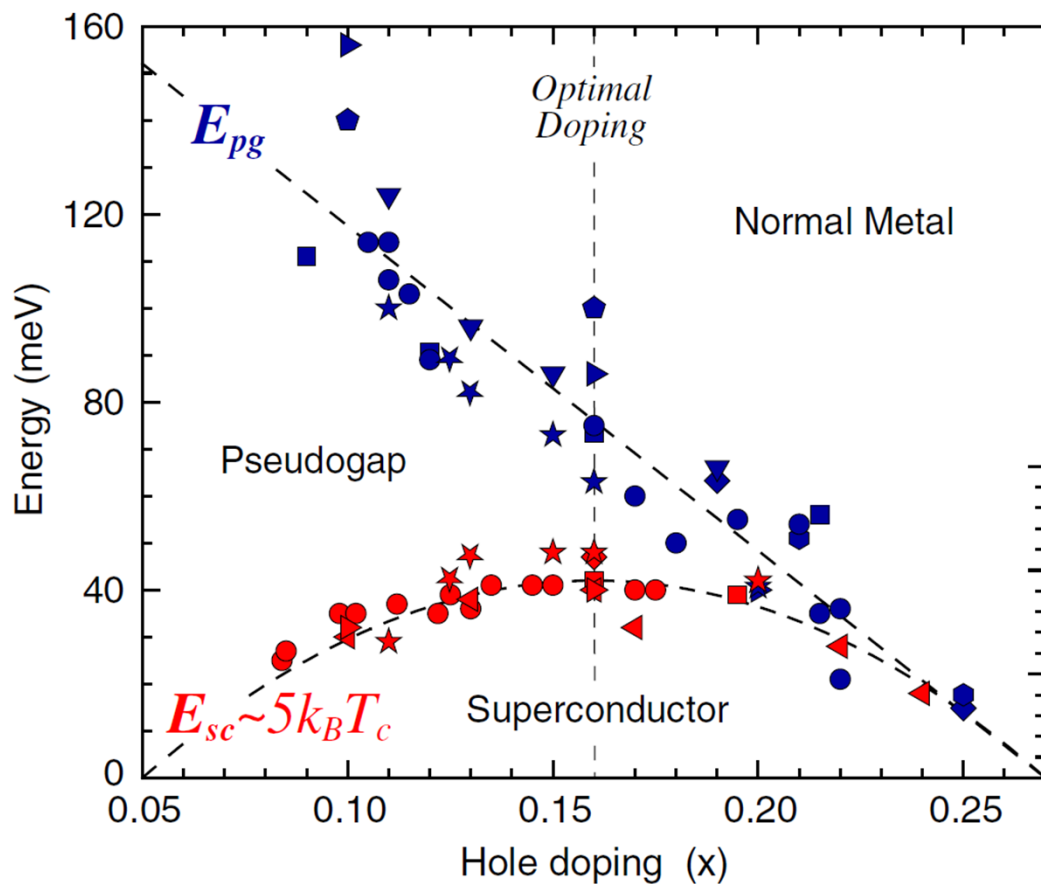
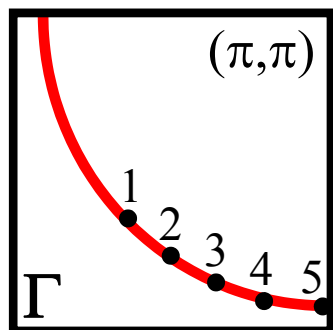
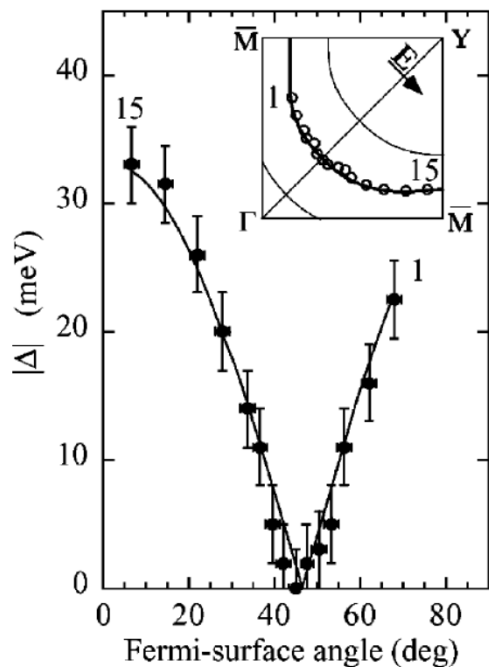
$$v_{\mathbf{k}}^2 = 1 - u_{\mathbf{k}}^2 = \frac{1}{2} \left( 1 - \epsilon_{\mathbf{k}} / E_{\mathbf{k}} \right)$$



$$E_{\mathbf{k}} = \sqrt{\epsilon_{\mathbf{k}}^2 + |\Delta(\mathbf{k})|^2}$$

# High-Tc Superconductors: s-wave vs. d-wave gap

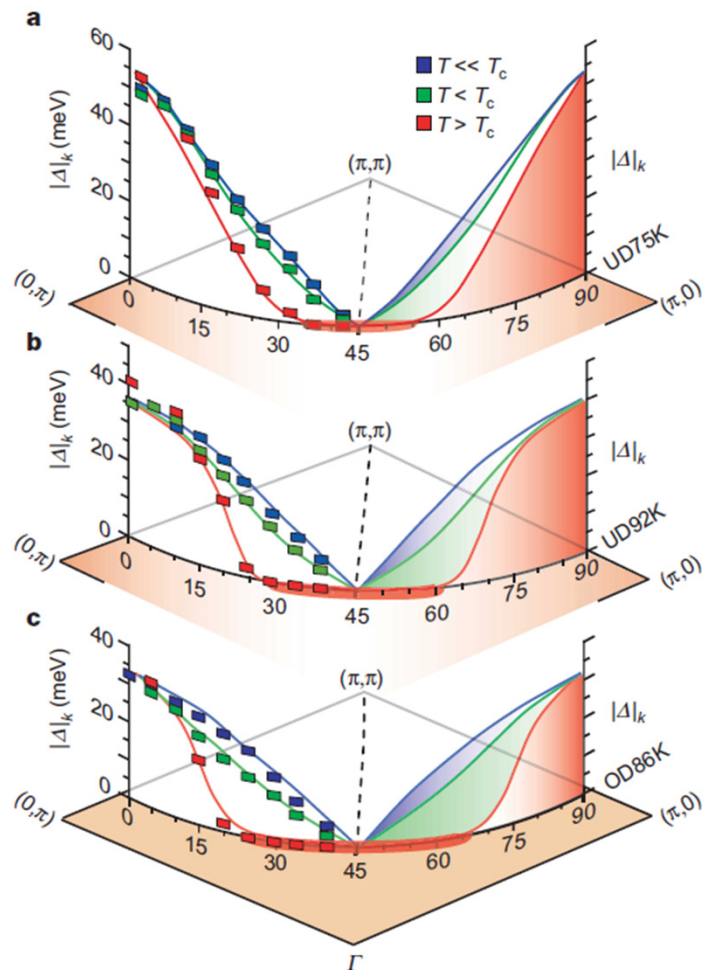
Two gaps make a HTSC?



Hufner, Hossain, Damascelli, Sawatzky  
Rep. Prog. Phys. 71, 062501 (2008)

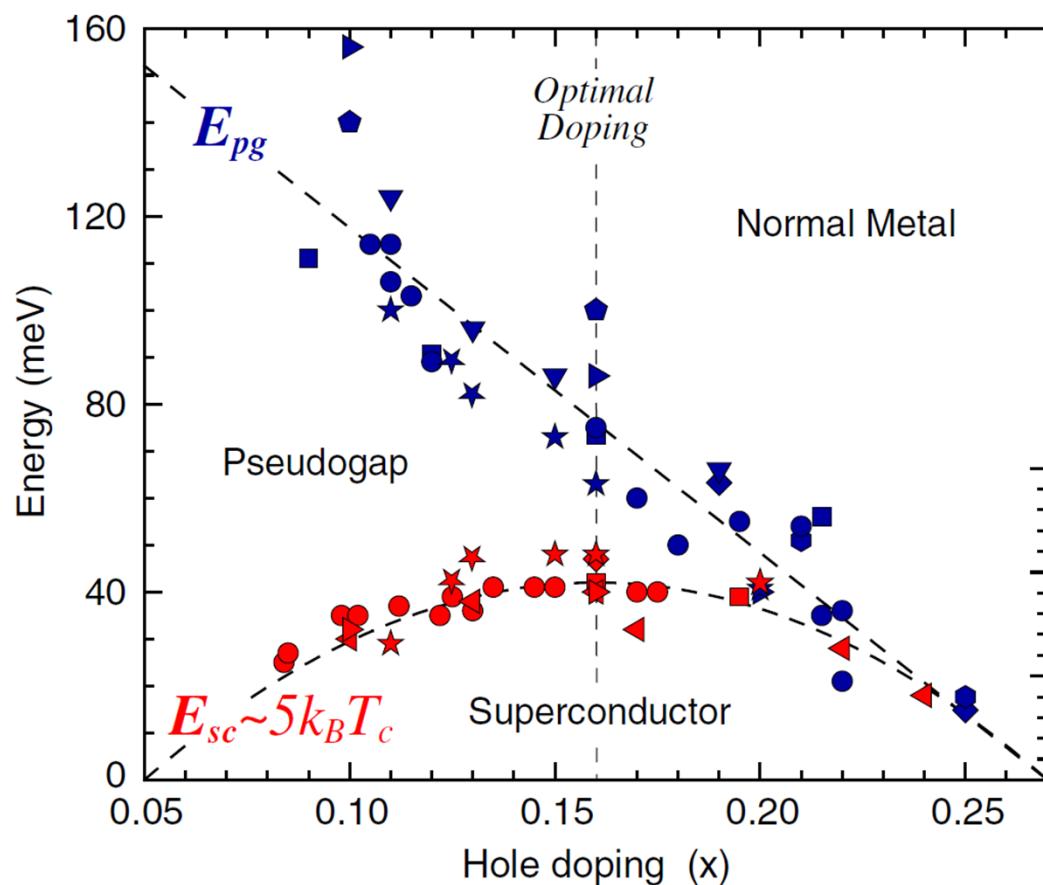


# High-Tc Superconductors: s-wave vs. d-wave gap



W. S. Lee et al., Nature 450, 81 (2007)

## Two gaps make a HTSC?



Hufner, Hossain, Damascelli, Sawatzky  
 Rep. Prog. Phys. 71, 062501 (2008)